

When Your DSL Needs to Support User-Defined *Domain* Functions

Affordable Deep Embeddings via Curry-Howard-Lambek Correspondence

Scaladays MADRID

September 14th, 2023

Tomas Mikula



What This Talk Is About



What This Talk Is About

DSLs



What This Talk Is About

DSLs

external



What This Talk Is About

DSLs

external

- Custom syntax
- Specialized tools
- Good error messages
- Build your own
 - Parser
 - Type checker
 - IDE integration



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- Specialized tools
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What This Talk Is About





What This Talk Is About

DSLs ➔ embedded
(internal)

external

- Constrained syntax
- Not so good error messages
- No custom IDE
- Piggy-back on host language's
 - Parser
 - Type checker
 - IDE integration

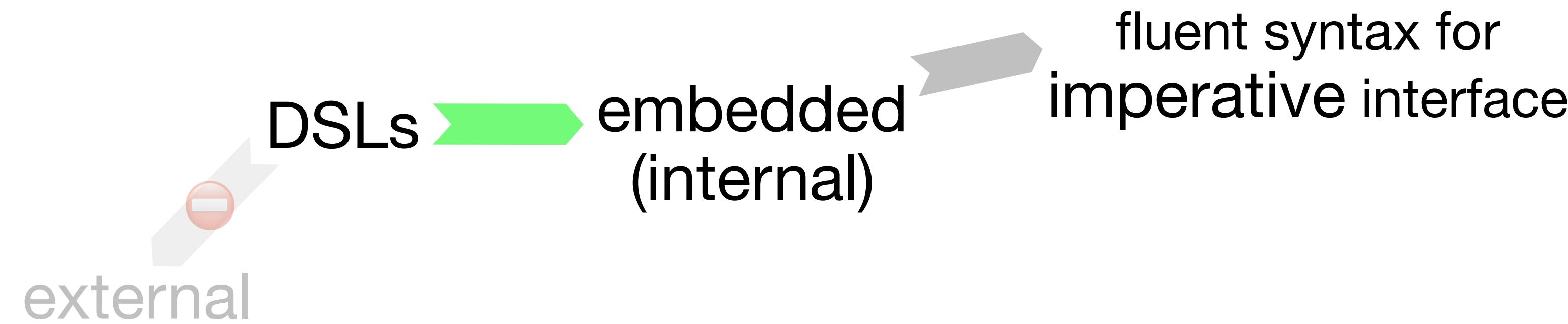


What This Talk Is About



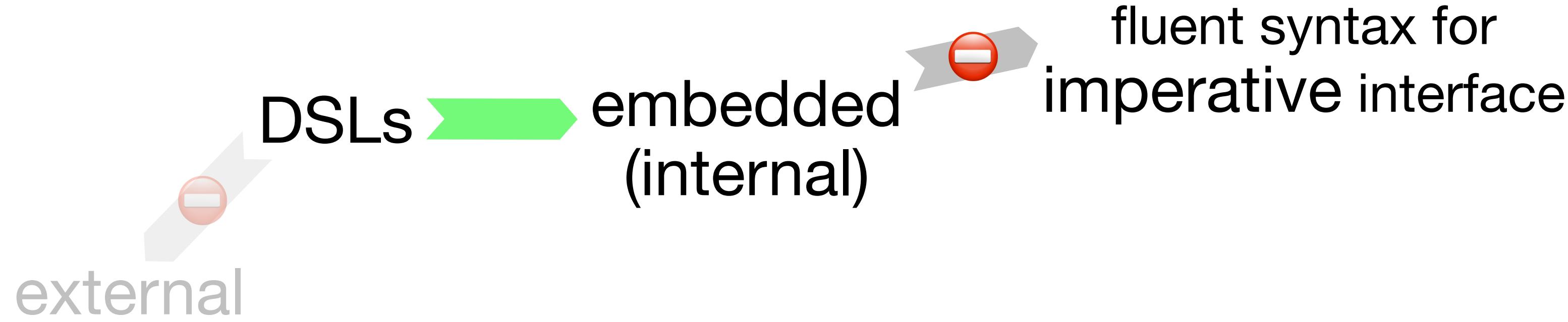


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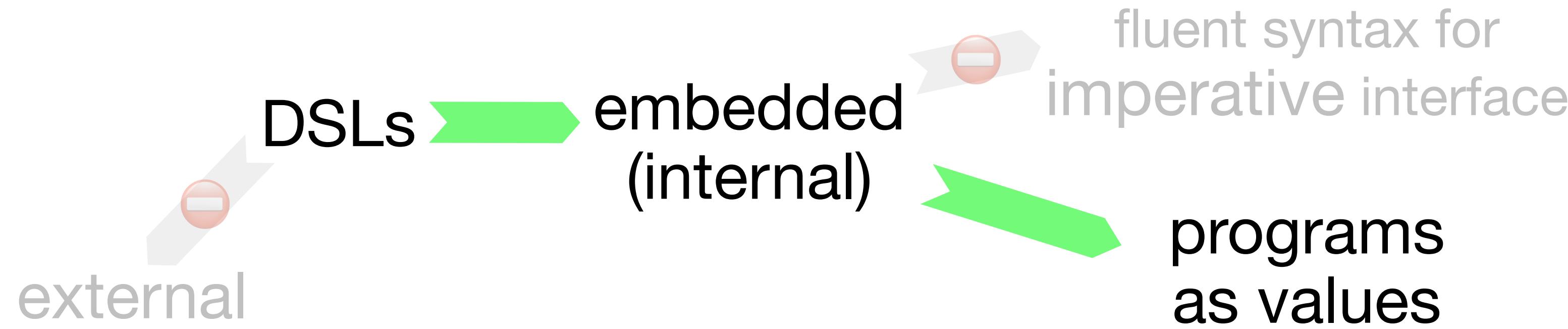


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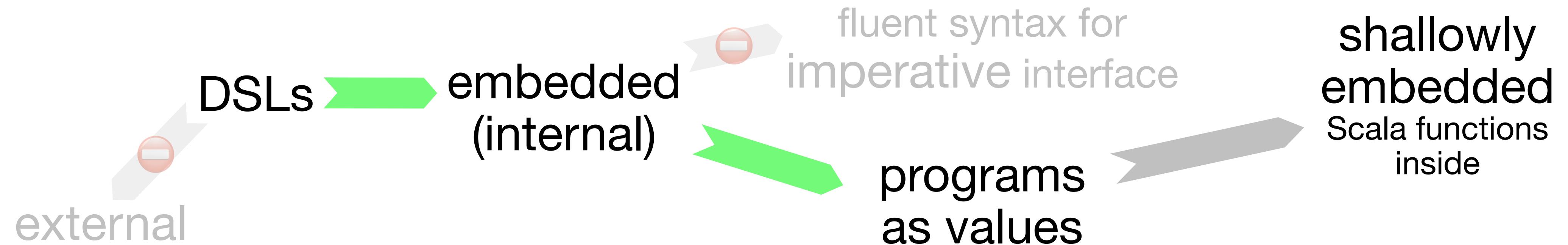


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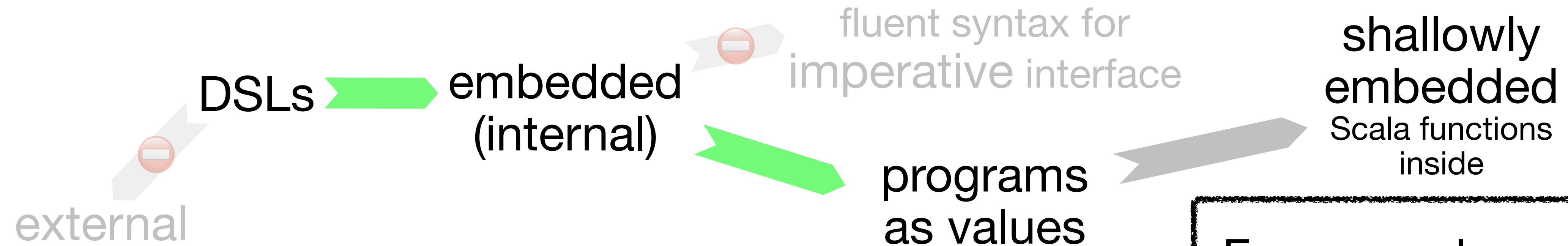


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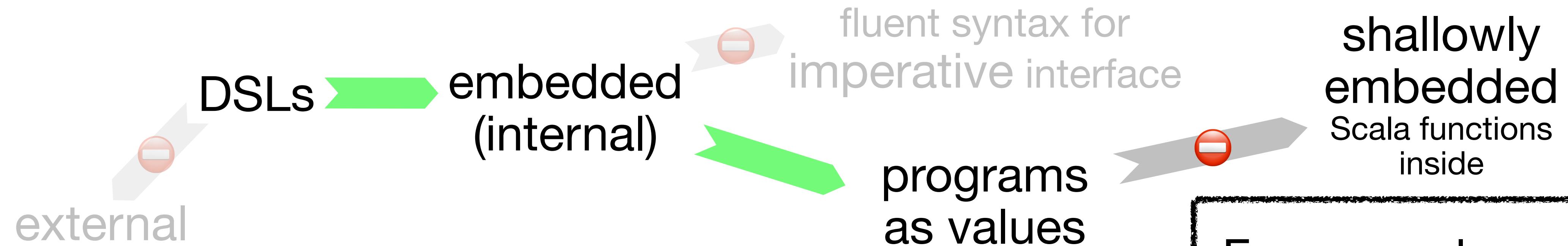


For example

- Parser combinators
- “Monadic” DSLs with deferred evaluation
- Easy to make
- Not introspectable
- Single interpretation
 - i.e. *run them*



What This Talk Is About

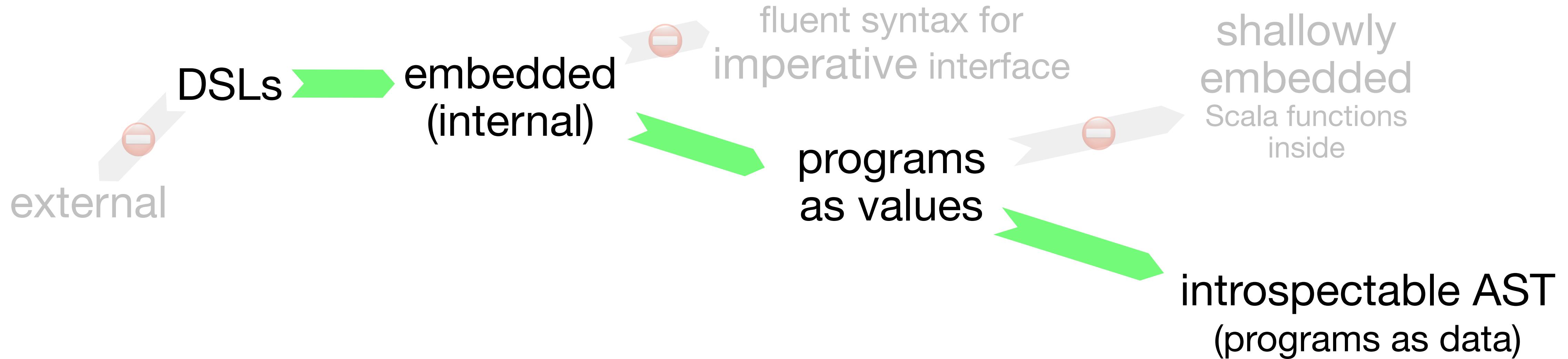


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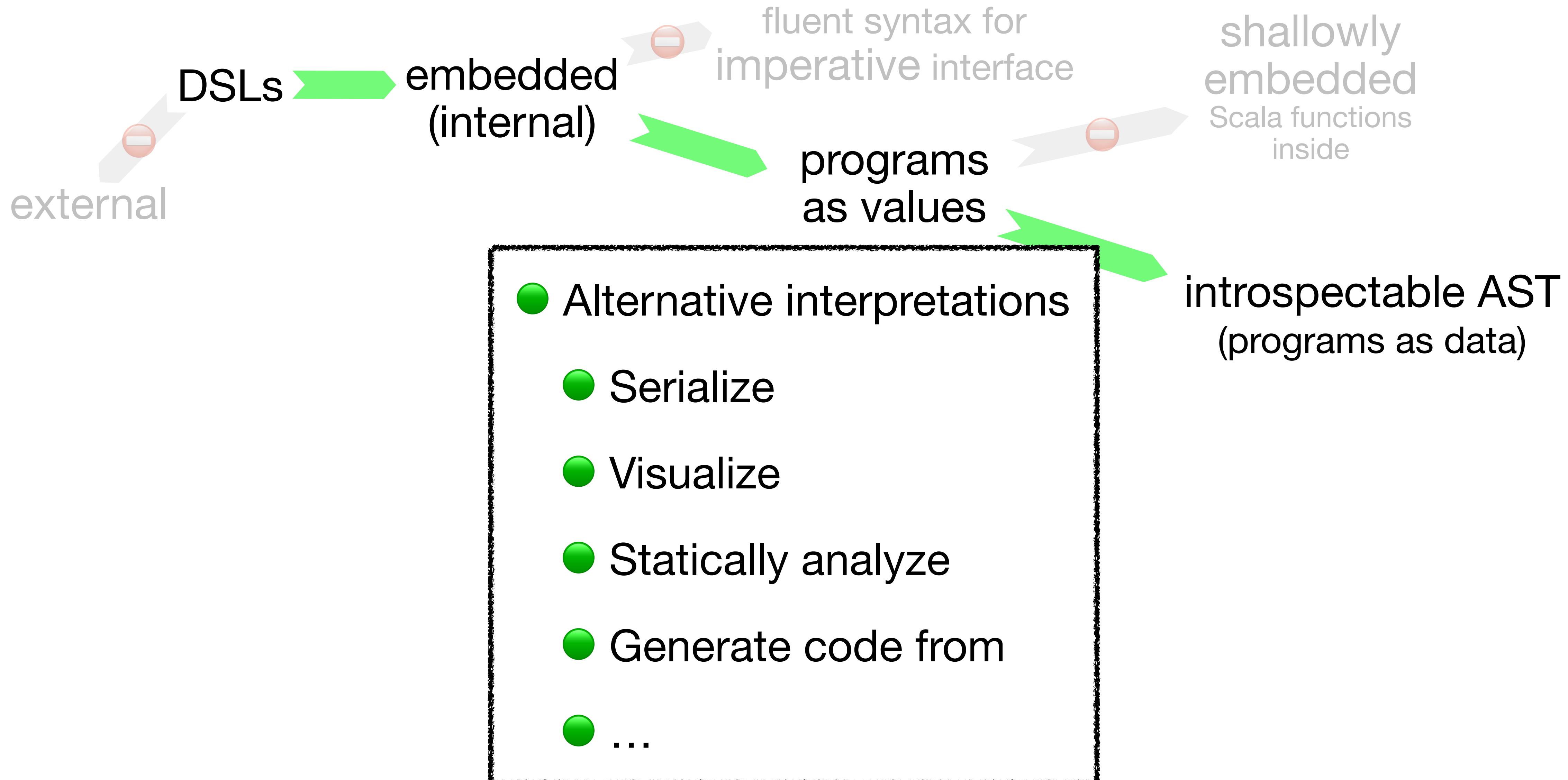


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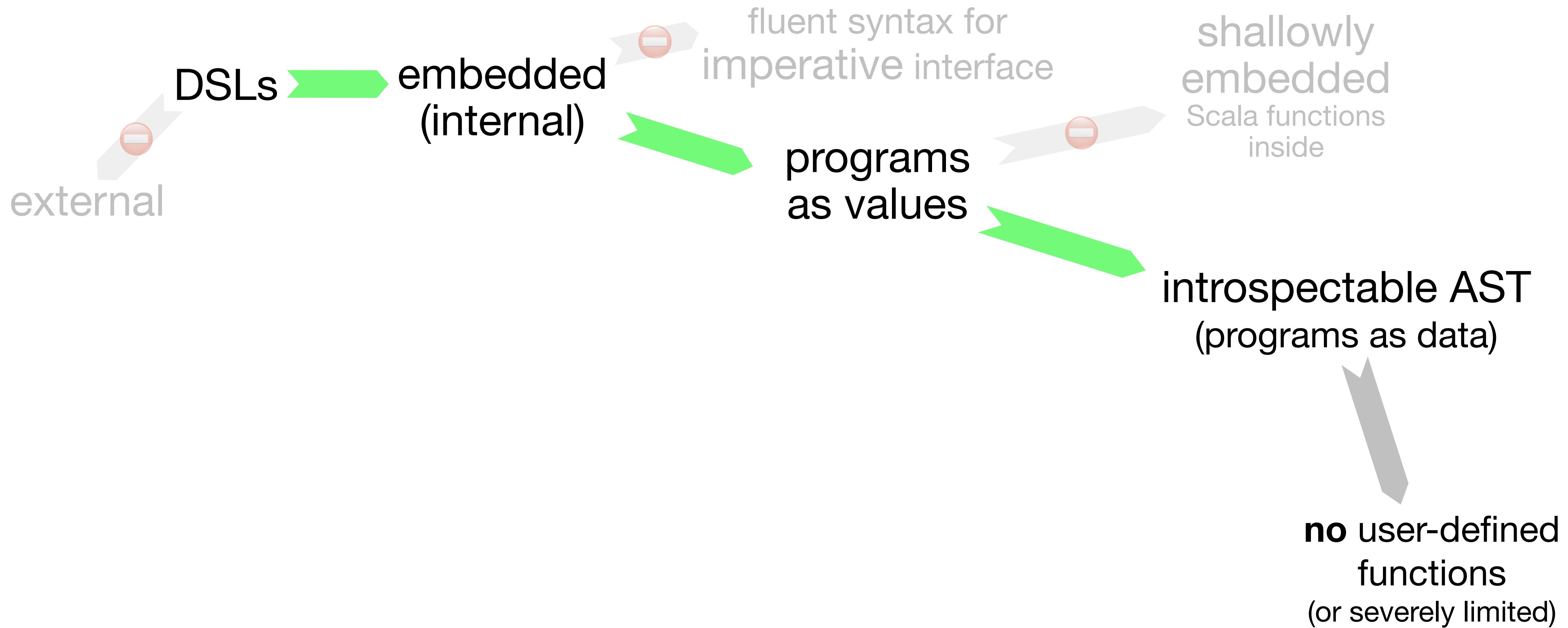


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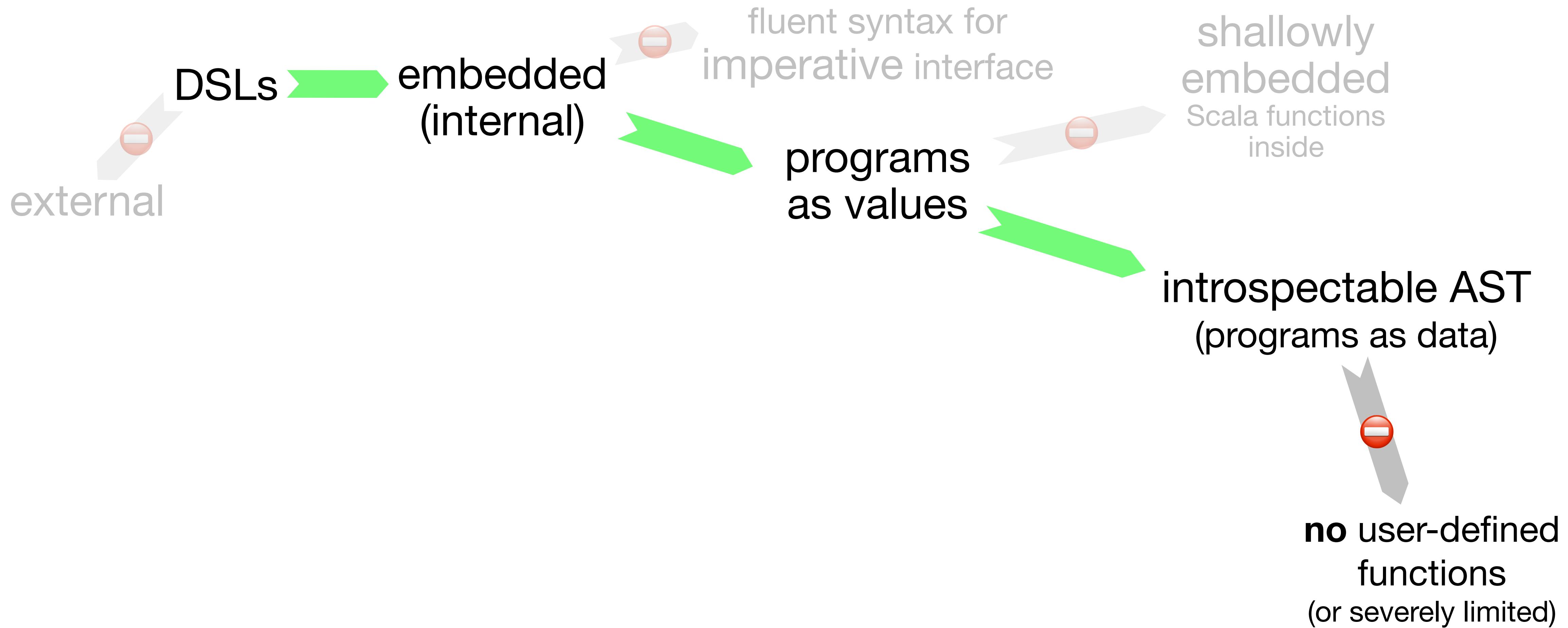


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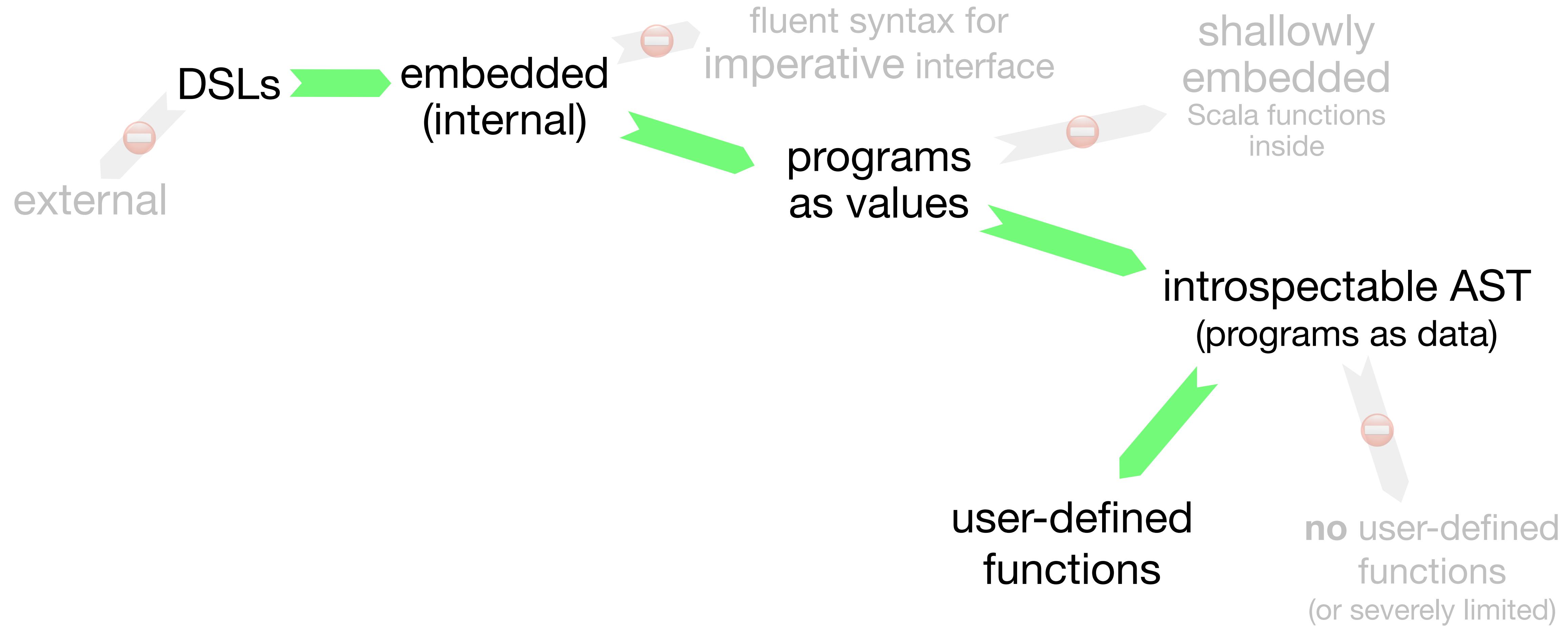


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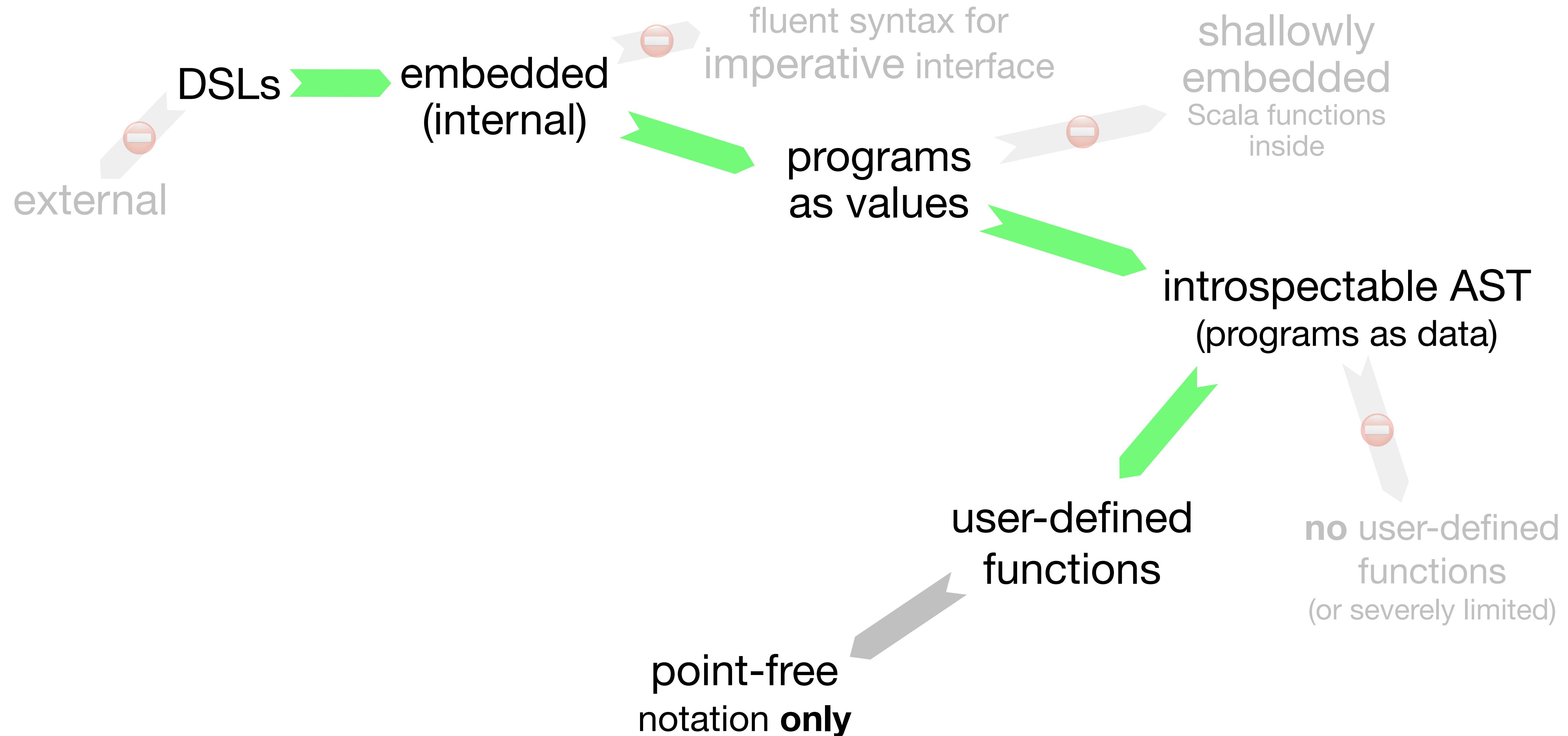


What This Talk Is About





What This Talk Is About





V

point-full

```
x => g( f( x ) )  
  
- match {  
  case Left(a) => f(a)  
  case Right(b) => g(b)  
}
```

DSLs
external

alk Is About

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erative interface

programs
as values

user-defined
functions

point-free
notation **only**

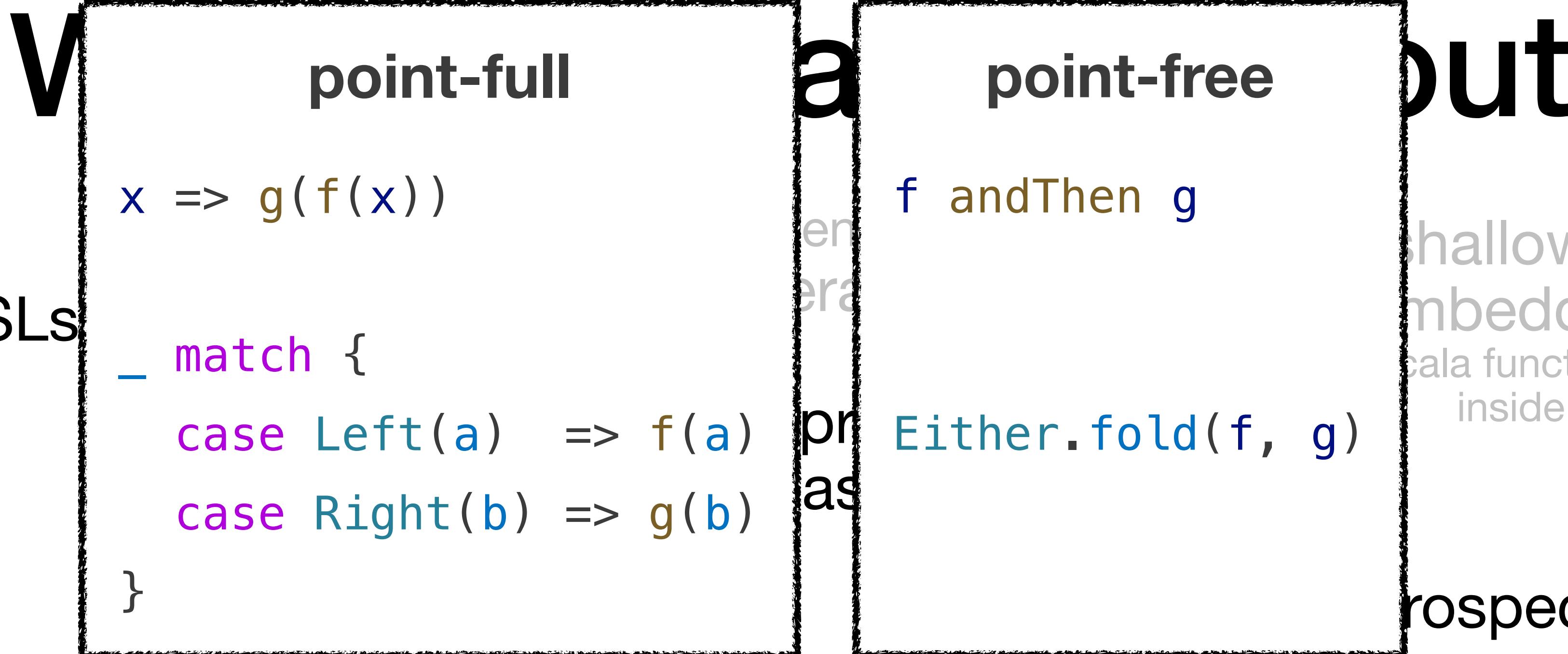
shallowly
embedded
Scala functions
inside

introspectable AST
(programs as data)

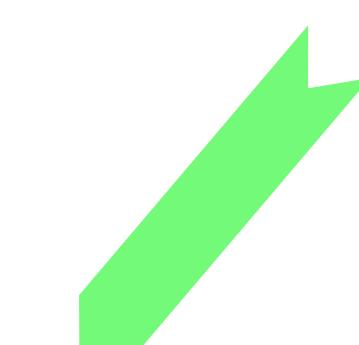
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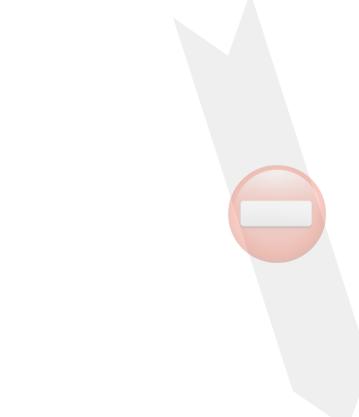


respectable AST
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user-defined
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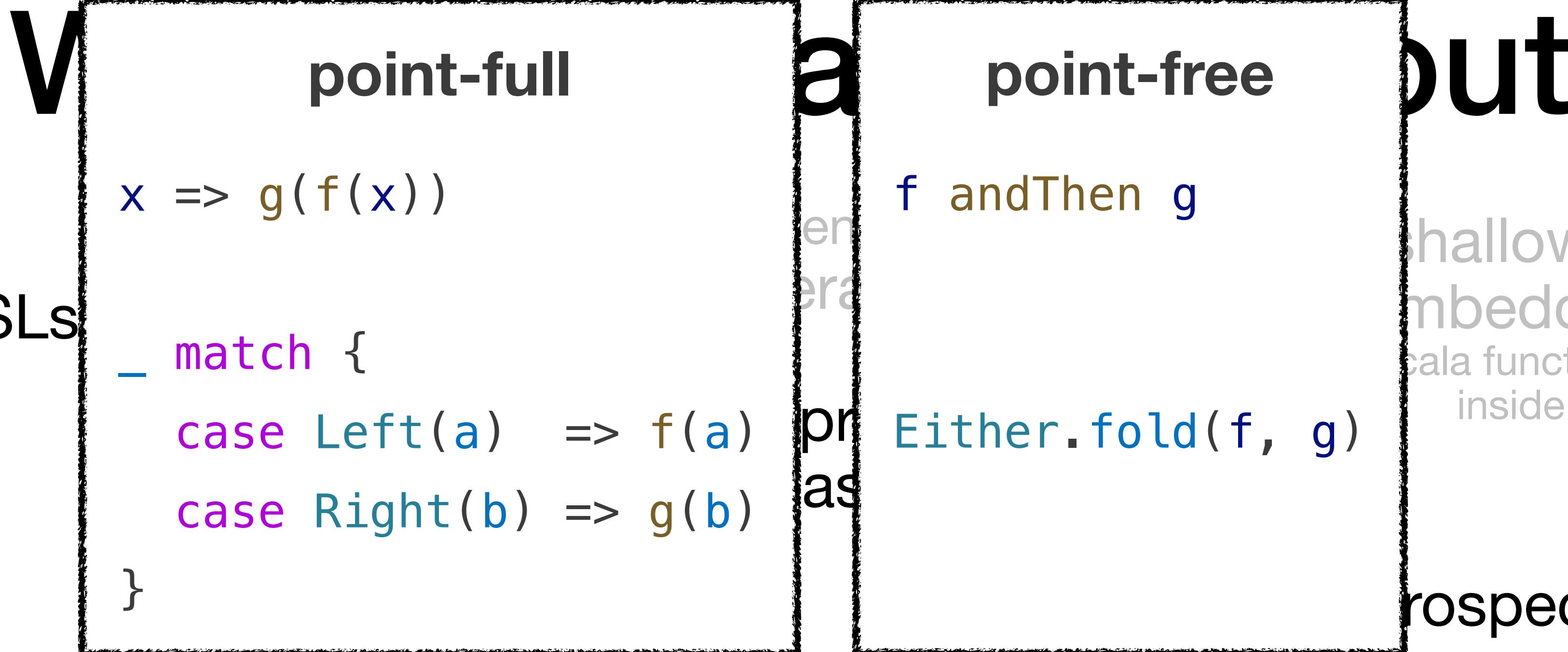
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DSLs
external



- Define a function without giving a name to its input
- Easy to represent as data
 - Good for programs
 - Hard for humans

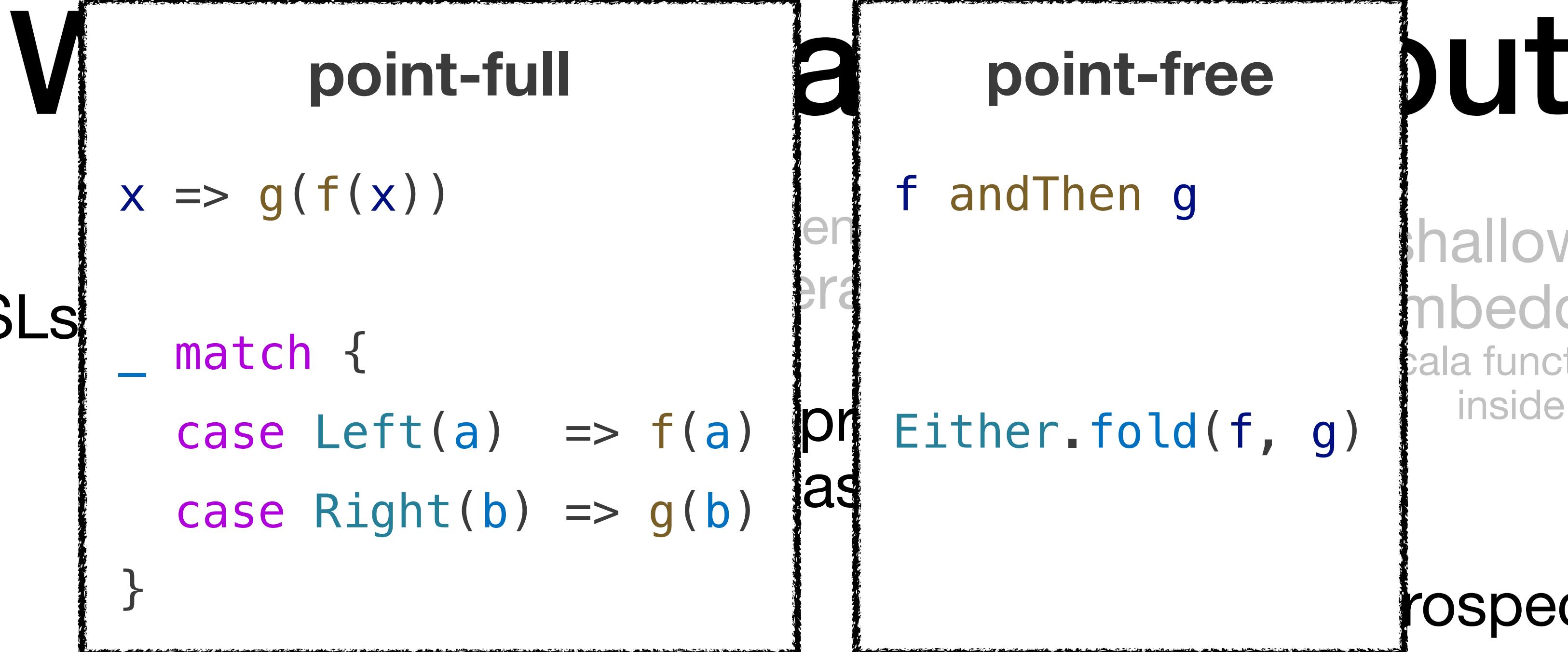
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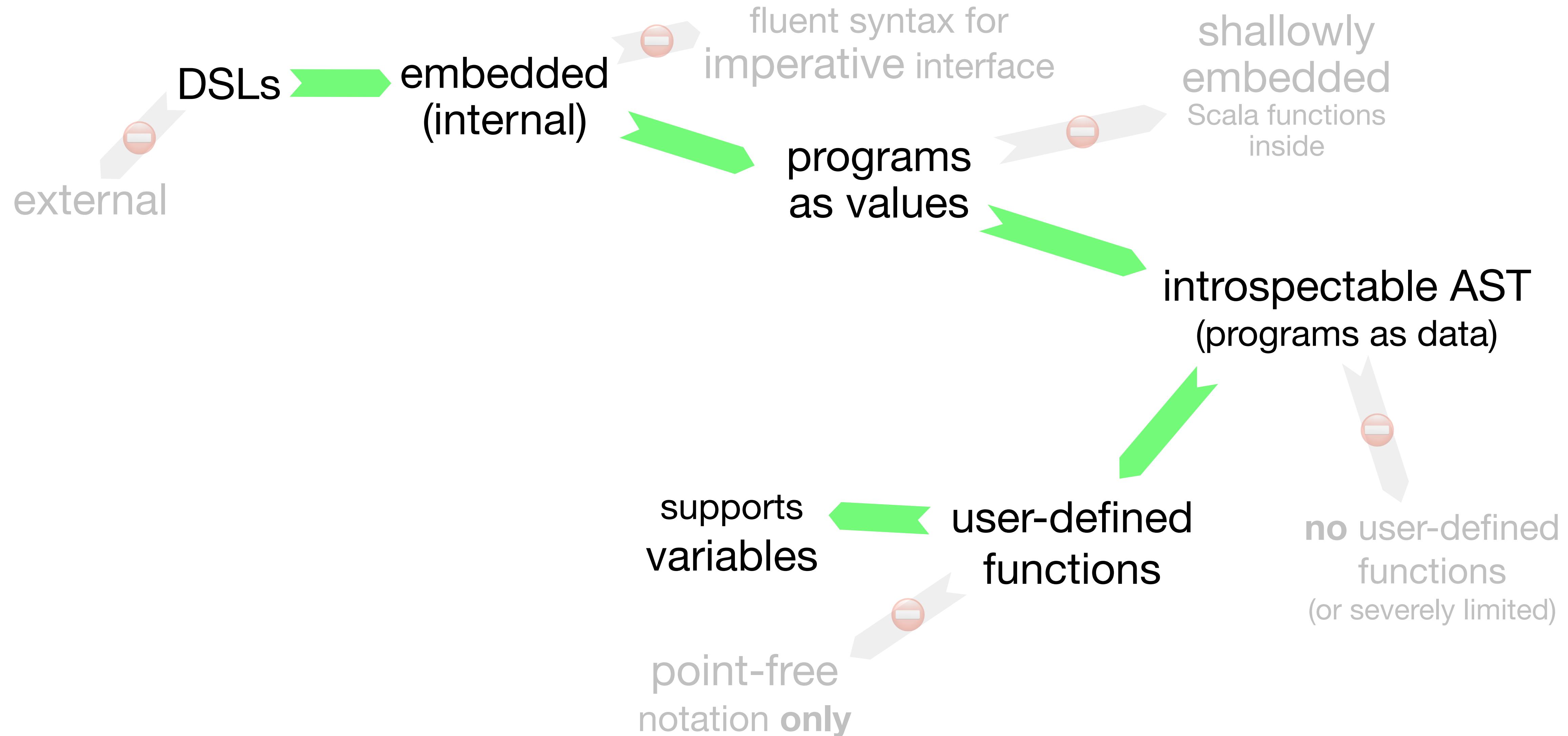
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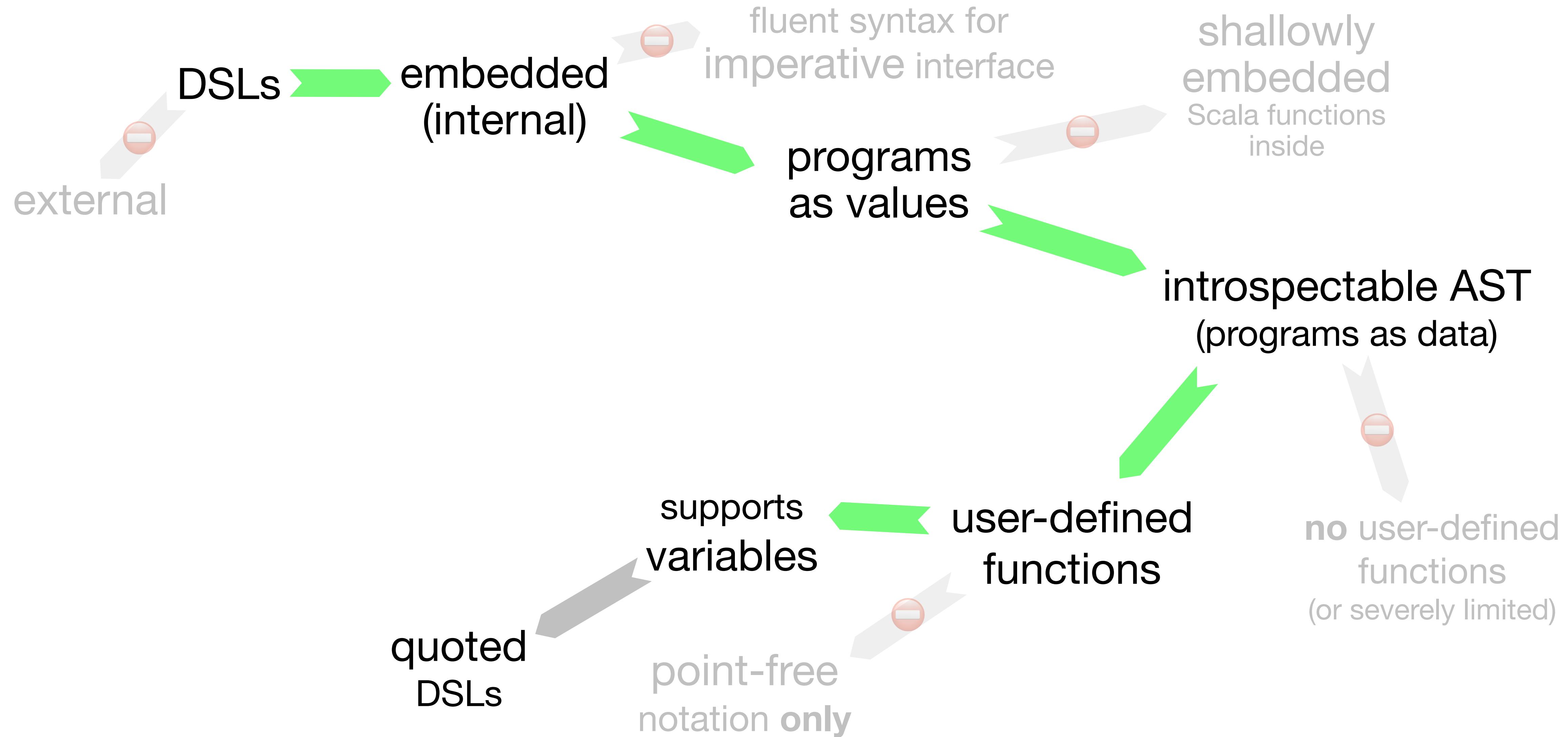


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What This Talk Is About

- Use Scala's anonymous function syntax
- Use a macro to give it a different meaning
- Dealing with Scala AST
- Macro does not see through an Ident

quoted
DSLs

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variables

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fluent syntax for
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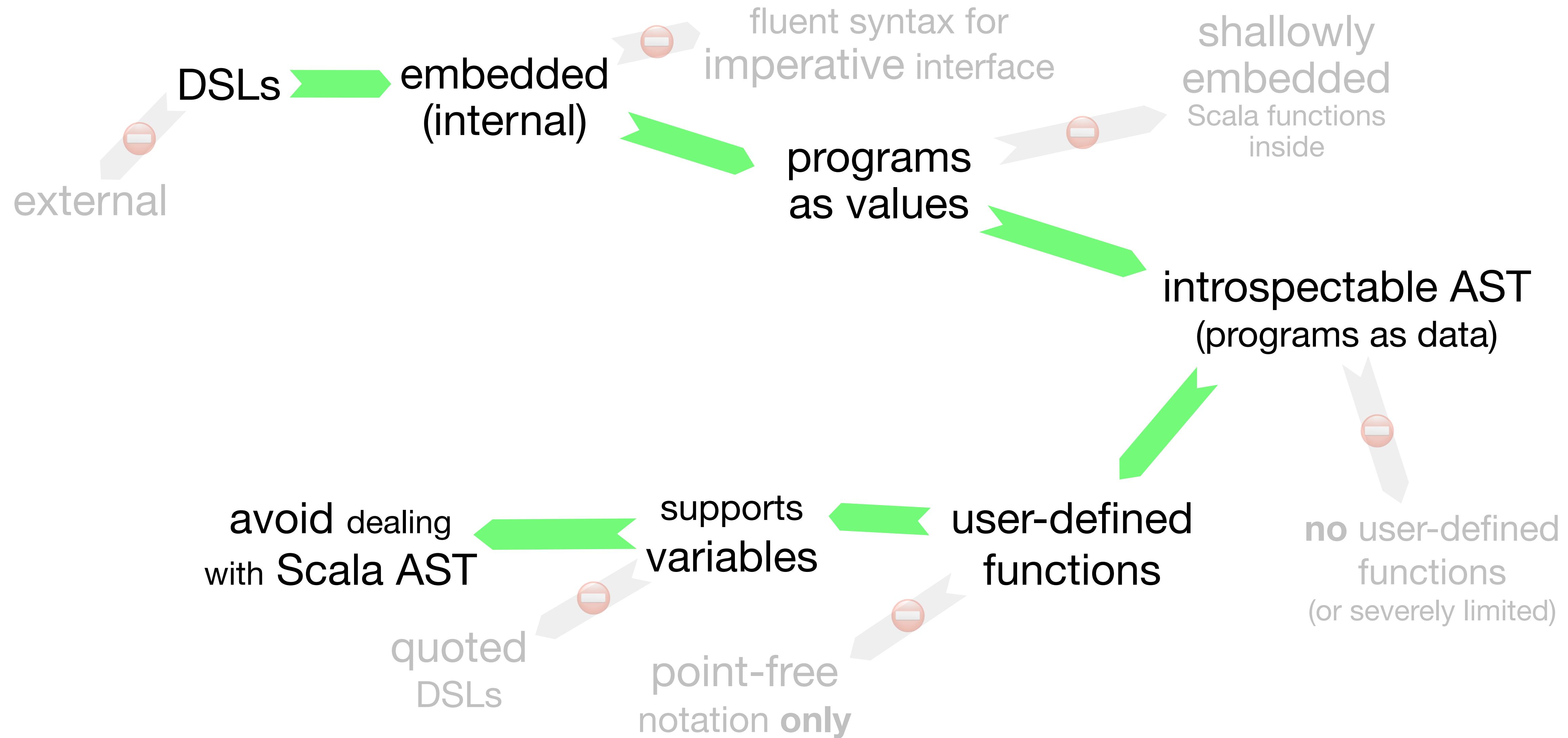
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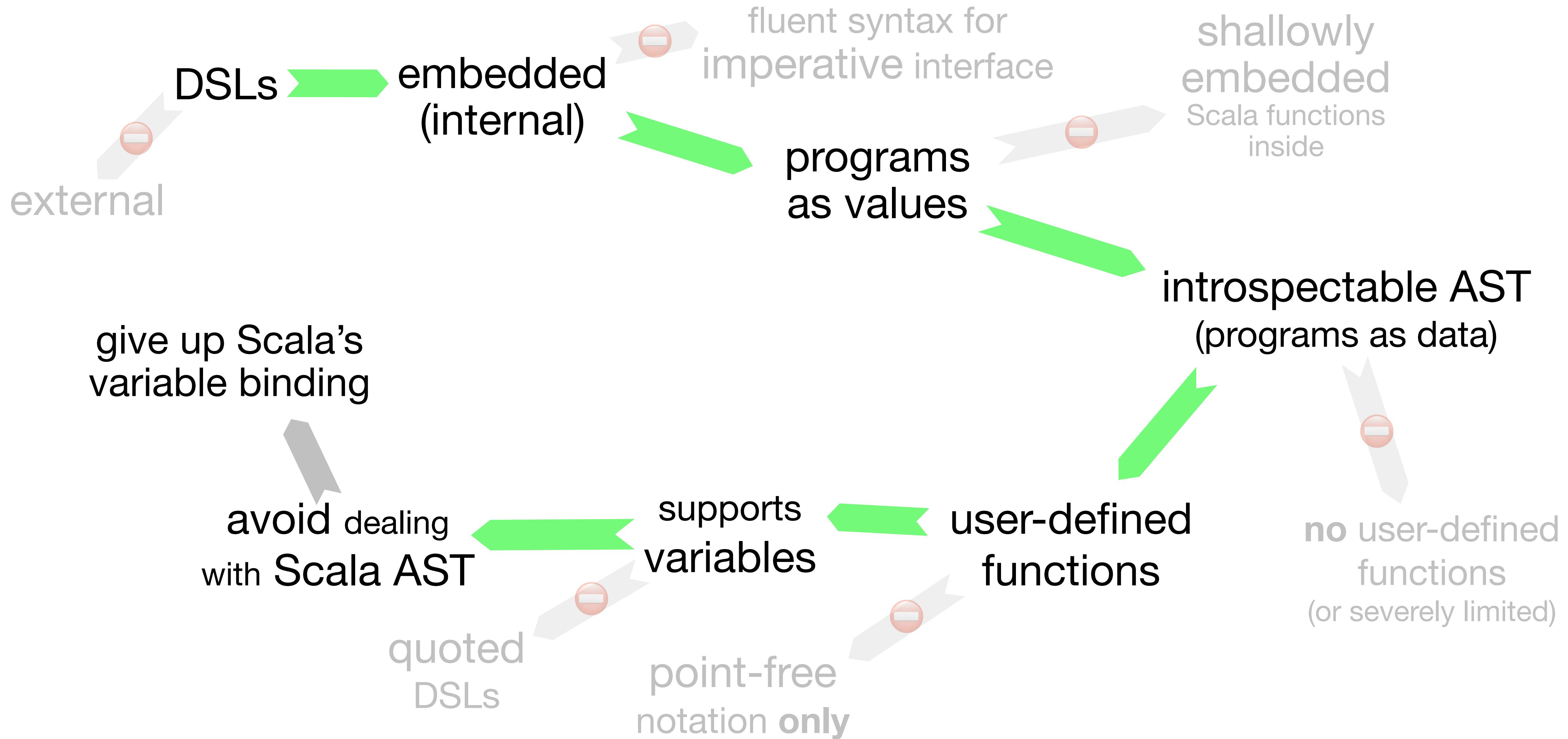


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DSLs ➤

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give up Scala's
variable binding

avoid dealing
with Scala AST

quoted
DSLs

fluent syntax for

shallowly
nested
selections

selectable AST
(lists as data)

no user-defined
functions
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```
// Declare your aliases before using them in SQL:  
Author a = AUTHOR.as("a");  
  
// Use aliased tables in your statement  
create.select()  
    .from(a)  
    .where(a.YEAR_OF_BIRTH.gt(1920)  
    .and(a.FIRST_NAME.eq("Paulo")));
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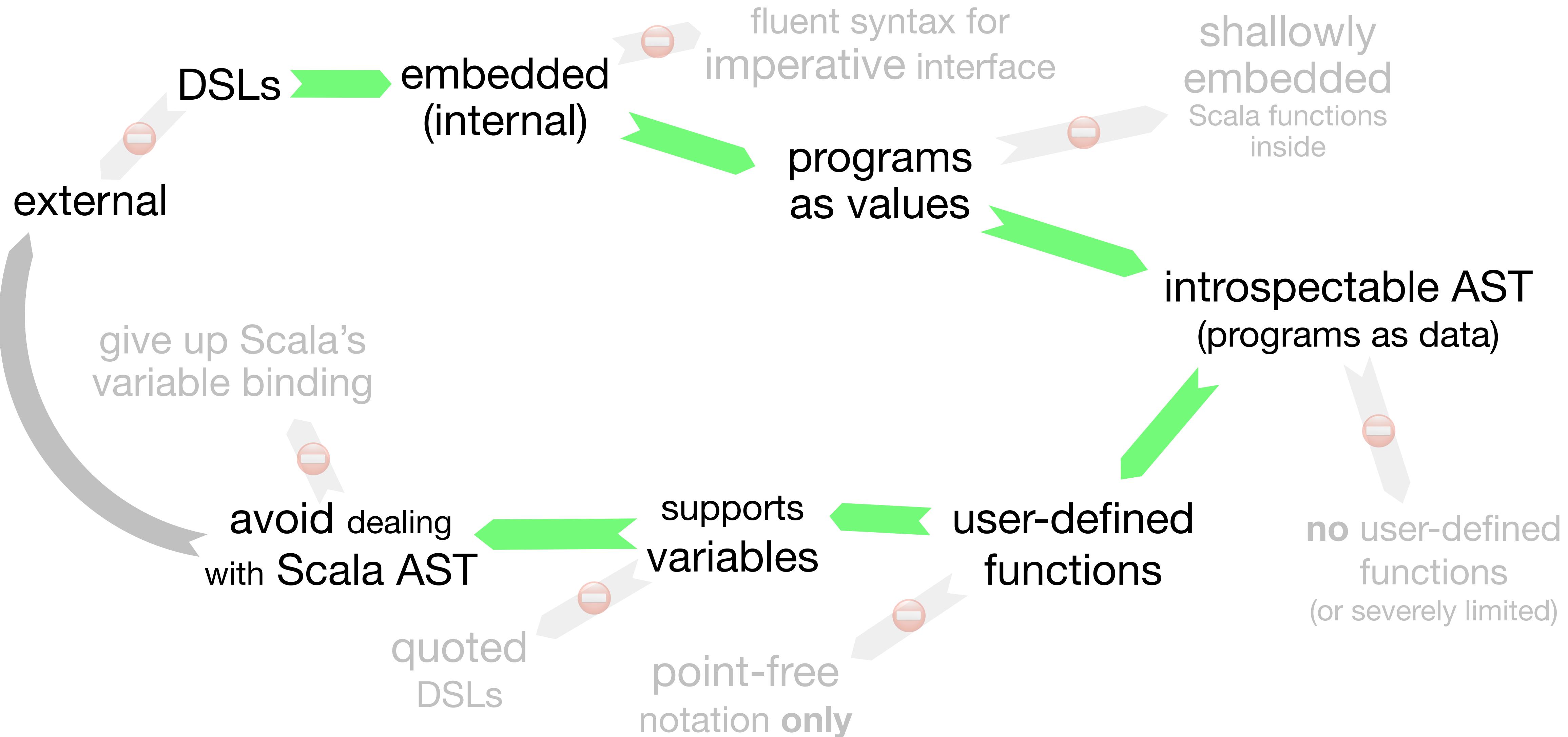
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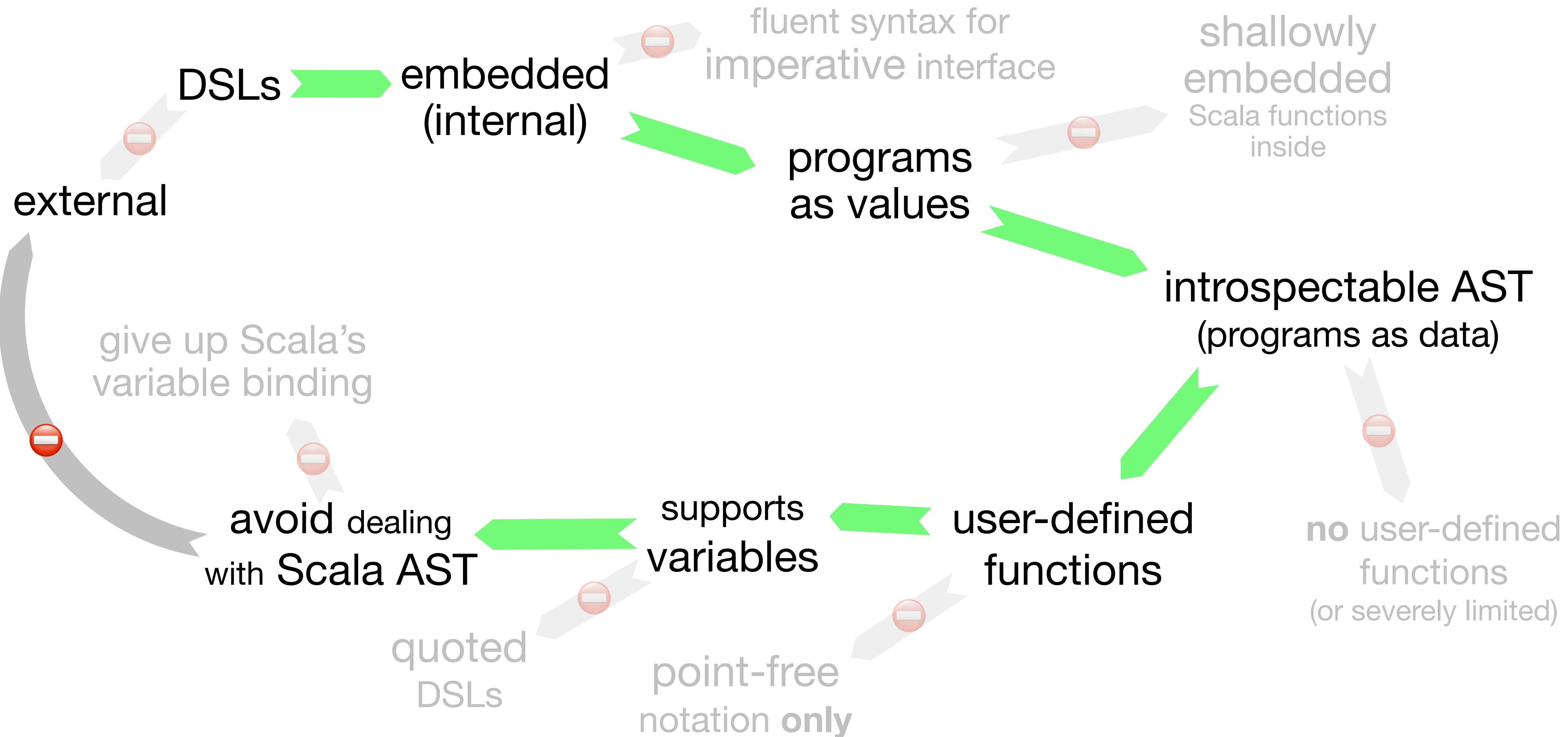


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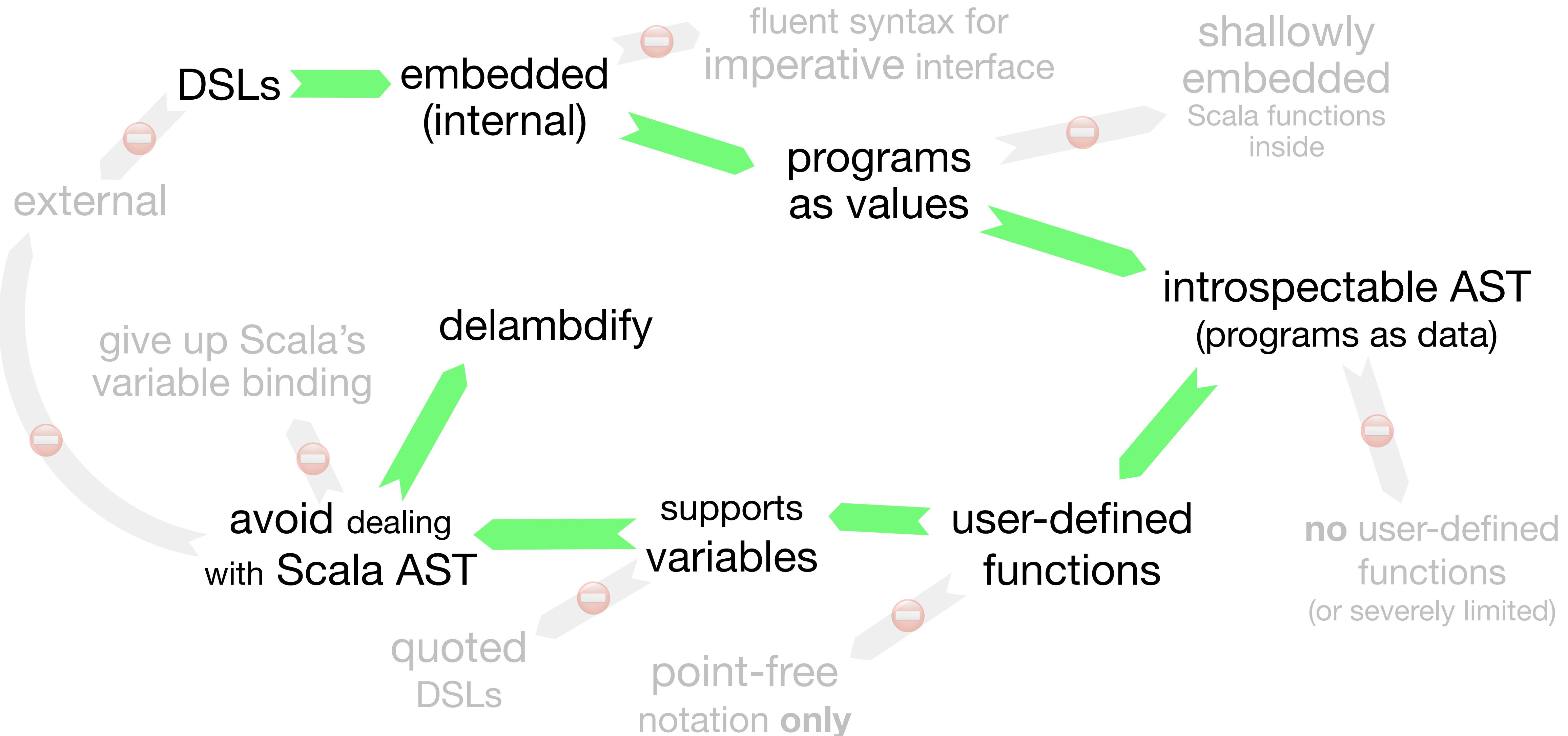


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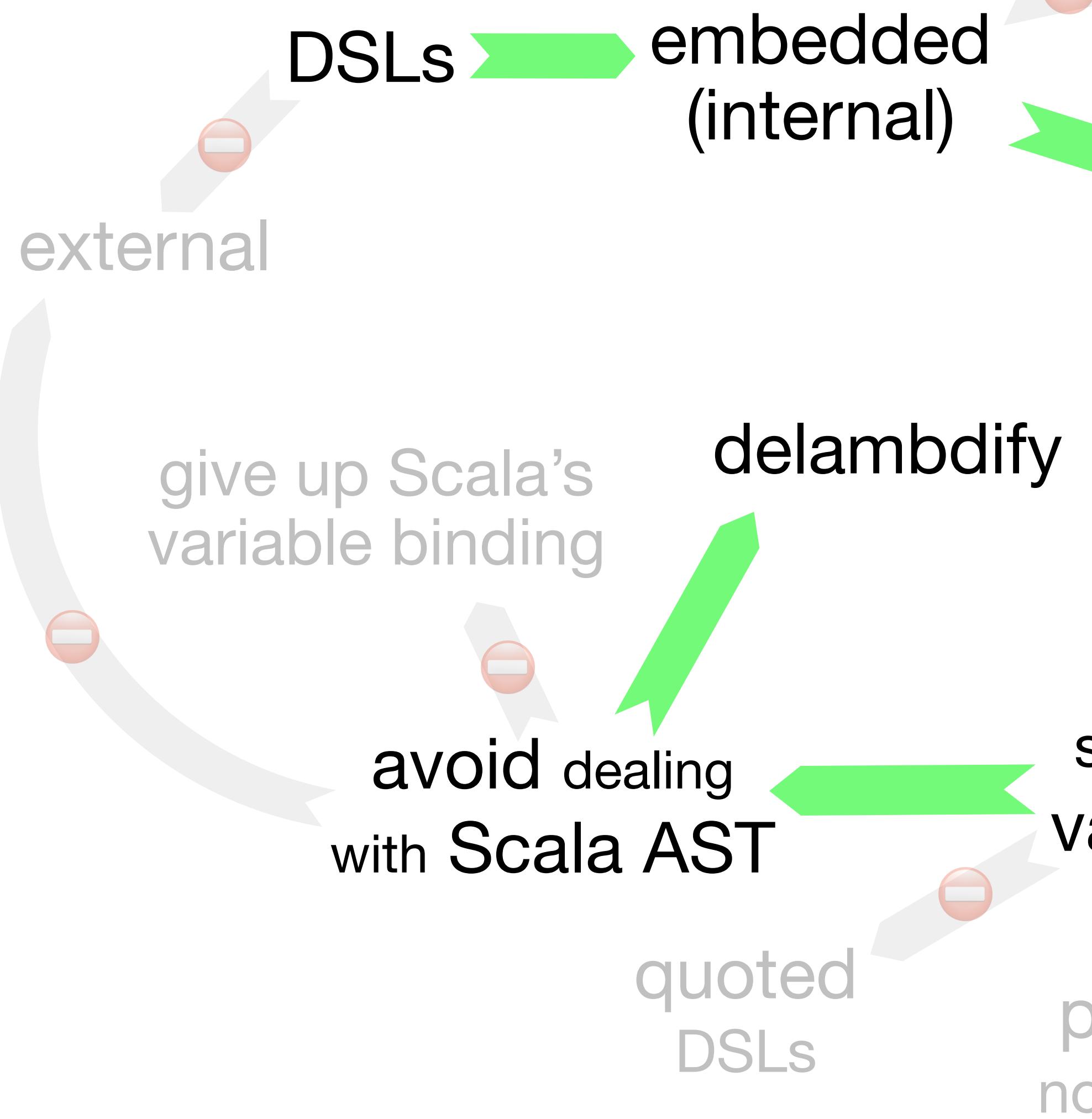


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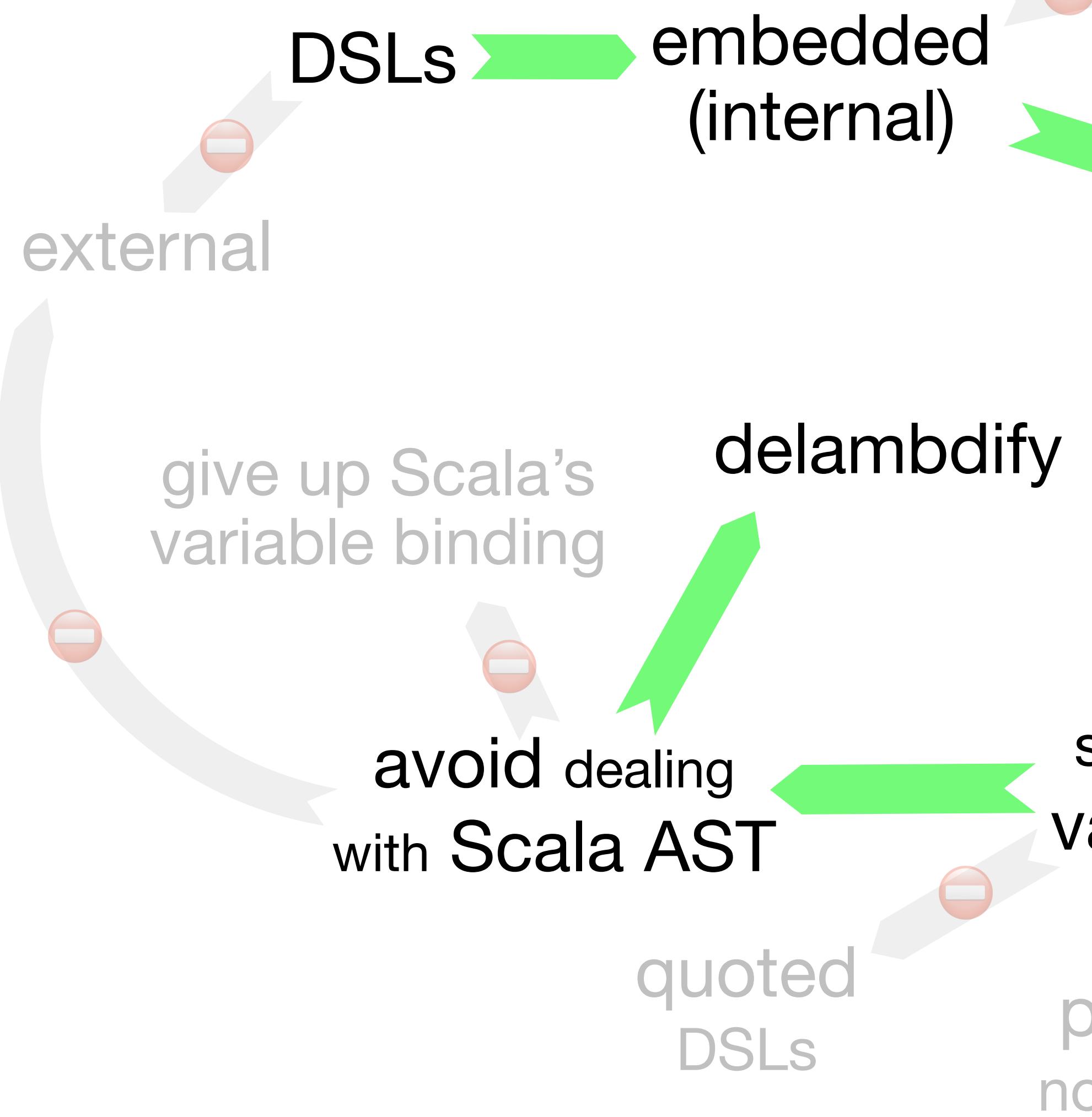


Instead of

notation only



What This

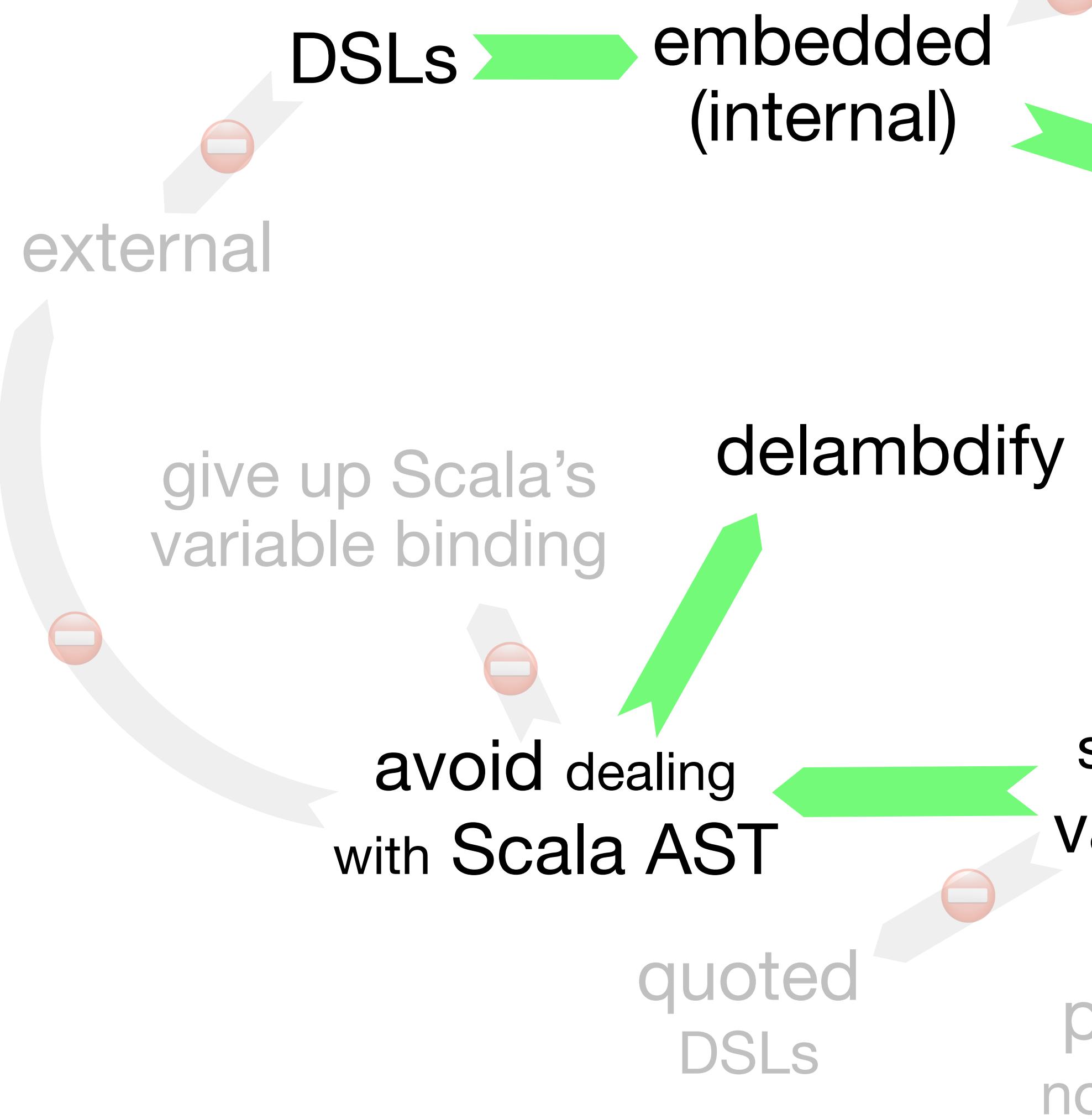


Instead of

`(a: A) => body: B`



What This



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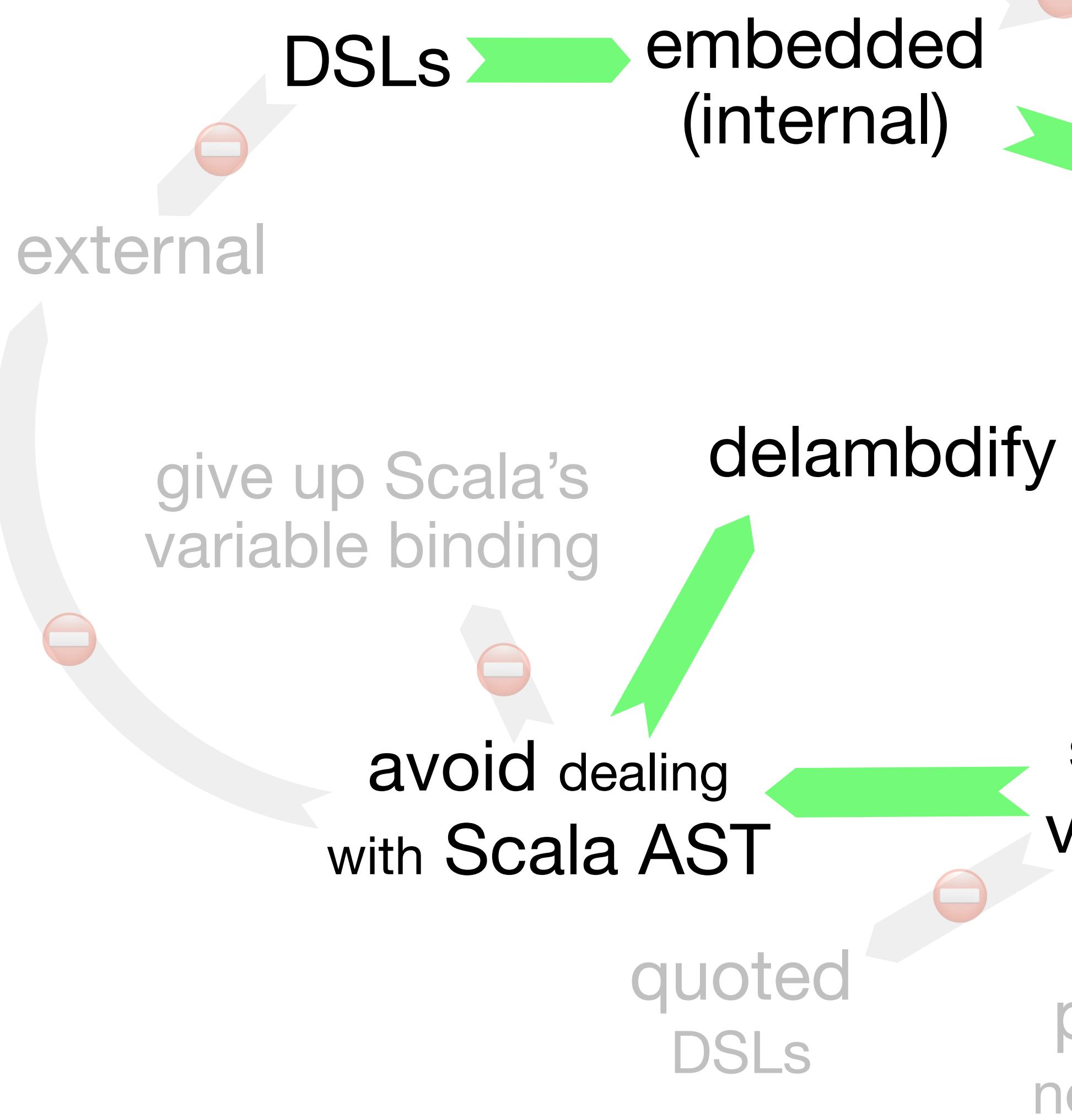
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so
variables
parameters
notation only



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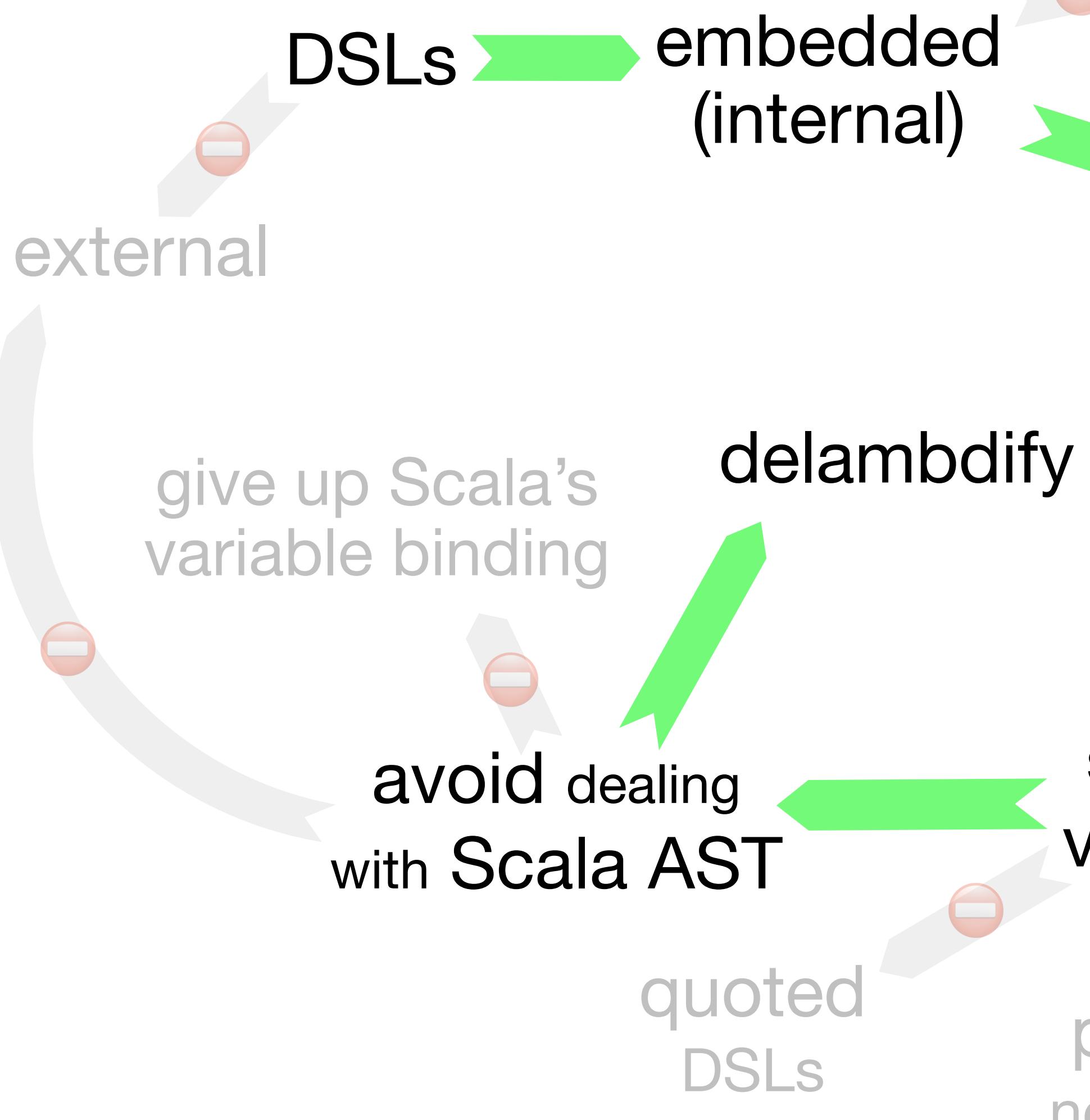
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notation only



What This



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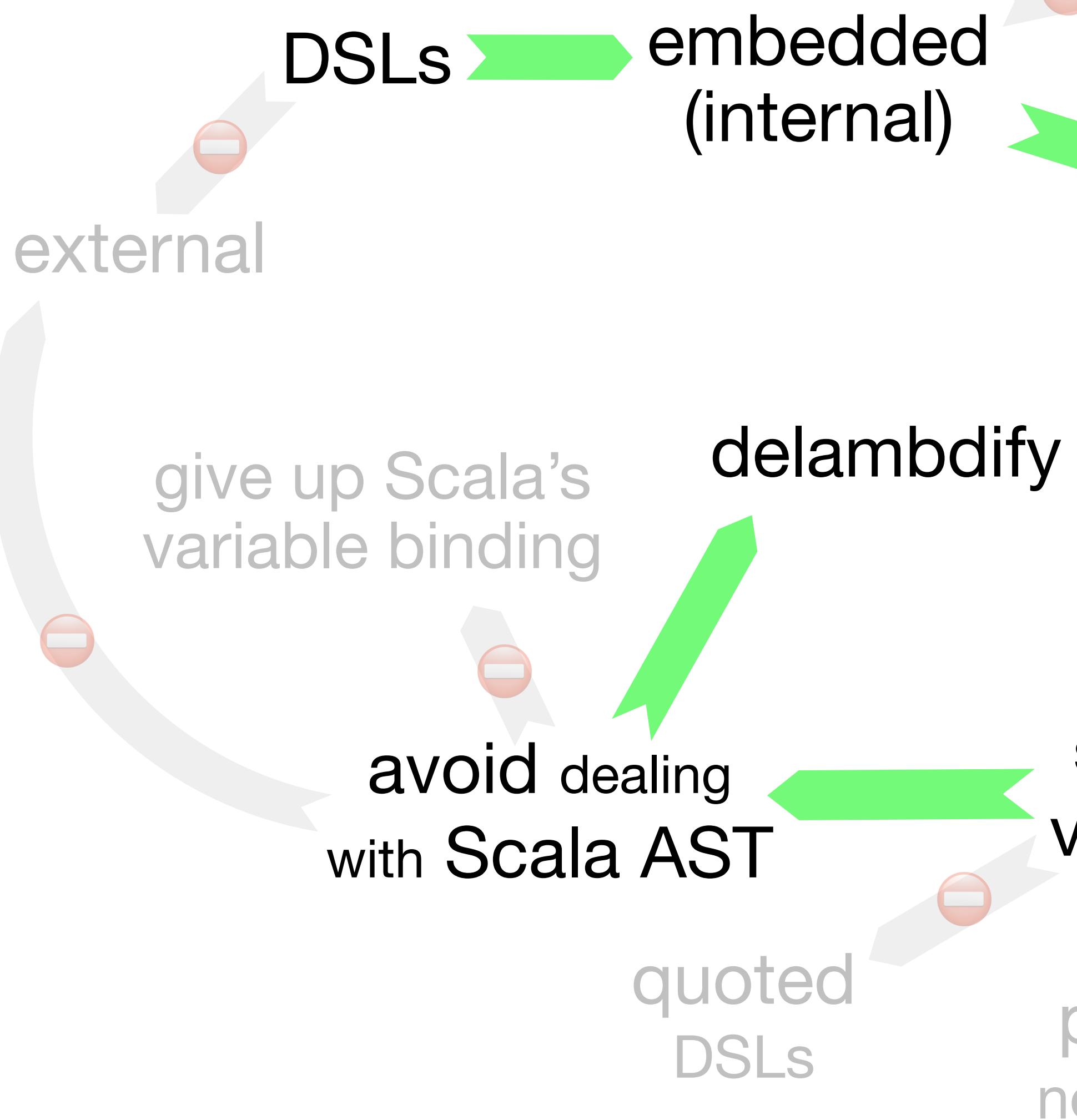
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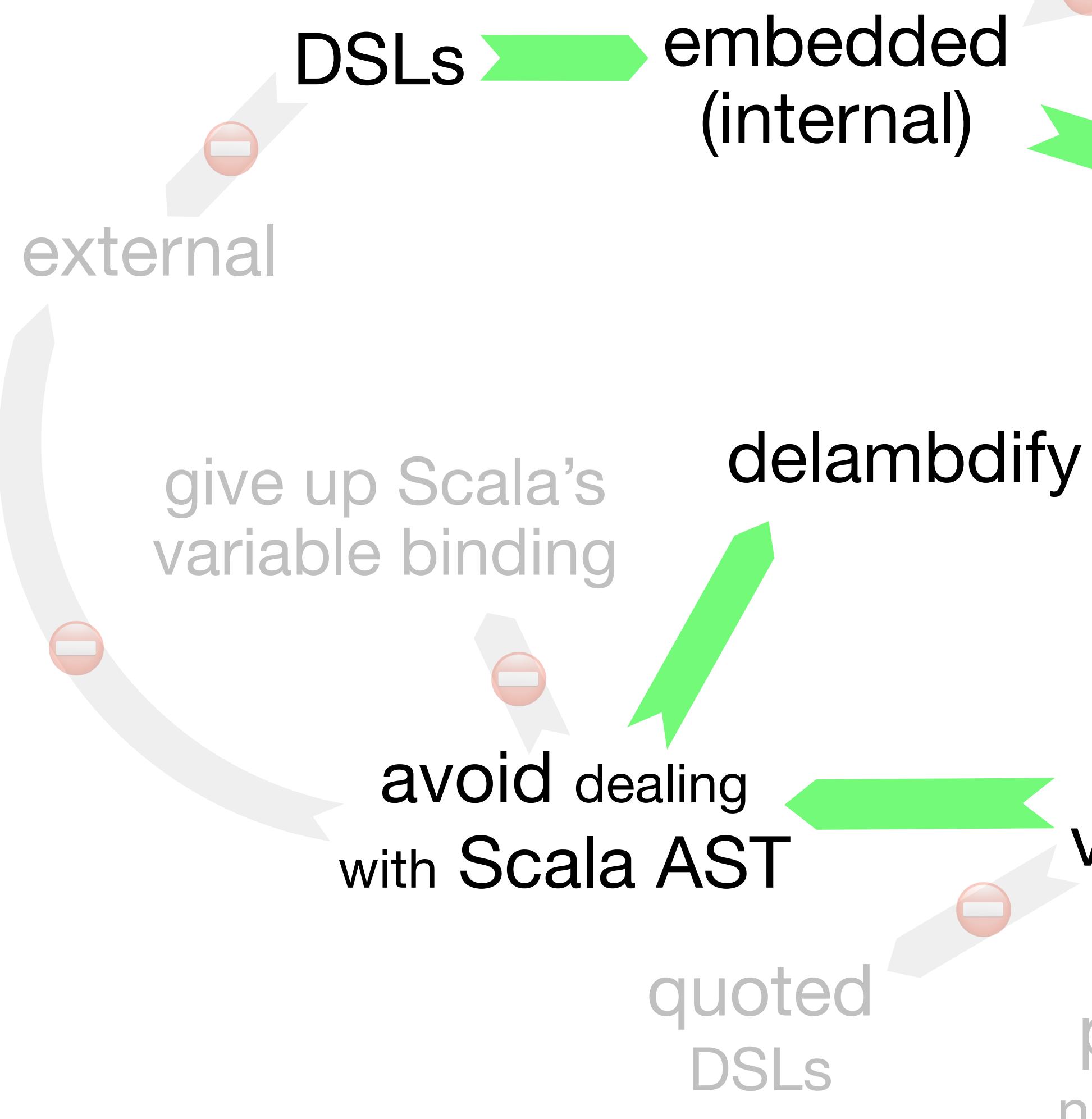
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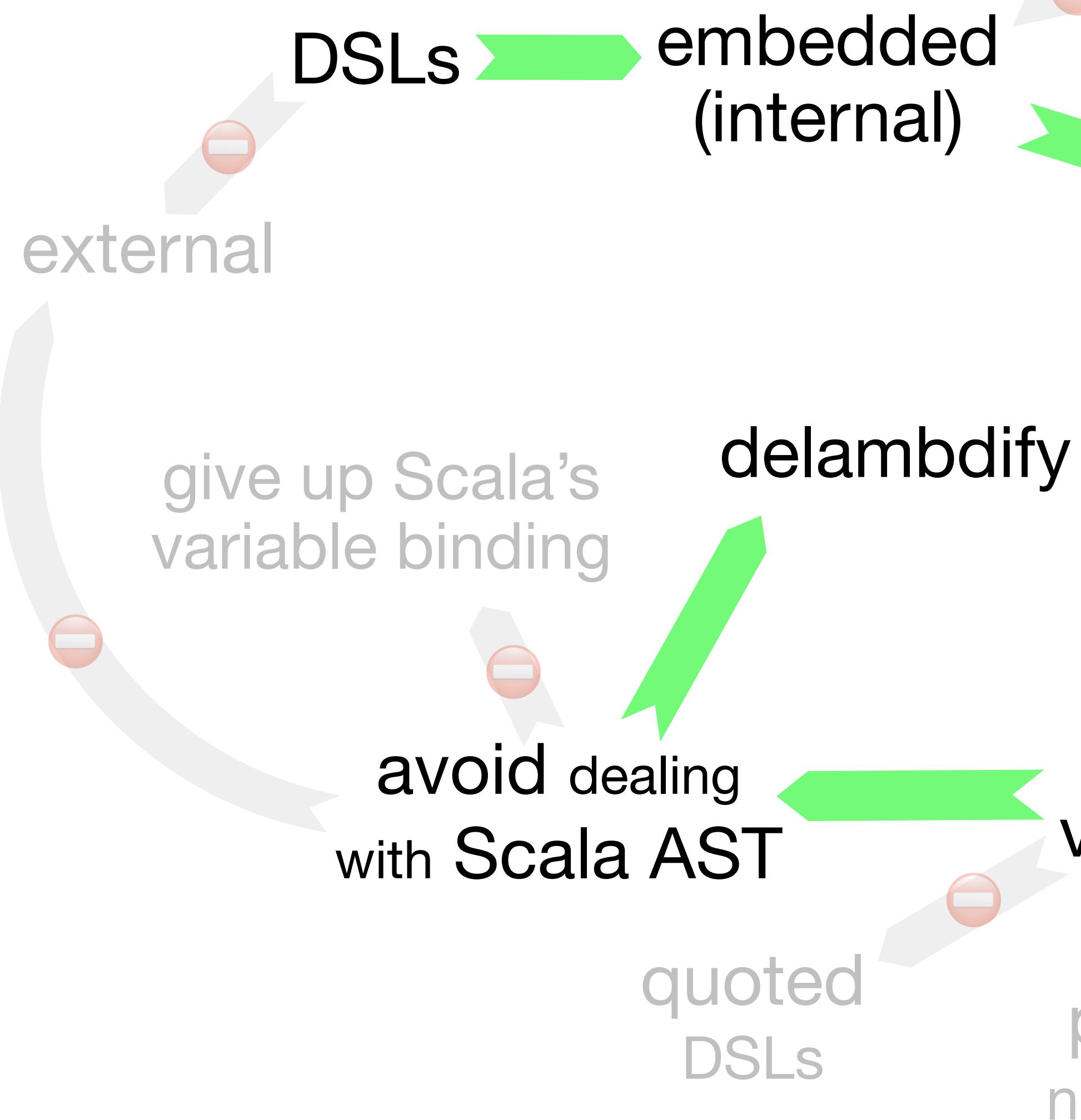
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notation only



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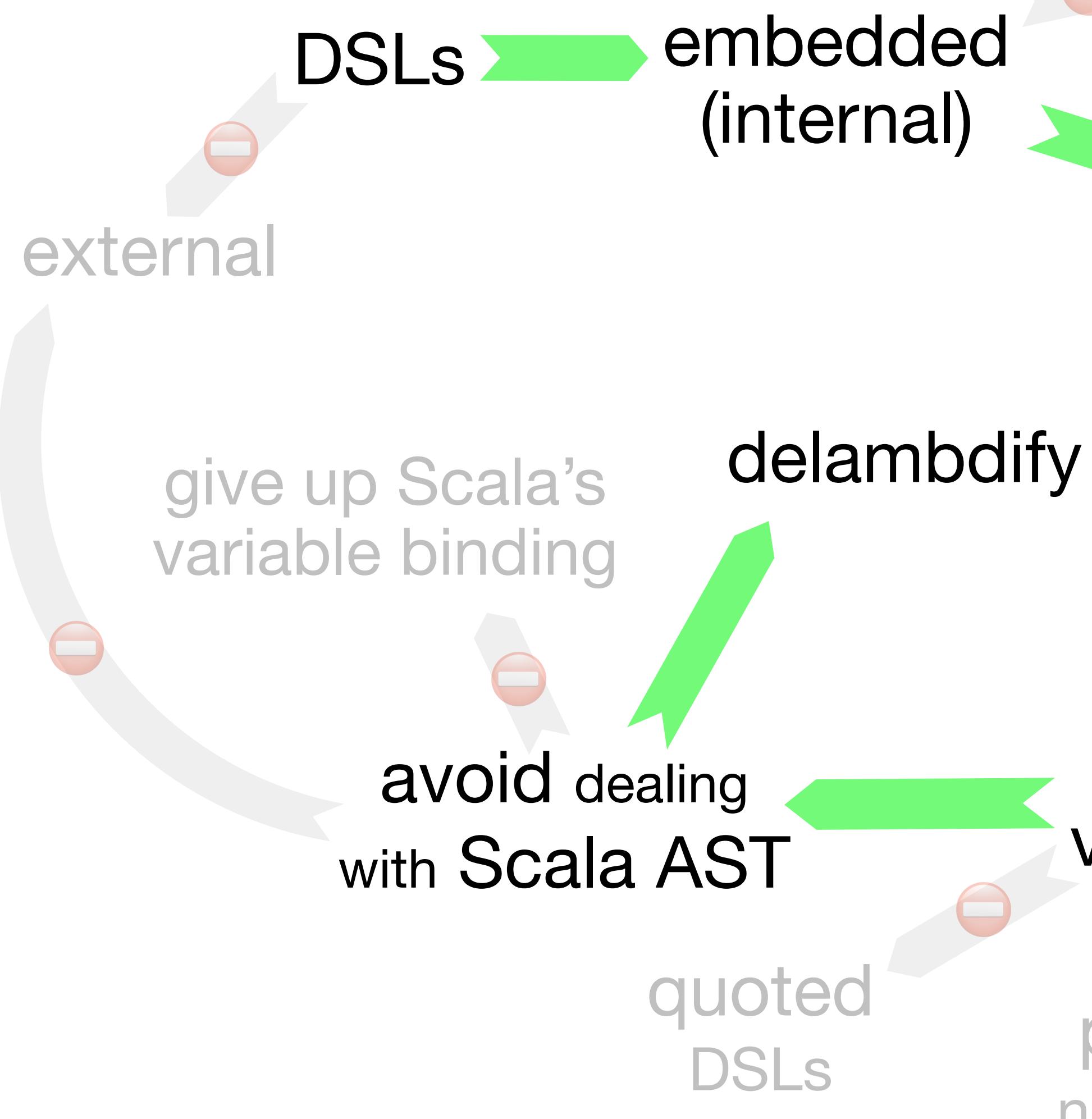
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● Programs as data



What This



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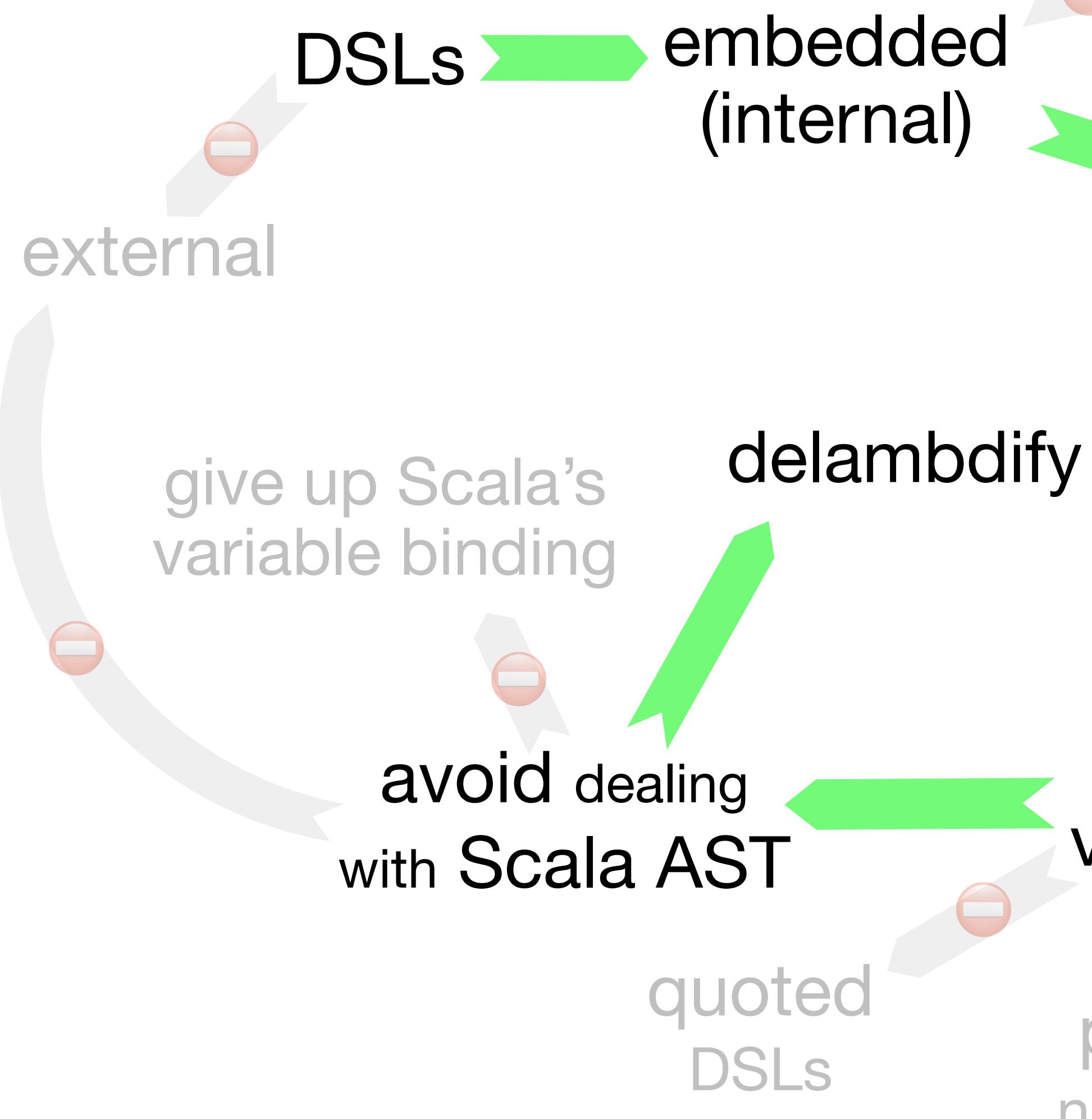
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- Programs as data

- Dealing with variables error-prone



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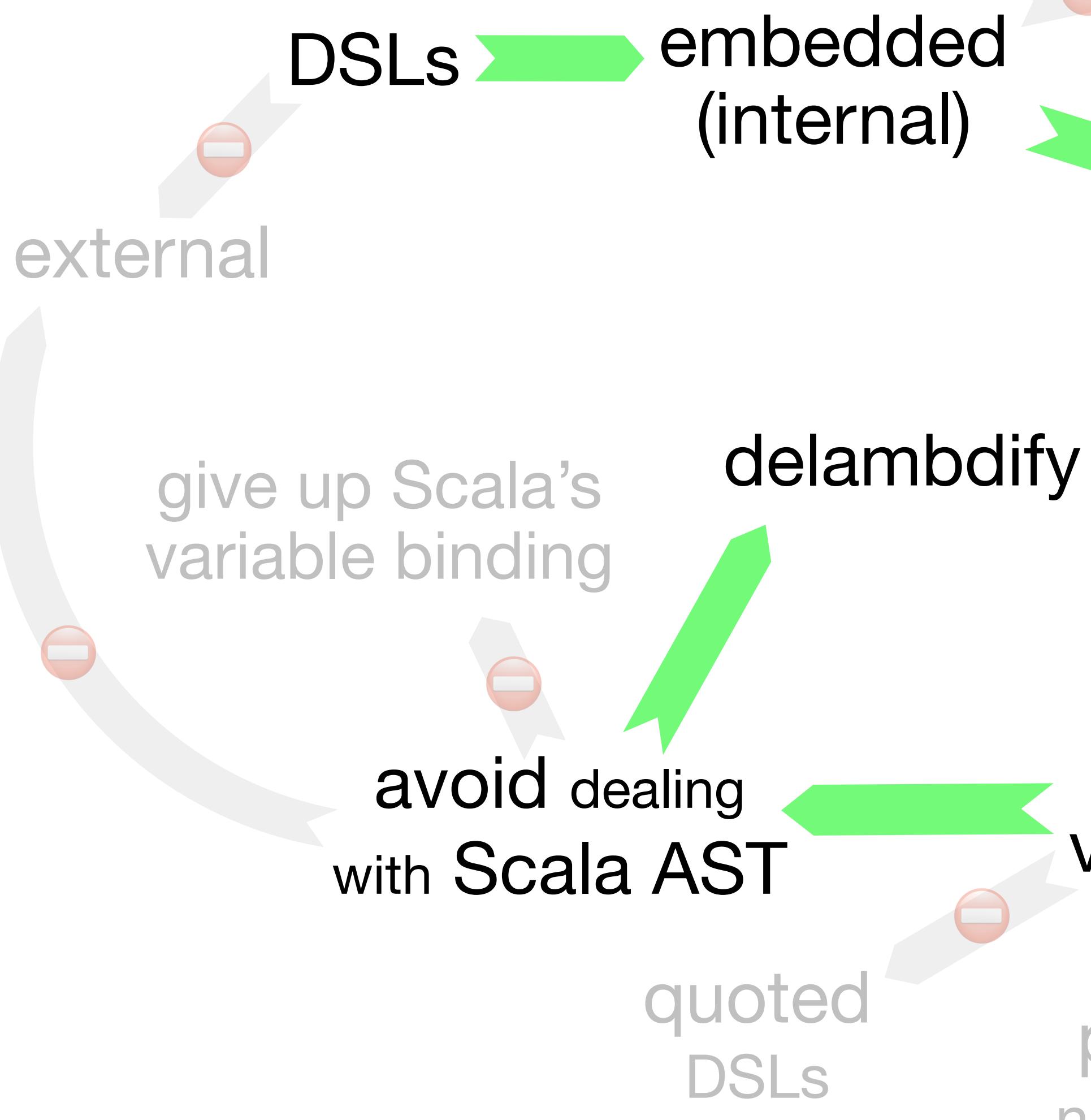
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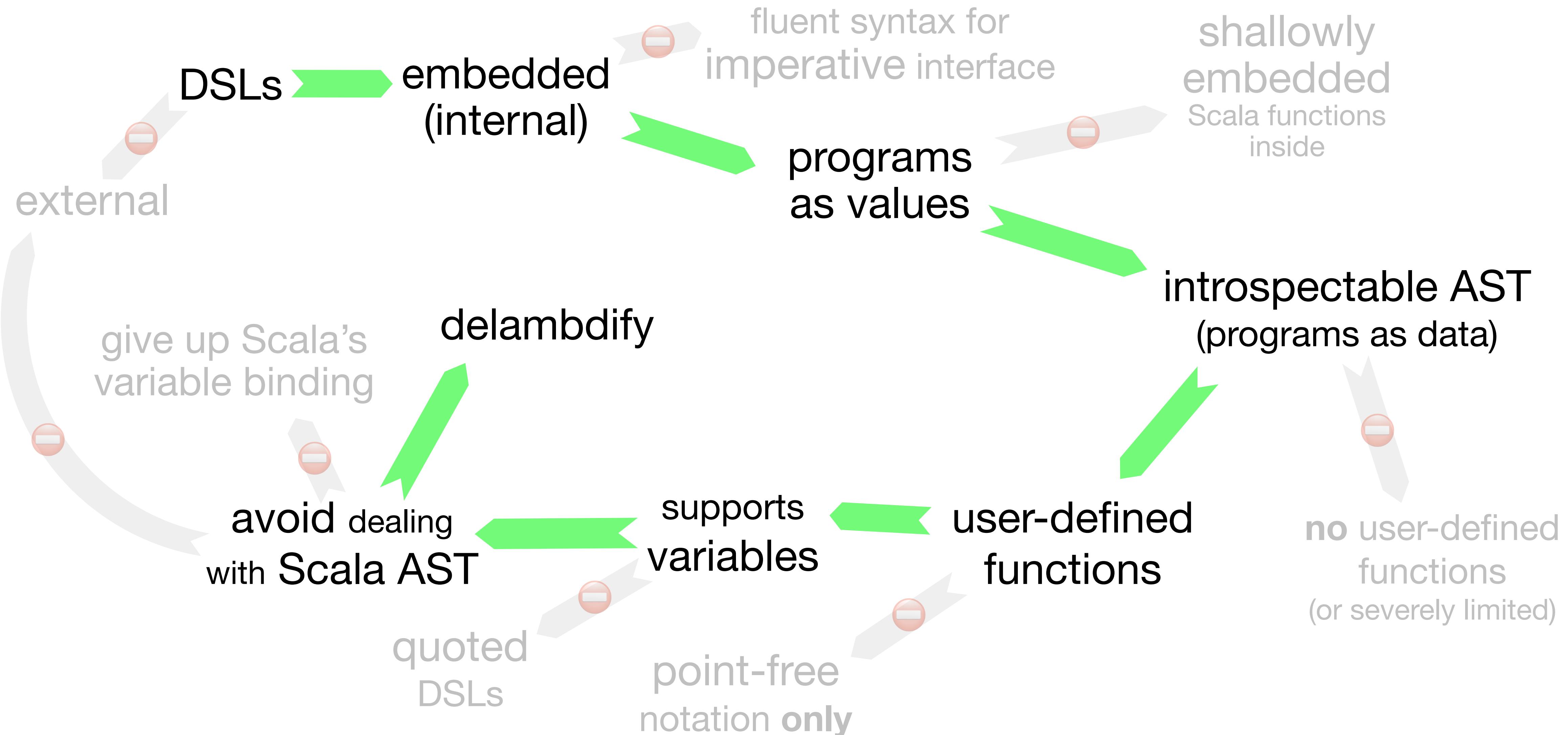
- Dealing with variables error-prone

- Non-locality of substitution

- Malformed programs representable

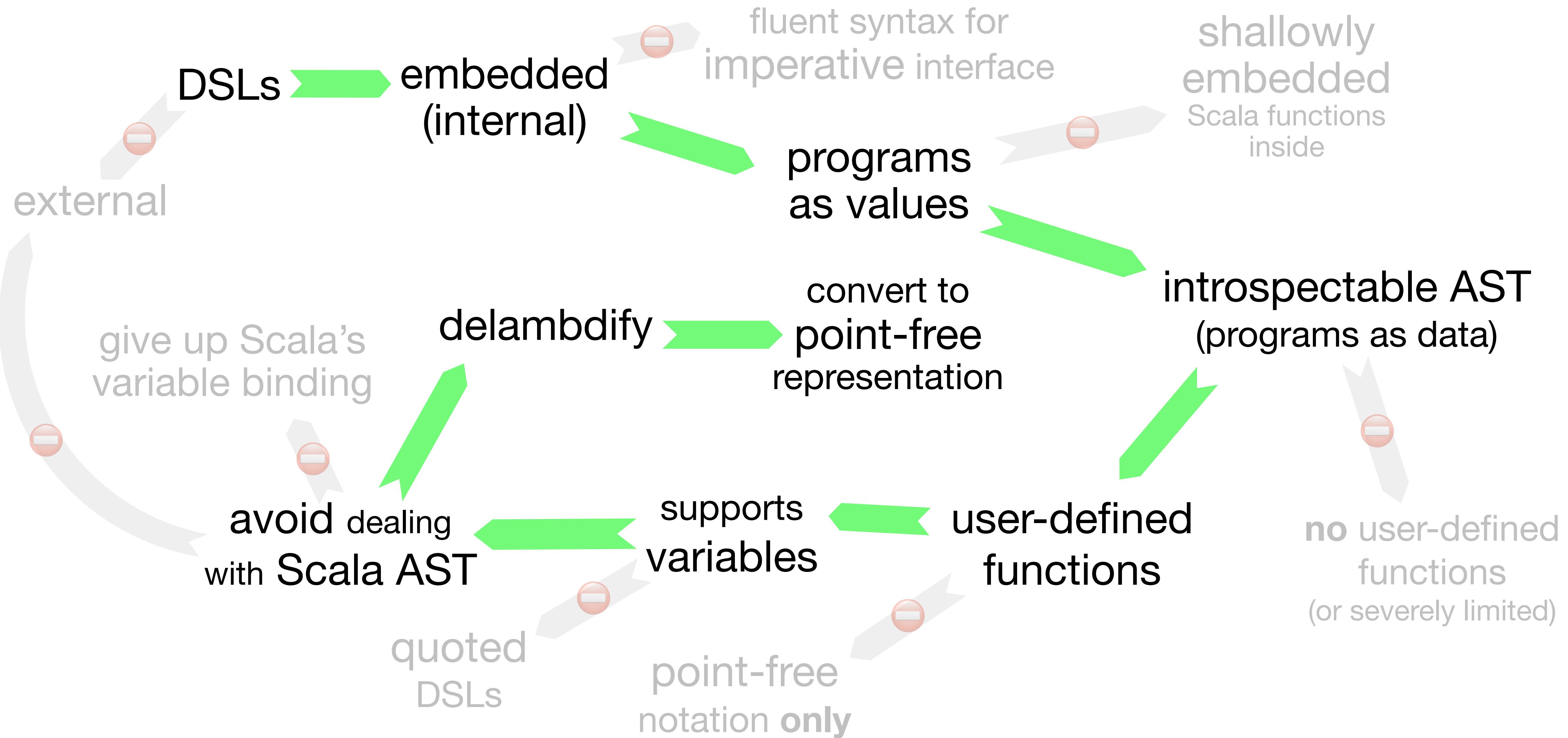


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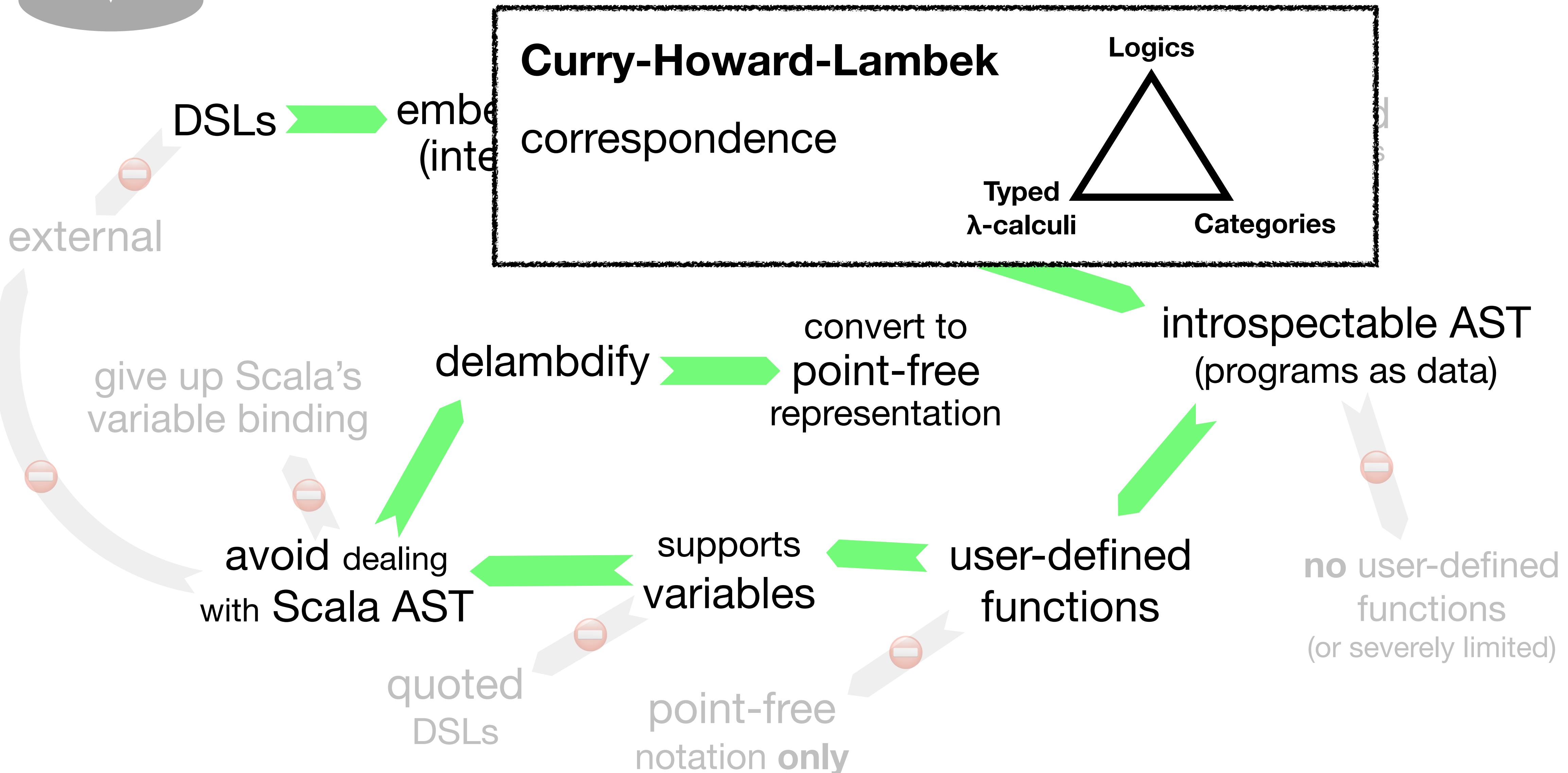


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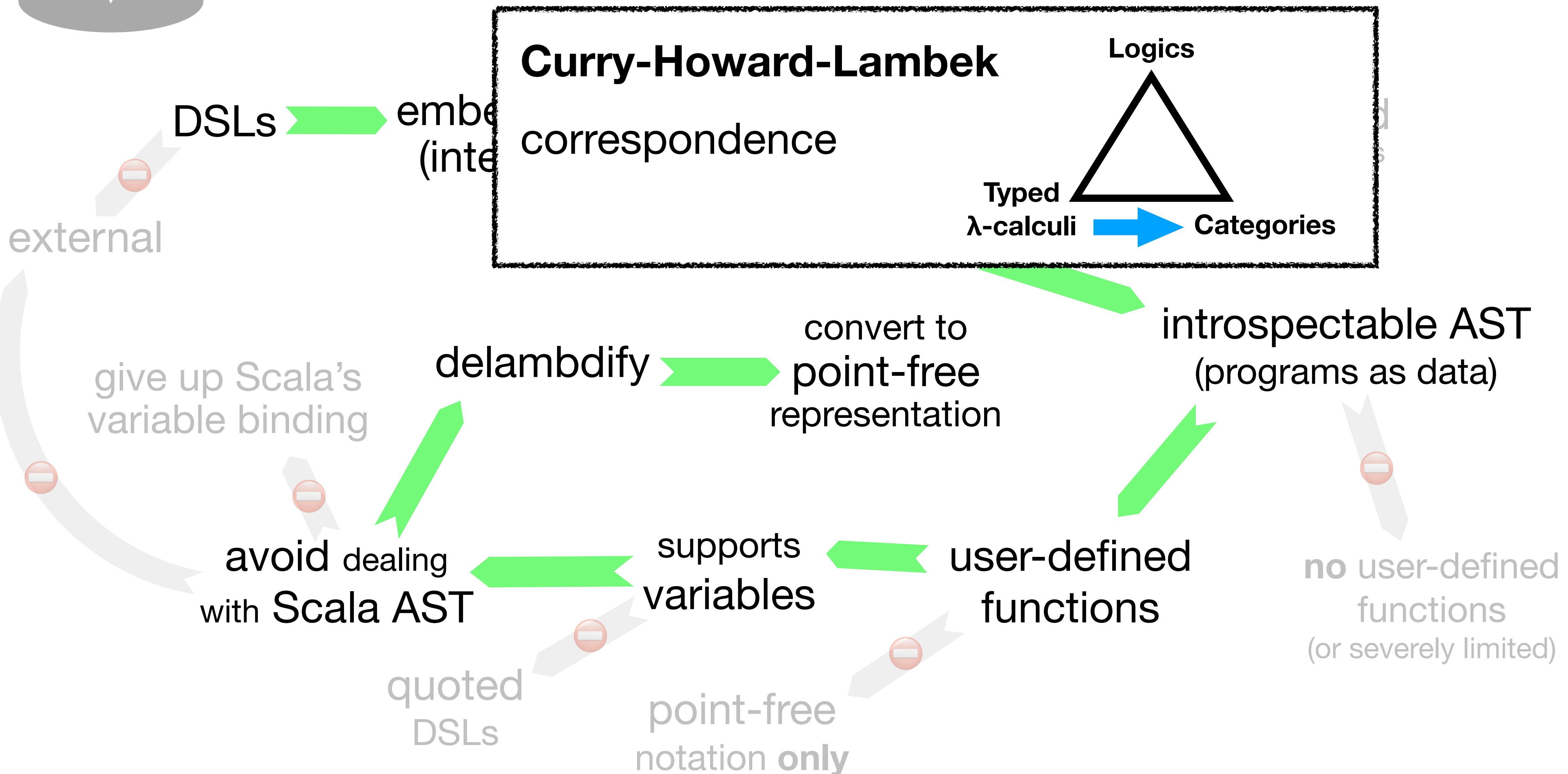


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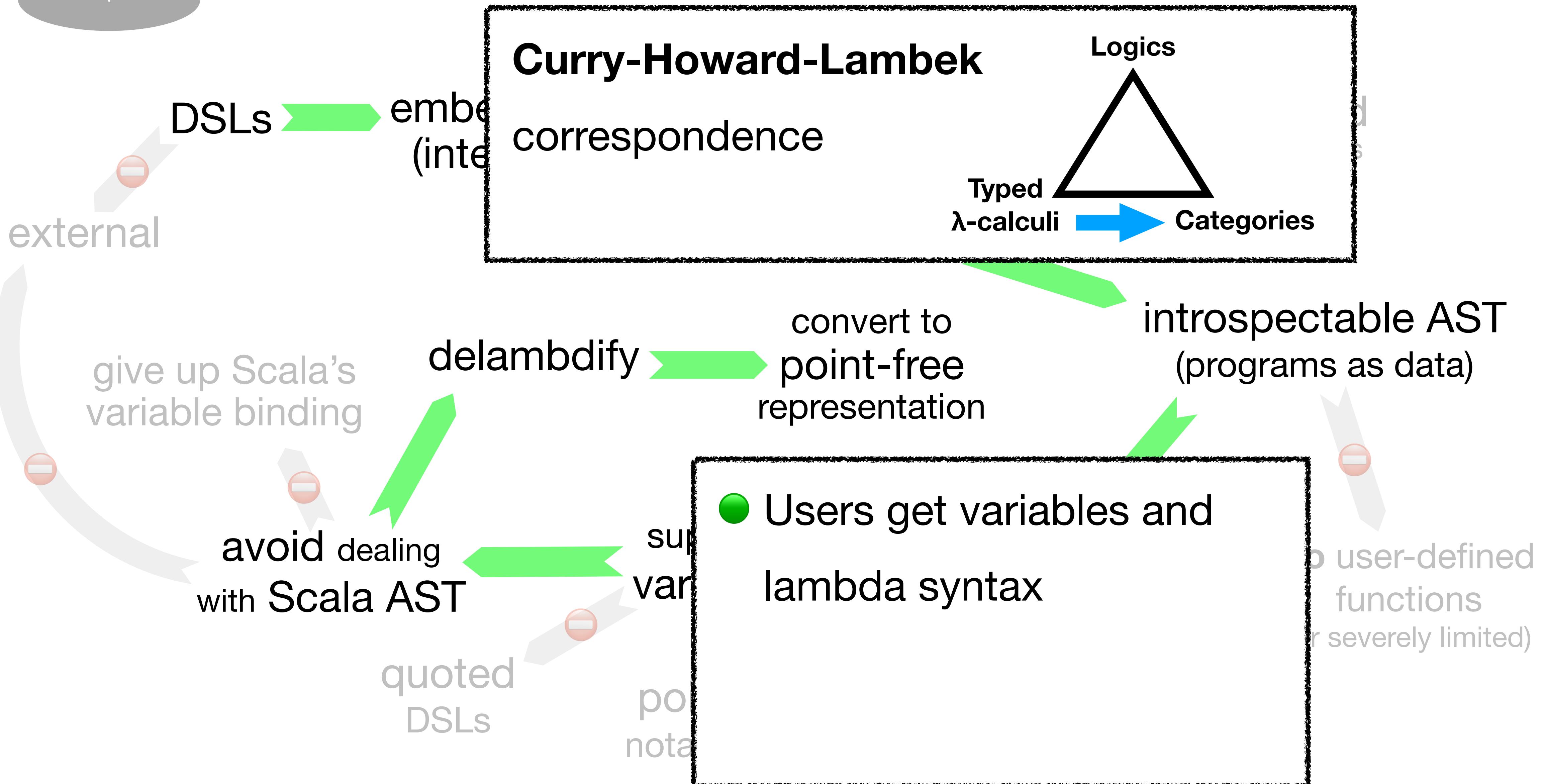


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external
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embed (inter)

Curry-Howard-Lambek
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Logics

Typed
 λ -calculi

Categories

give up Scala's
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avoid dealing
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quoted
DSLs

convert to
point-free
representation

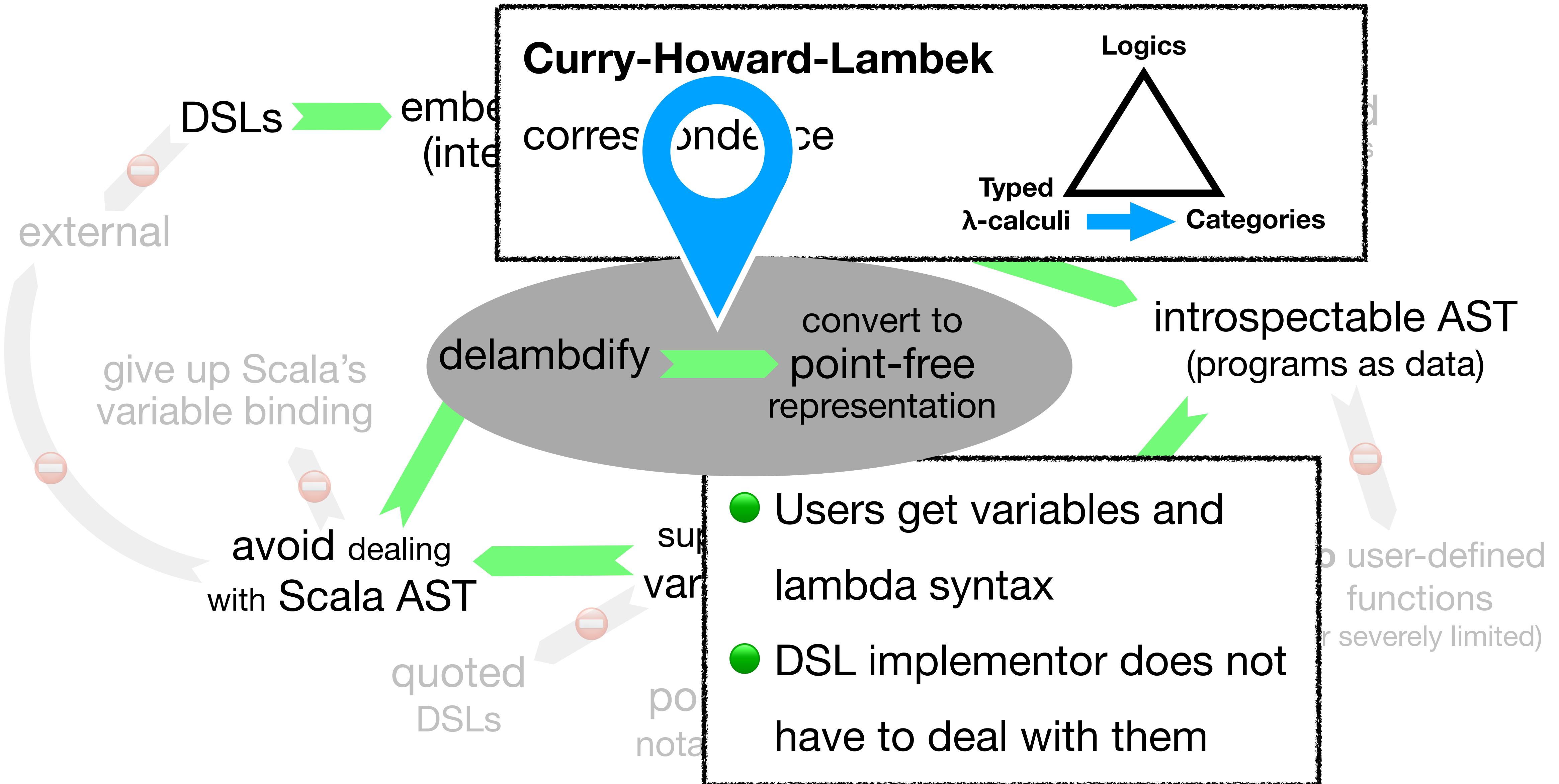
introspectable AST
(programs as data)

- Users get variables and lambda syntax
- DSL implementor does not have to deal with them

user-defined
functions
(or severely limited)

support
variables
point
notation

What This Talk Is About



Goal



Language User

writes lambdas

```
fun { a =>
    val b = f(a)
    val c = g(a)
    h(b, c)
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```

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AndThen(
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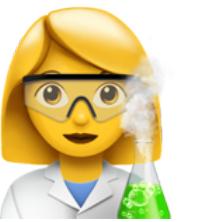
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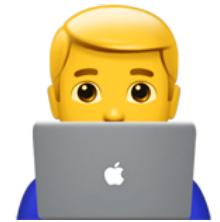
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    ) extends AST[A, C]

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    // ...
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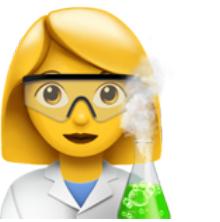
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provided by the
Libretto library



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Demo Domain: Workflows

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“orchestrated and repeatable patterns of activity” – Wikipedia

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 - for activity to complete

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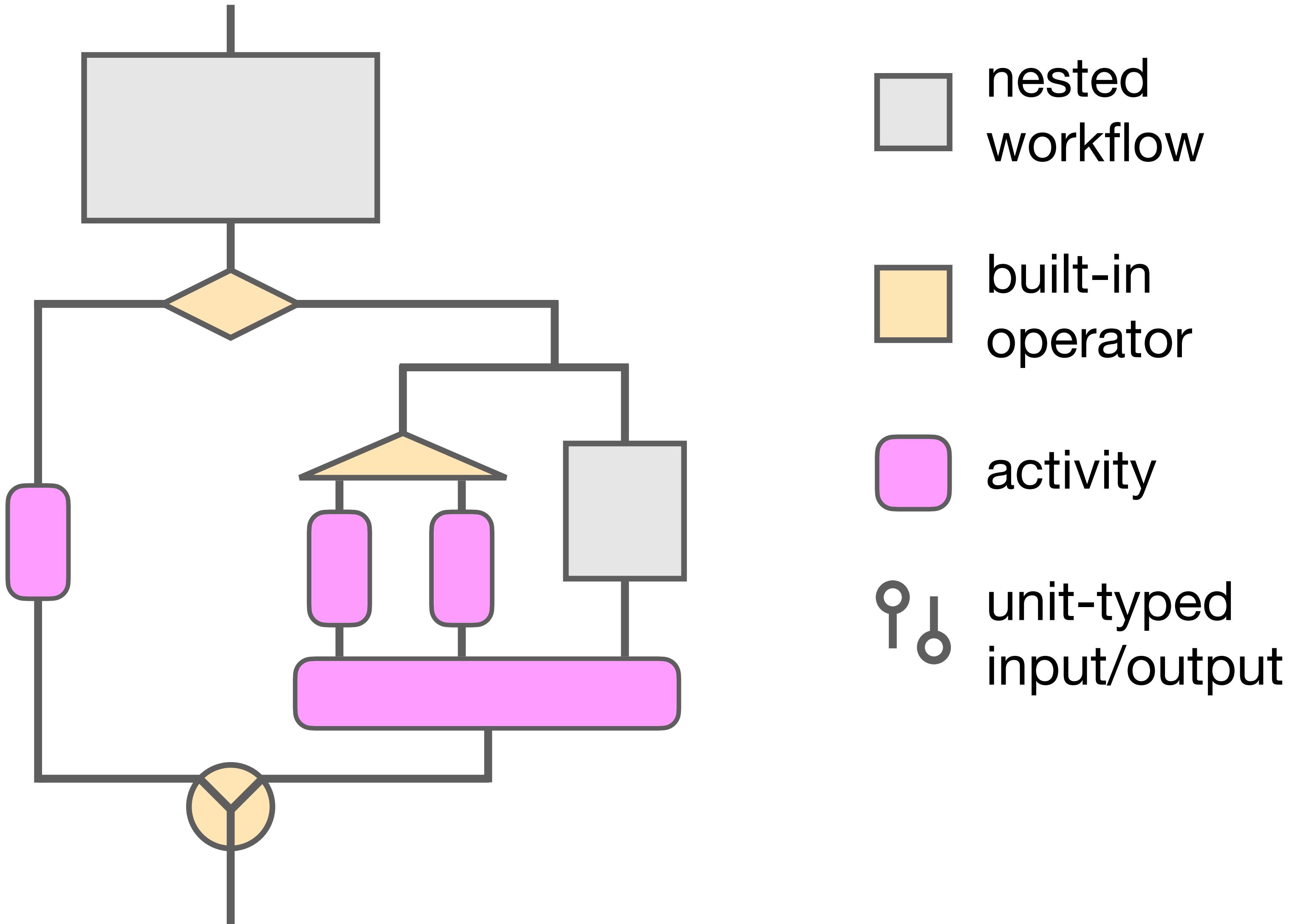
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- (often) long running (hours, days)
- (often) mostly waiting
 - for activity to complete
 - for human input
- require **durable execution**

Demo Domain: Workflows

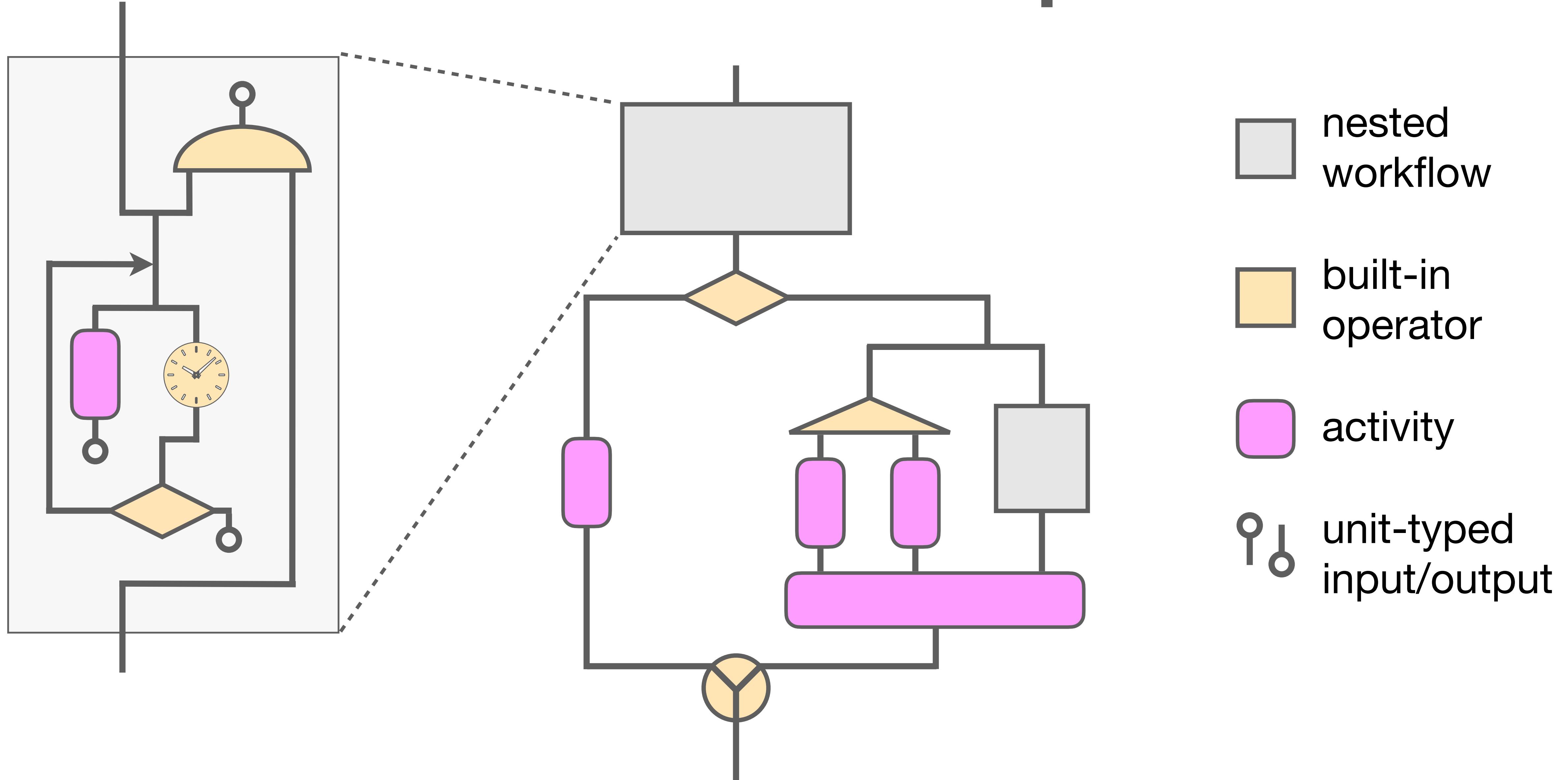
“orchestrated and repeatable patterns of activity” – [Wikipedia](#)

- scripted *activities*
- (often) long running (hours, days)
- (often) mostly waiting
 - for activity to complete
 - for human input
- require **durable execution**
 - can't assume to stay in memory for the whole execution

Workflow: Example



Workflow: Example



Workflow DSL Requirements

Workflow DSL Requirements

- expressive control flow

Workflow DSL Requirements

- expressive control flow
 - branching

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops
 - parallel processing

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops
 - parallel processing
 - sharing intermediate results

Workflow DSL Requirements

- expressive control flow
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 - sharing intermediate results
- (reasonable) type-safety

Workflow DSL Requirements

- expressive control flow
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- (reasonable) type-safety
 - inherited from the host lang

Workflow DSL Requirements

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- **executable durably**

Workflow DSL Requirements

- expressive control flow
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 - parallel processing
 - sharing intermediate results
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- **executable durably**

Maybe later

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops
 - parallel processing
 - sharing intermediate results
 - (reasonable) type-safety
 - inherited from the host lang
 - **executable durably**
- Maybe later**
- graphical rendering

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops
 - parallel processing
 - sharing intermediate results
- (reasonable) type-safety
 - inherited from the host lang
- **executable durably**
 - Maybe later**
 - graphical rendering
 - statically

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops
 - parallel processing
 - sharing intermediate results
 - (reasonable) type-safety
 - inherited from the host lang
 - **executable durably**
- Maybe later**
- graphical rendering
 - statically
 - mid-execution

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops
 - parallel processing
 - sharing intermediate results
 - (reasonable) type-safety
 - inherited from the host lang
 - **executable durably**
- Maybe later**
- graphical rendering
 - statically
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 - static analyses

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops
 - parallel processing
 - sharing intermediate results
 - (reasonable) type-safety
 - inherited from the host lang
 - **executable durably**
- Maybe later**
- graphical rendering
 - statically
 - mid-execution
 - static analyses
 - execution traces

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops
 - parallel processing
 - sharing intermediate results
 - (reasonable) type-safety
 - inherited from the host lang
 - **executable durably**
- Maybe later**
- graphical rendering
 - statically
 - mid-execution
 - static analyses
 - execution traces
 - switch to an external DSL later

Workflow DSL Requirements

- expressive control flow
 - branching
 - loops
 - parallel processing
 - sharing intermediate results
 - (reasonable) type-safety
 - inherited from the host lang
 - **executable durably**
- Maybe later**
- graphical rendering
 - statically
 - mid-execution
 - static analyses
 - execution traces
 - switch to an external DSL later
 - *without having to rewrite old workflows*

Demo Sub-Domain: Background Check

Inspired by <https://learn.temporal.io/examples/go/background-checks/>

Demo Sub-Domain: Background Check

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- HR person initiates

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- HR person initiates
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 - Ask candidate (via email) to accept

Demo Sub-Domain: Background Check

Inspired by <https://learn.temporal.io/examples/go/background-checks/>

- HR person initiates
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 - Ask candidate (via email) to accept
 - Candidate accepts by providing

Demo Sub-Domain: Background Check

Inspired by <https://learn.temporal.io/examples/go/background-checks/>

- HR person initiates
 - Inputs candidate email
 - Ask candidate (via email) to accept
 - Candidate accepts by providing
 - Personal info

Demo Sub-Domain: Background Check

Inspired by <https://learn.temporal.io/examples/go/background-checks/>

- HR person initiates
 - Inputs candidate email
 - Ask candidate (via email) to accept
 - Candidate accepts by providing
 - Personal info
 - Employment history

Demo Sub-Domain: Background Check

Inspired by <https://learn.temporal.io/examples/go/background-checks/>

- HR person initiates
 - Concurrently
- Inputs candidate email
- Ask candidate (via email) to accept
- Candidate accepts by providing
 - Personal info
 - Employment history

Demo Sub-Domain: Background Check

Inspired by <https://learn.temporal.io/examples/go/background-checks/>

- HR person initiates
 - Inputs candidate email
 - Ask candidate (via email) to accept
 - Candidate accepts by providing
 - Personal info
 - Employment history
 - Concurrently
 - Check criminal record

Demo Sub-Domain: Background Check

Inspired by <https://learn.temporal.io/examples/go/background-checks/>

- HR person initiates
 - Inputs candidate email
 - Ask candidate (via email) to accept
 - Candidate accepts by providing
 - Personal info
 - Employment history
- Concurrently
 - Check criminal record
 - Check civil record

Demo Sub-Domain: Background Check

Inspired by <https://learn.temporal.io/examples/go/background-checks/>

- HR person initiates
 - Inputs candidate email
 - Ask candidate (via email) to accept
 - Candidate accepts by providing
 - Personal info
 - Employment history
- Concurrently
 - Check criminal record
 - Check civil record
 - Verify employment history

Demo Sub-Domain: Background Check

Inspired by <https://learn.temporal.io/examples/go/background-checks/>

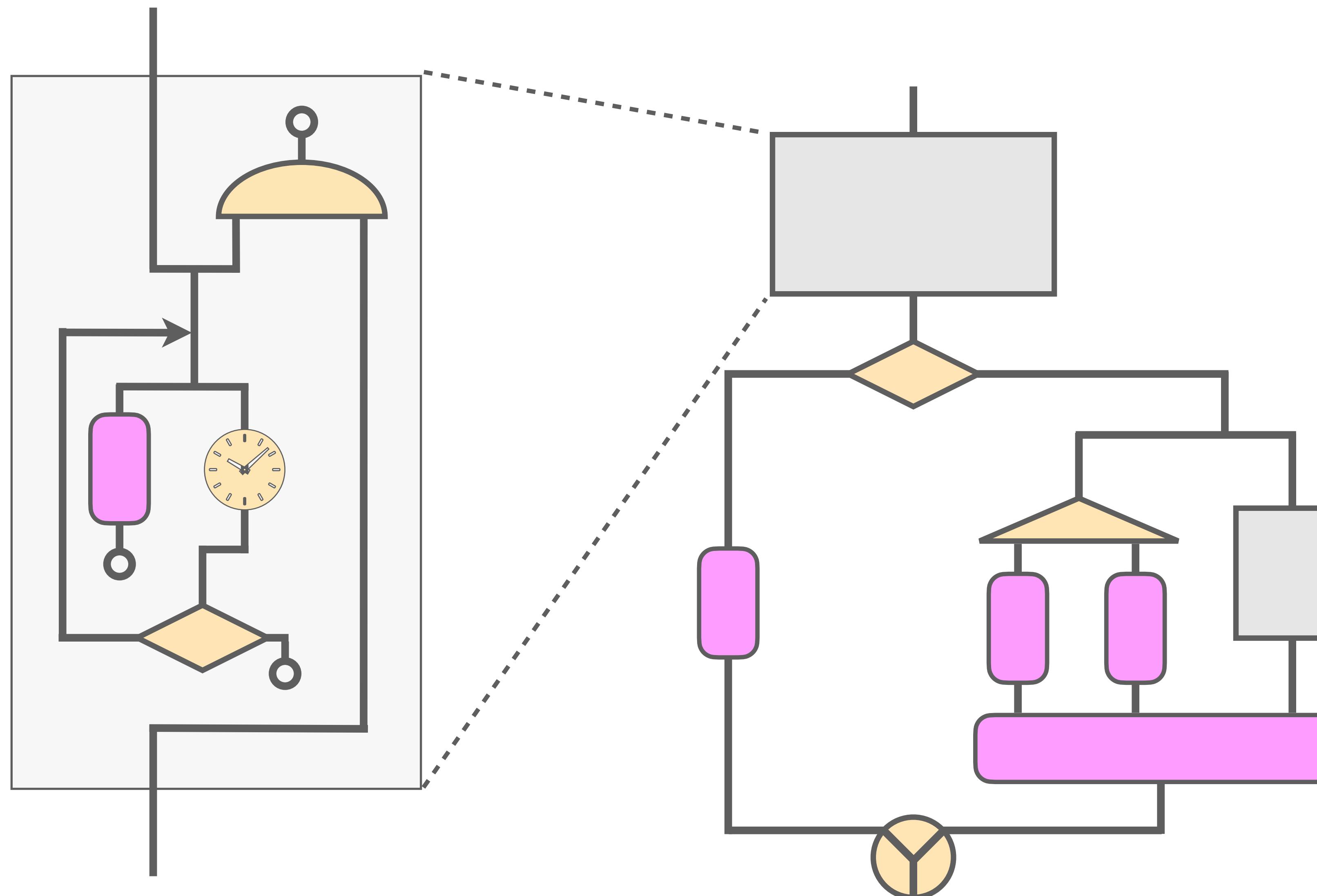
- HR person initiates
 - Inputs candidate email
 - Ask candidate (via email) to accept
 - Candidate accepts by providing
 - Personal info
 - Employment history
- Concurrently
 - Check criminal record
 - Check civil record
 - Verify employment history
 - Notify a human researcher

Demo Sub-Domain: Background Check

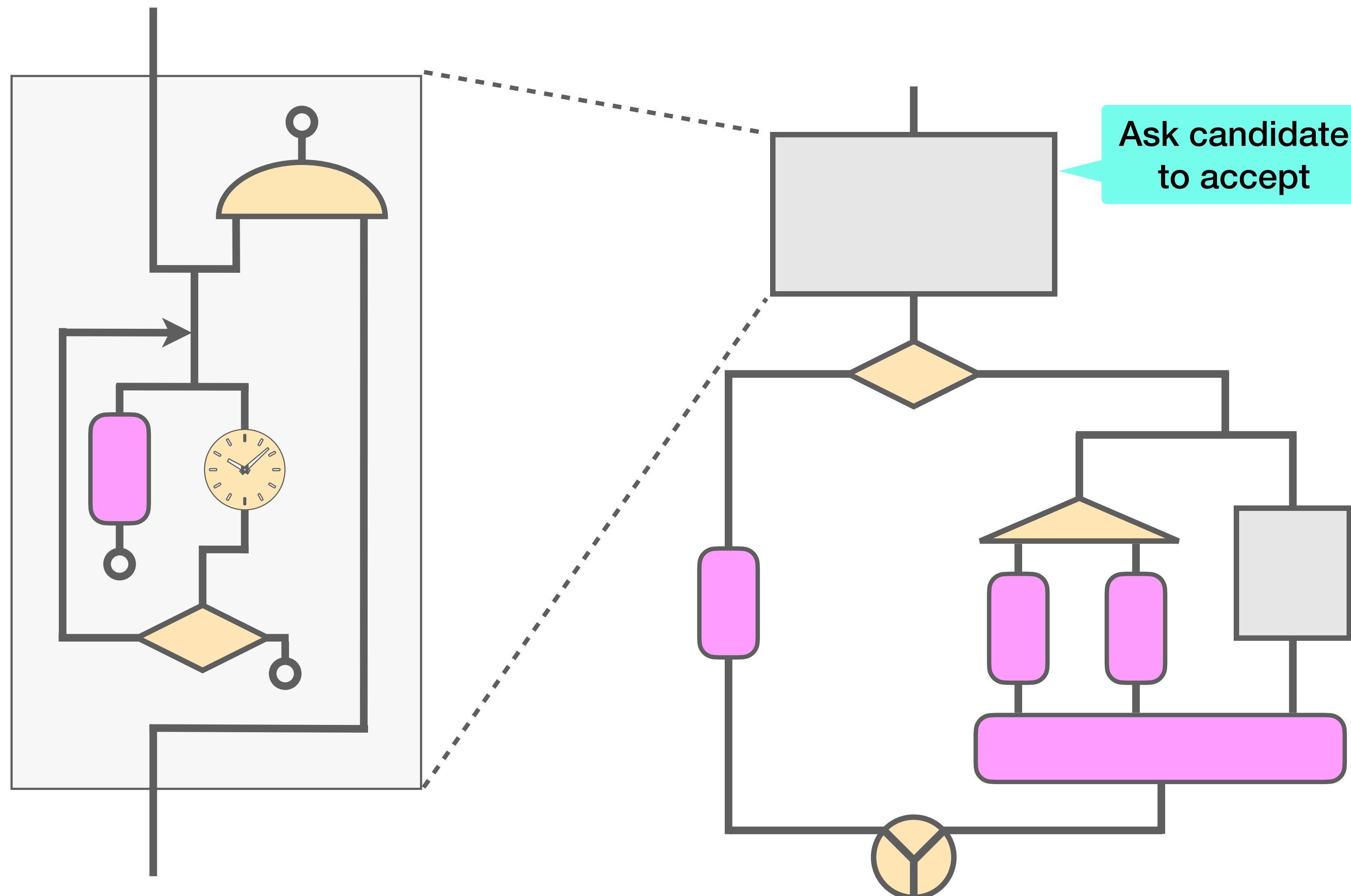
Inspired by <https://learn.temporal.io/examples/go/background-checks/>

- HR person initiates
 - Inputs candidate email
 - Ask candidate (via email) to accept
 - Candidate accepts by providing
 - Personal info
 - Employment history
- Concurrently
 - Check criminal record
 - Check civil record
 - Verify employment history
 - Notify a human researcher
 - Produce report (for the HR person)

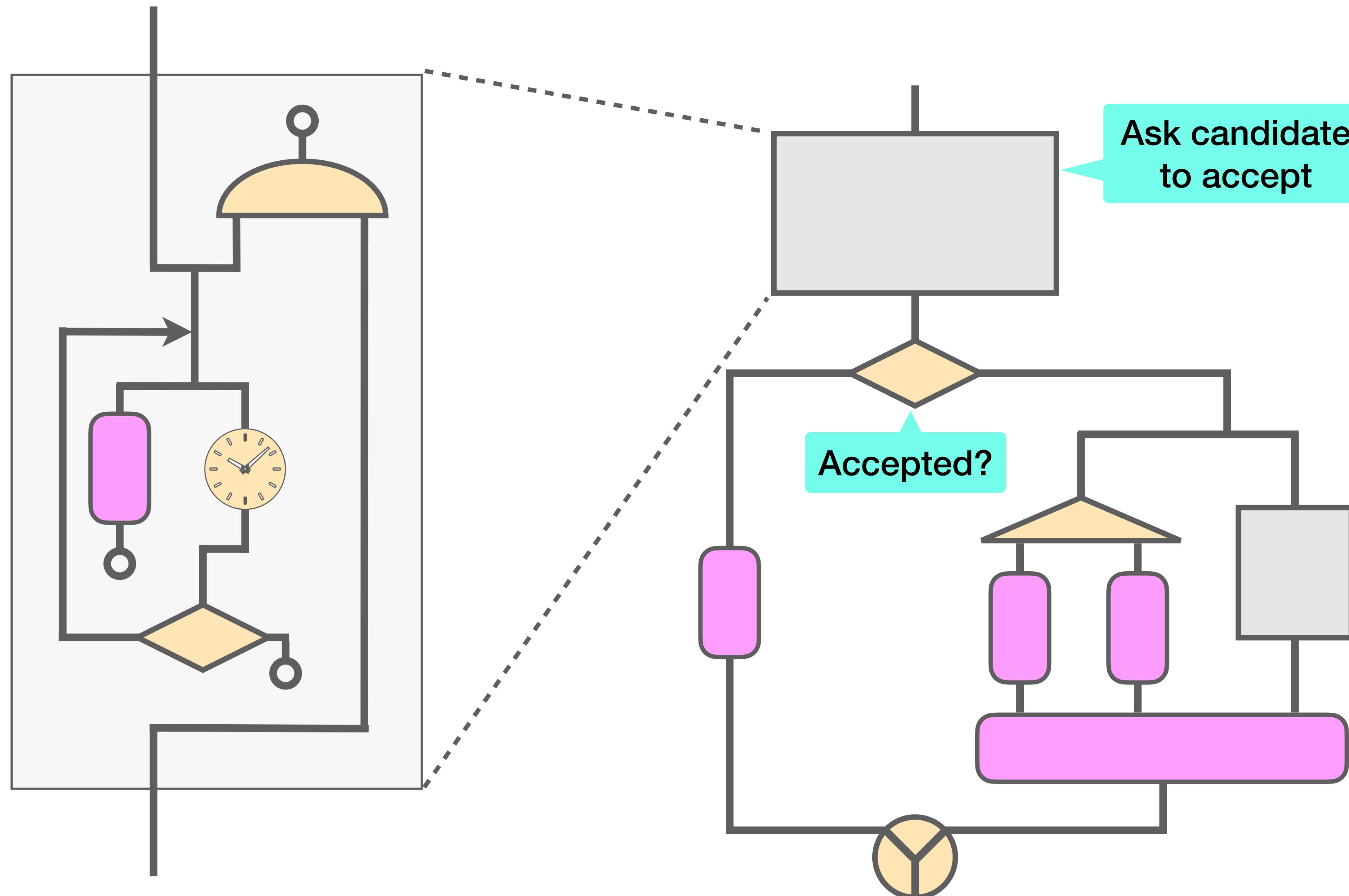
Background Check Workflow



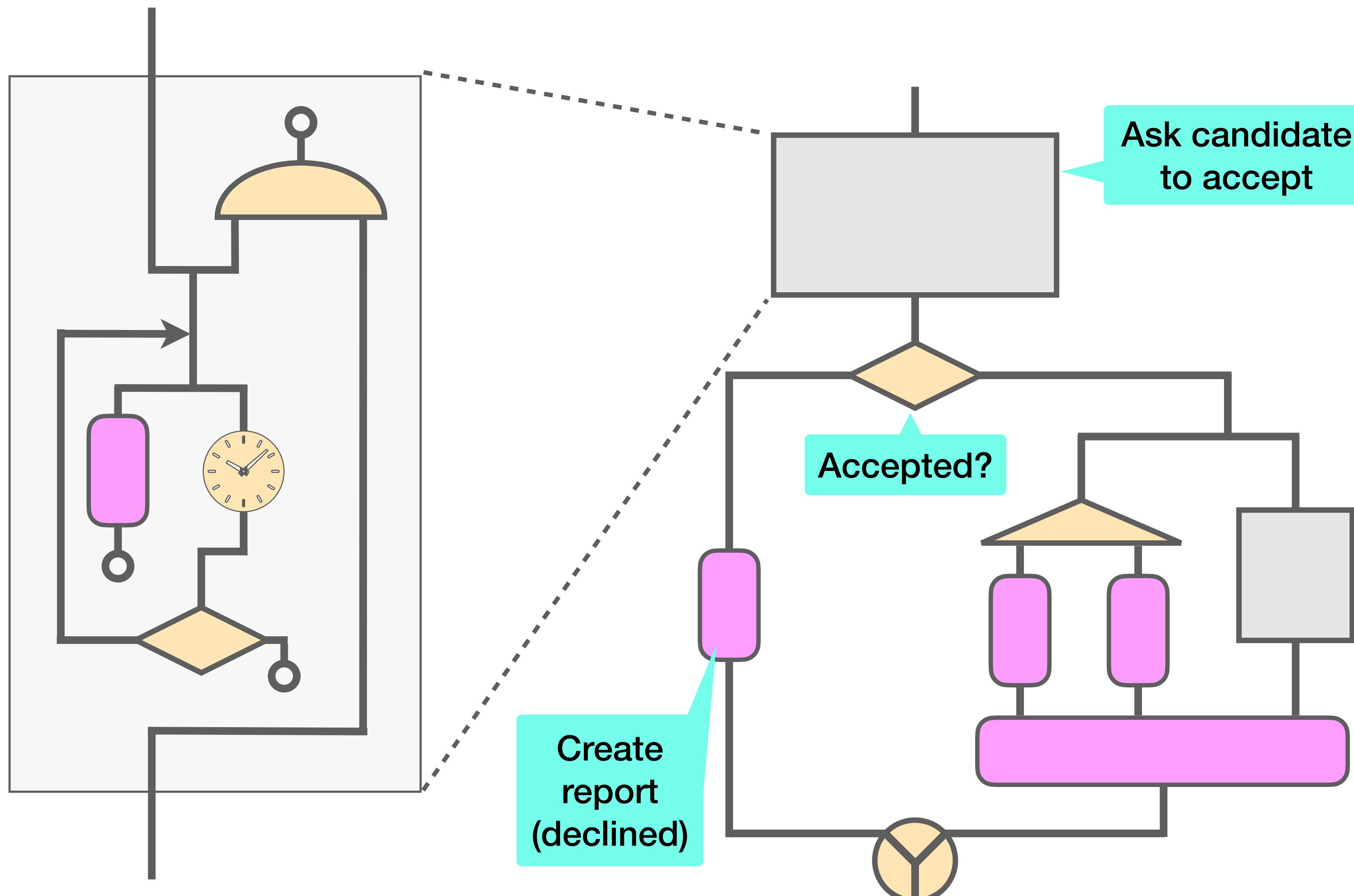
Background Check Workflow



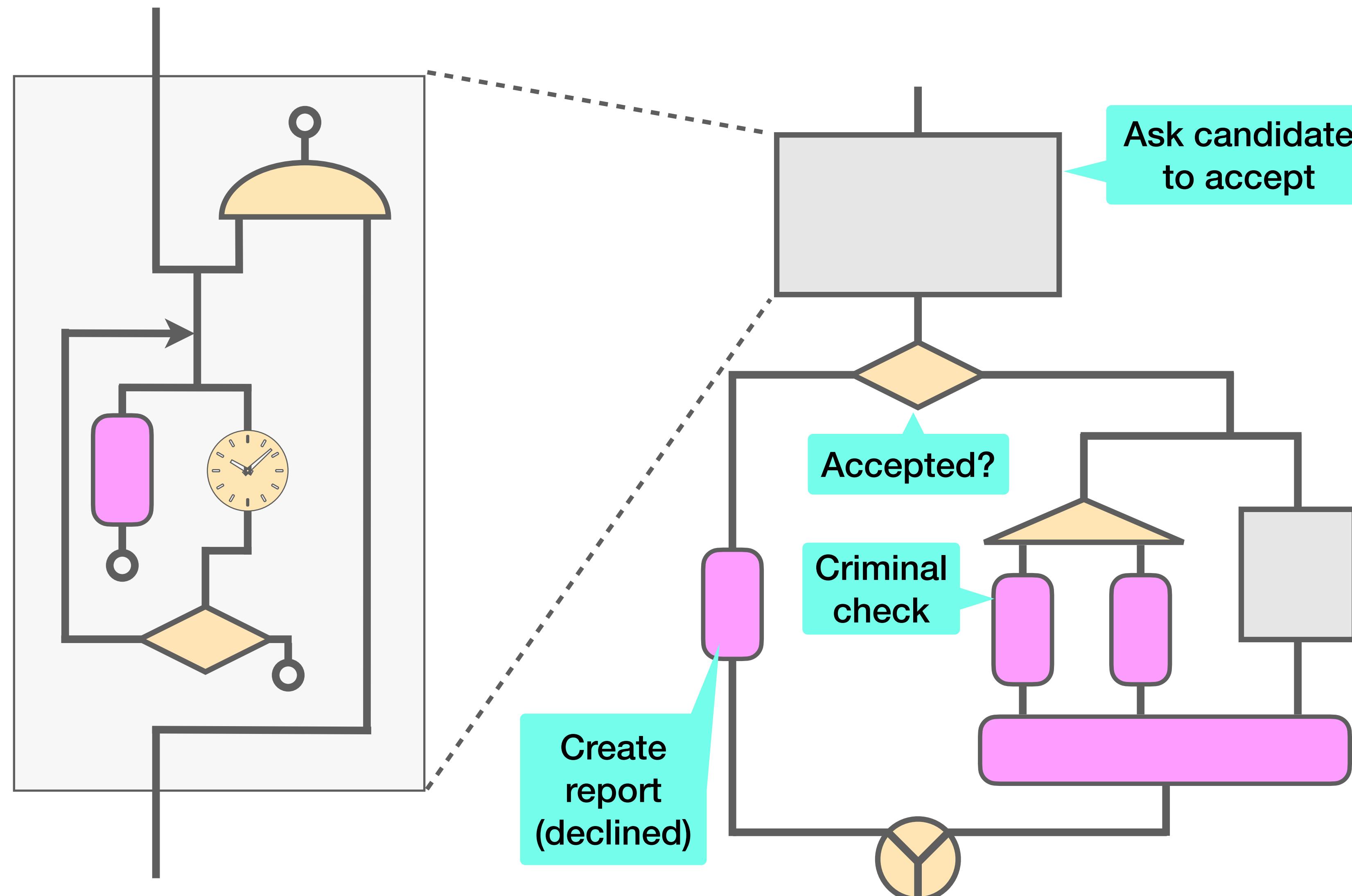
Background Check Workflow



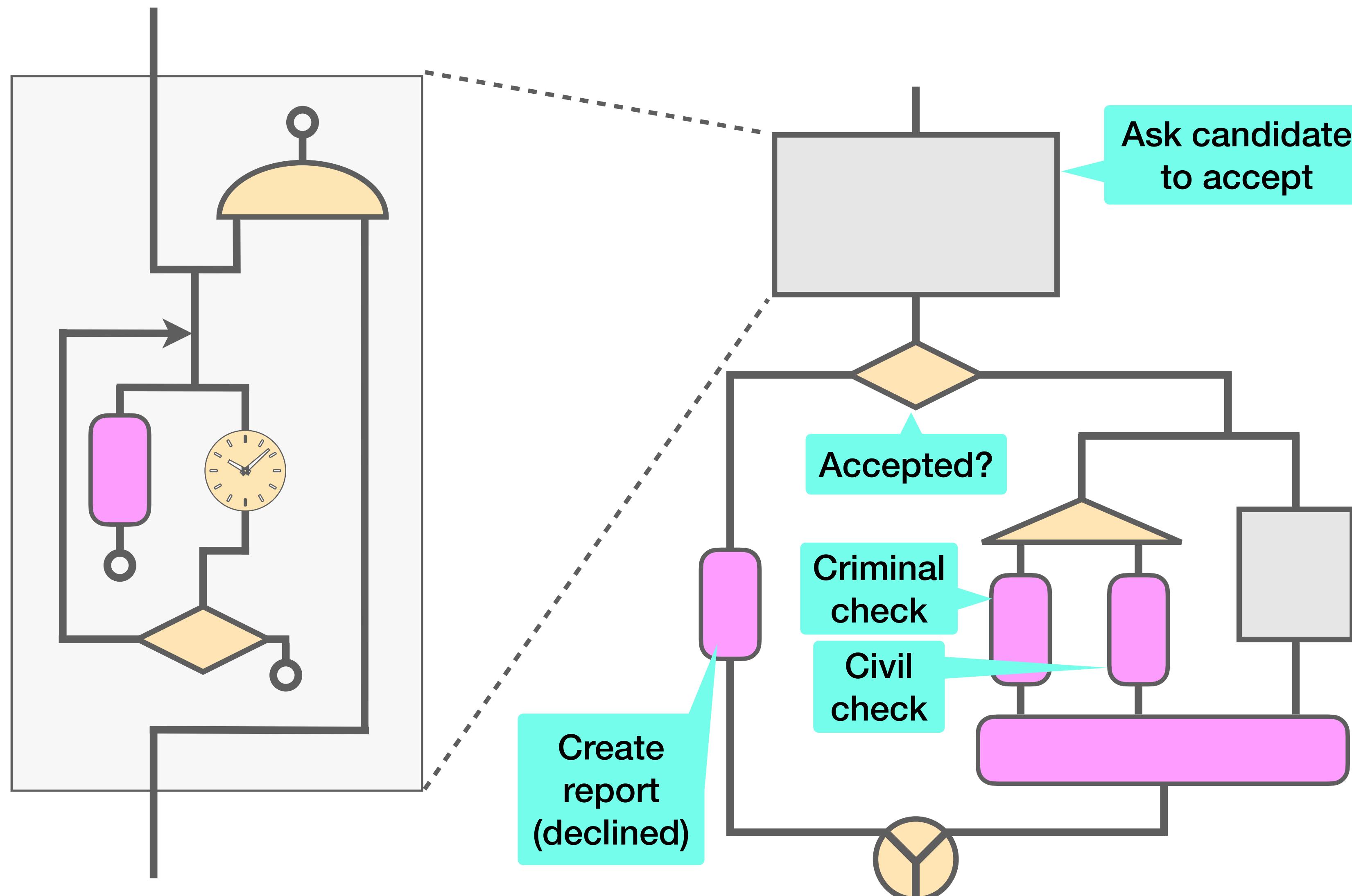
Background Check Workflow



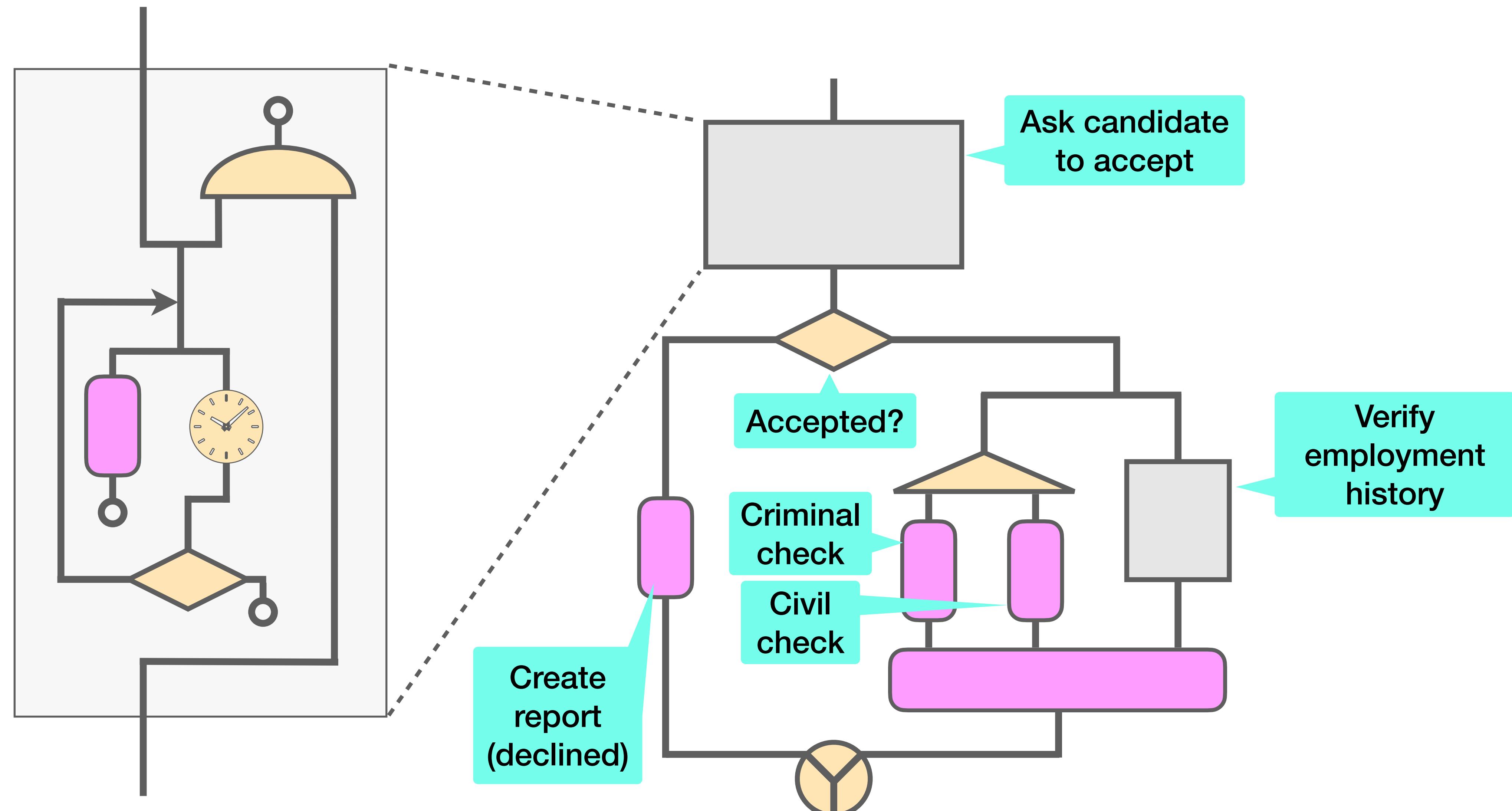
Background Check Workflow



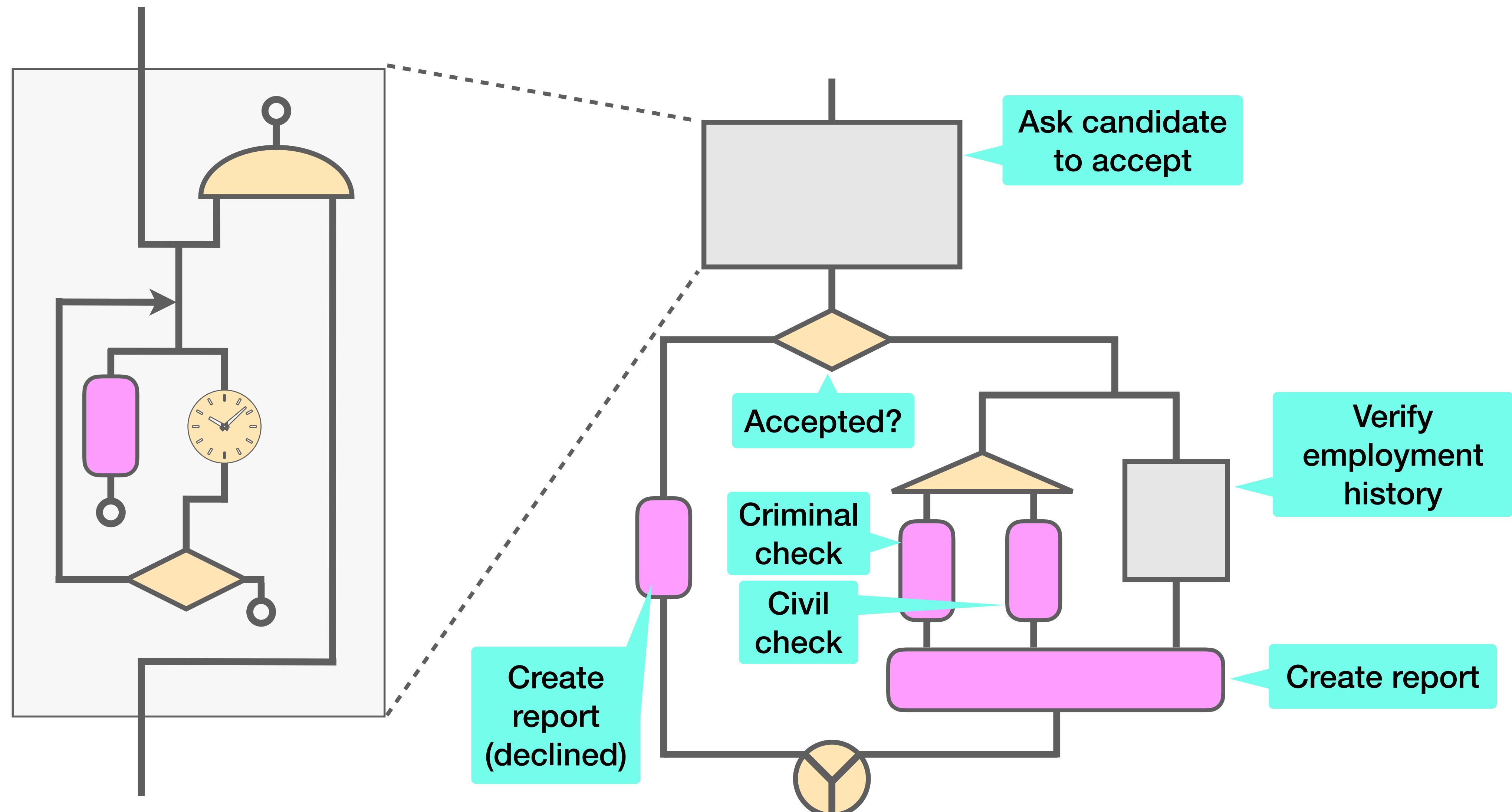
Background Check Workflow



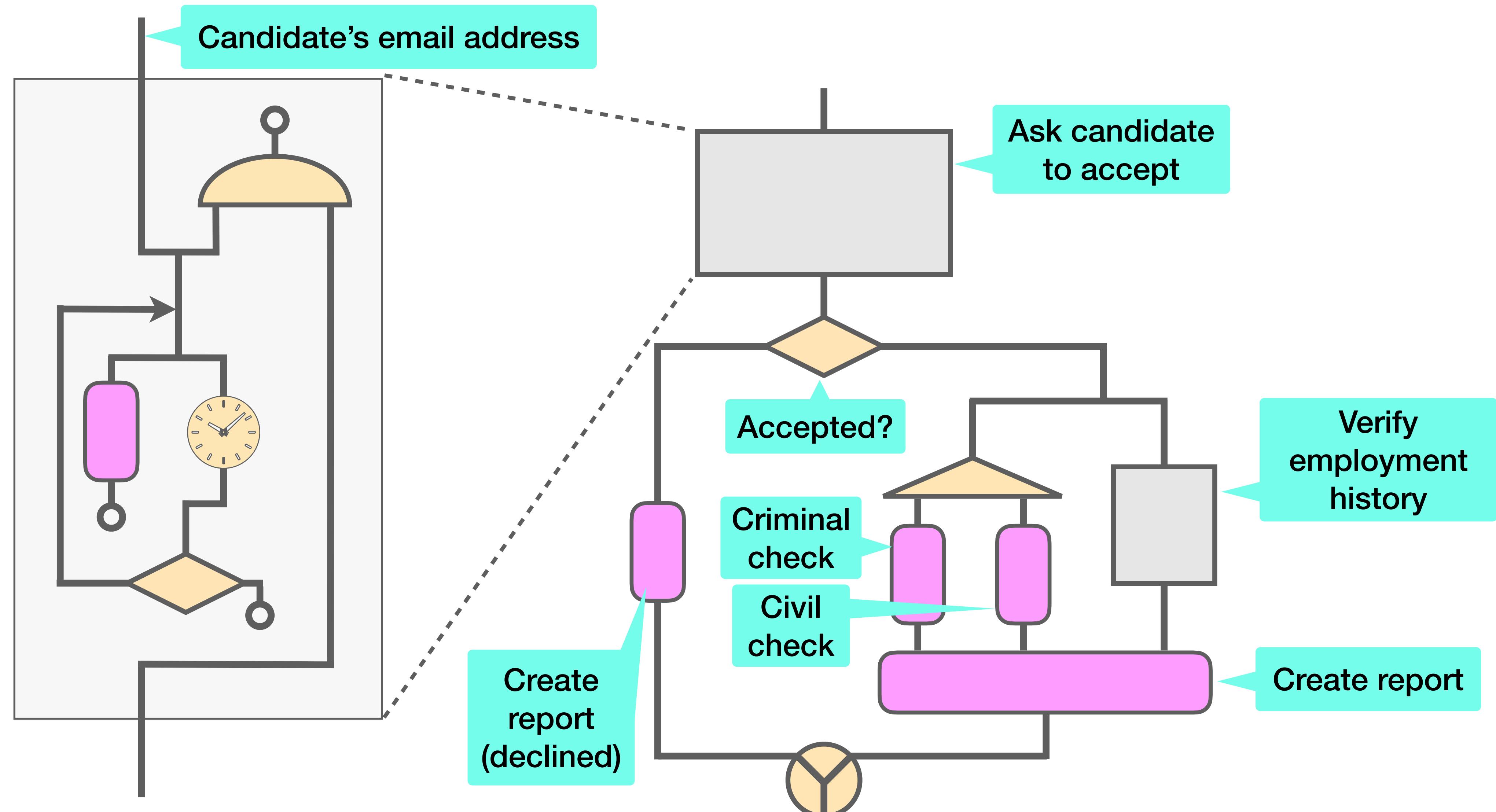
Background Check Workflow



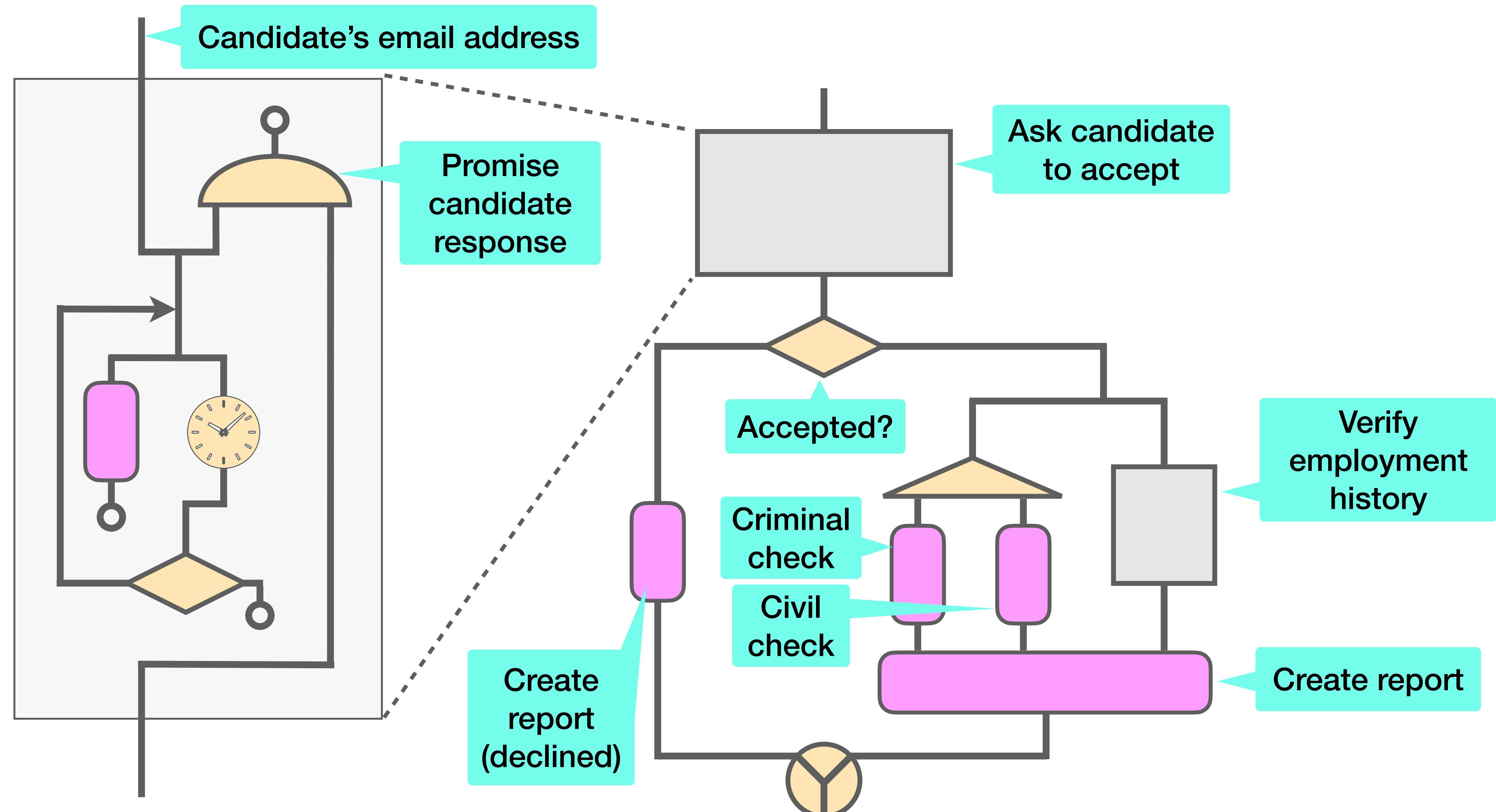
Background Check Workflow



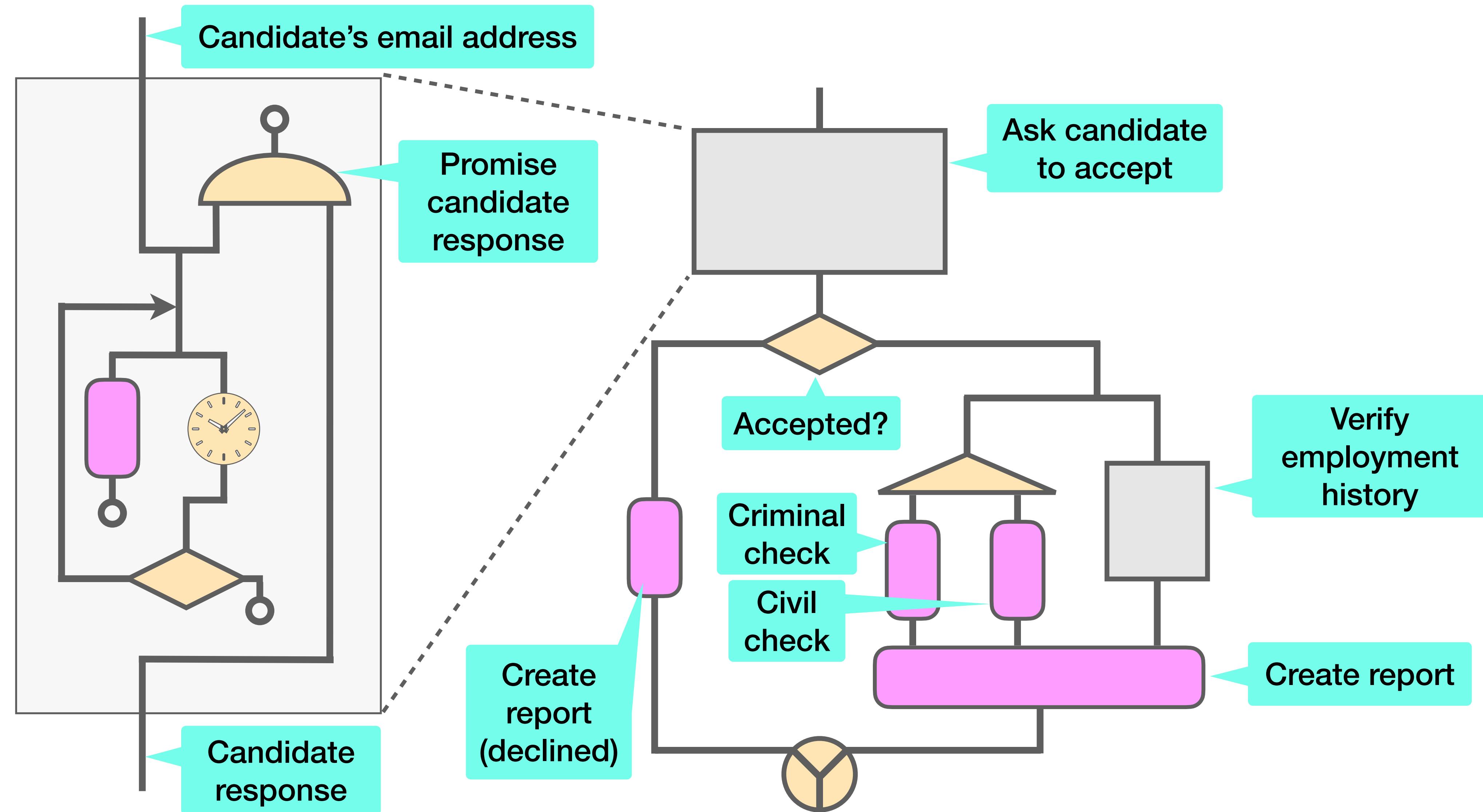
Background Check Workflow



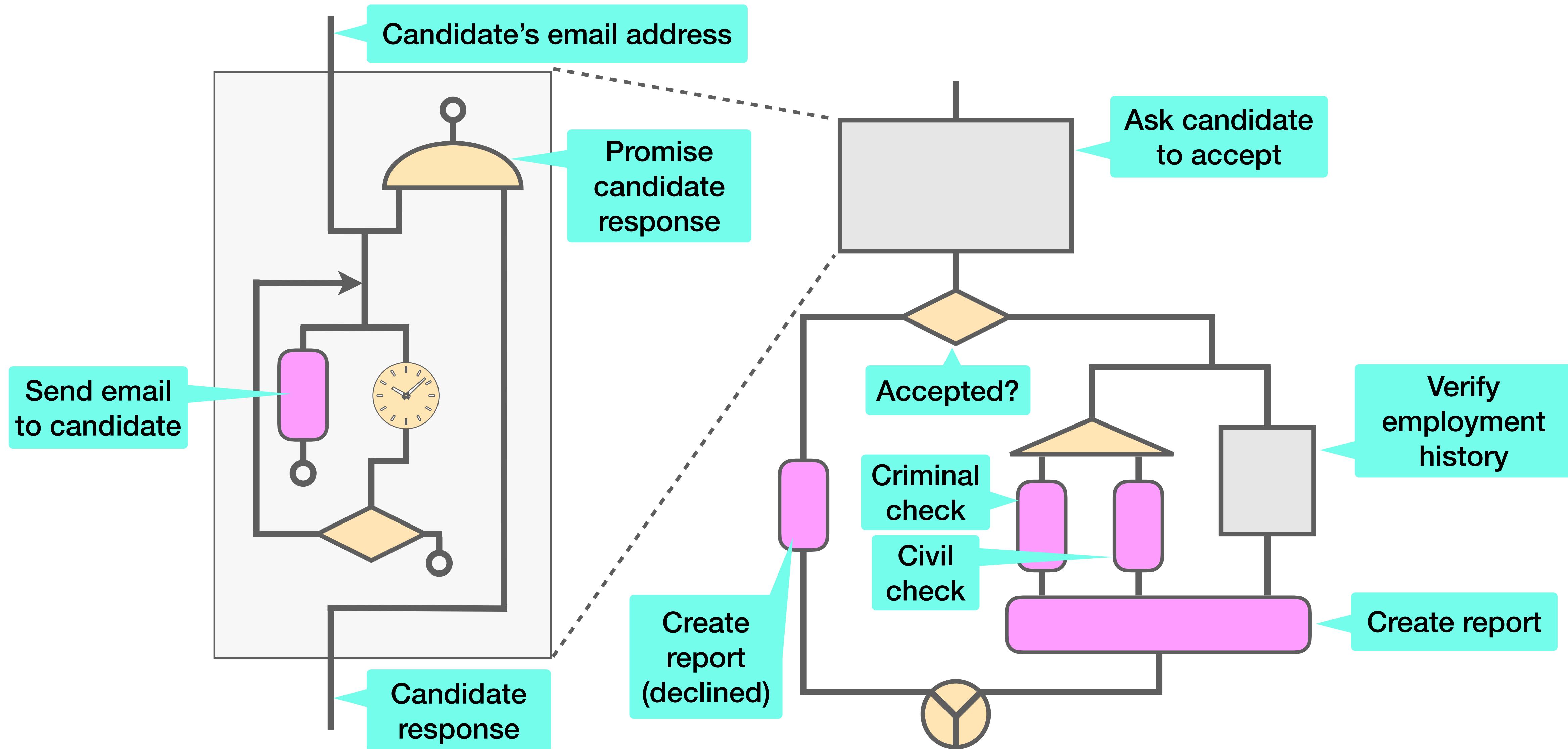
Background Check Workflow



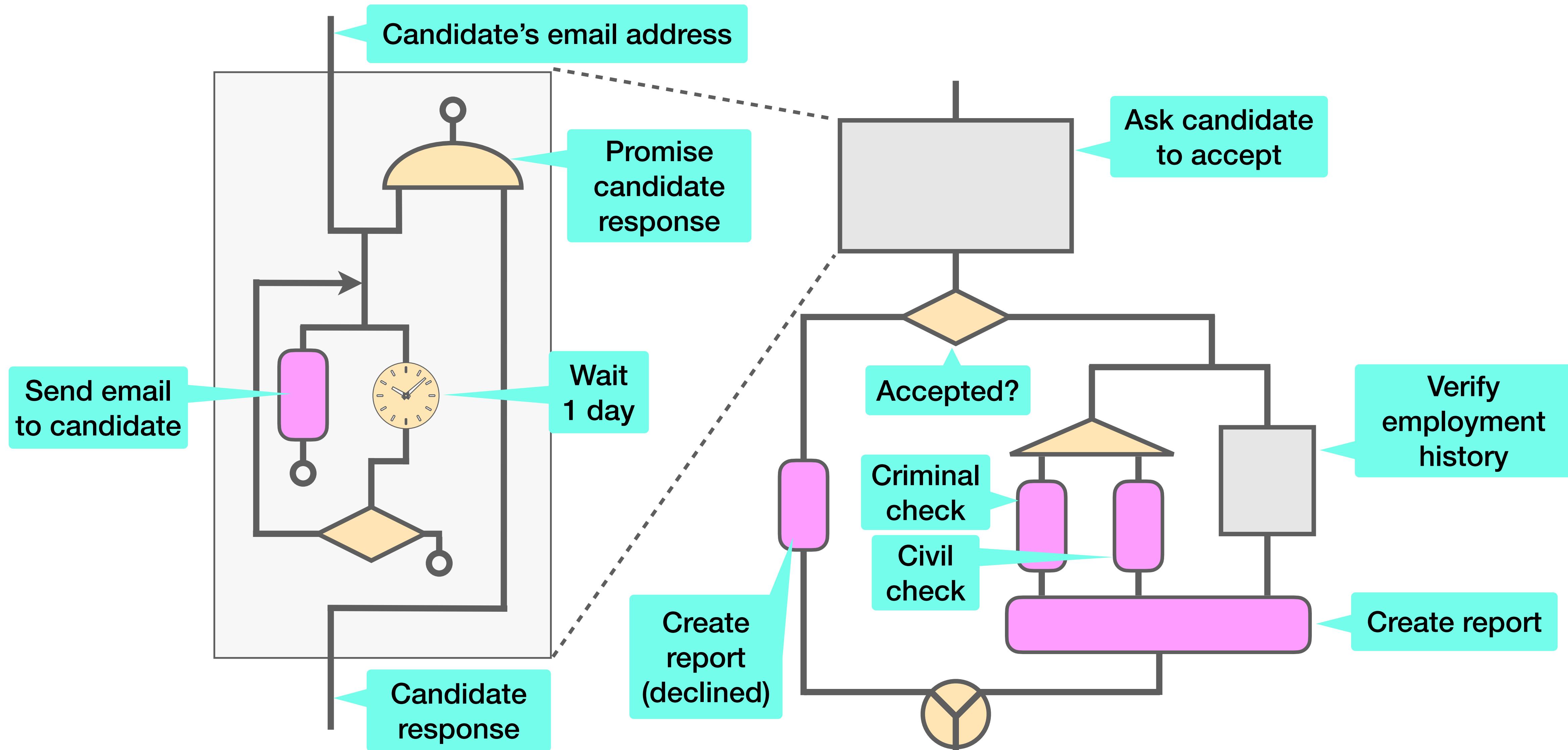
Background Check Workflow



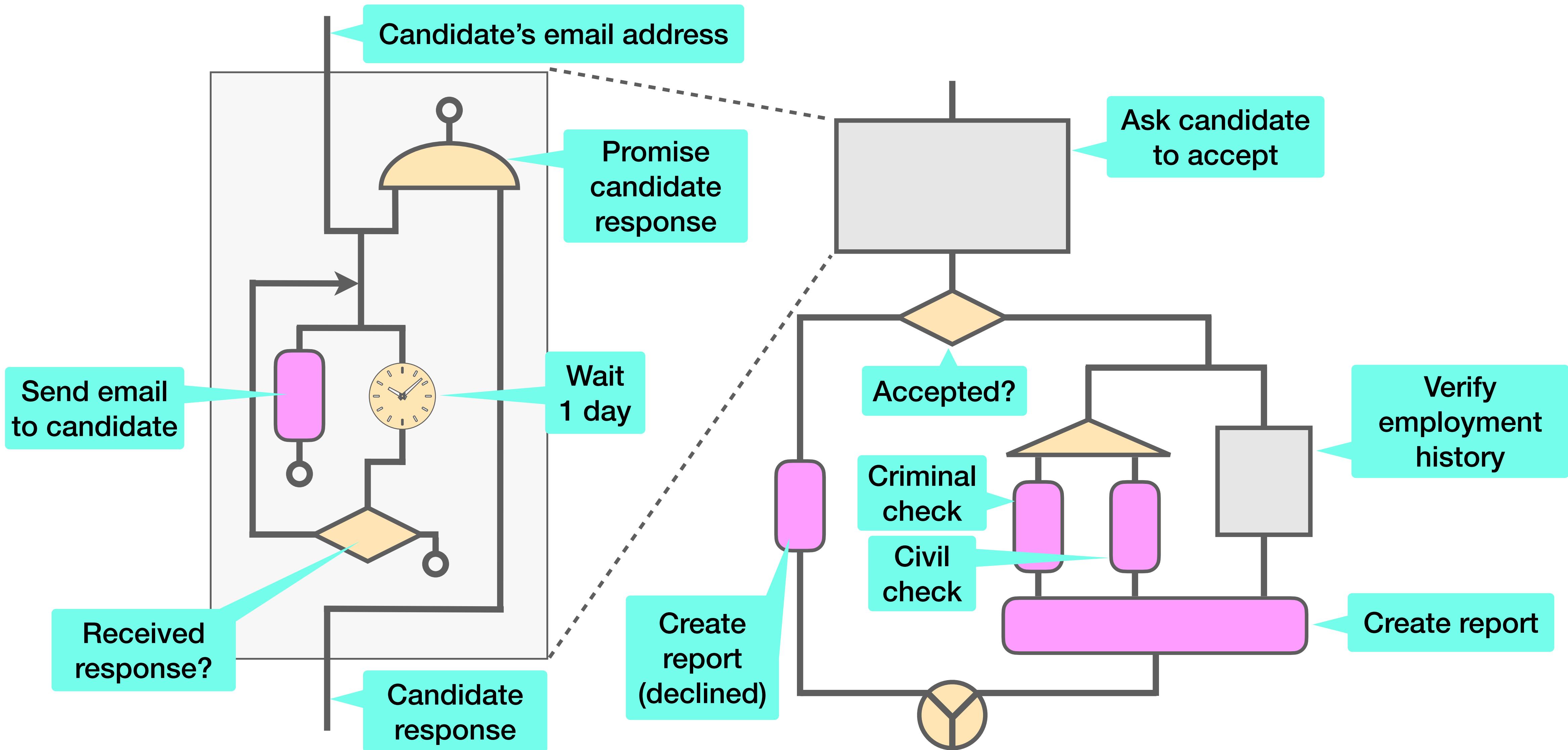
Background Check Workflow



Background Check Workflow



Background Check Workflow





User Code

```
val backgroundCheck: Flow[EmailAddress, Report] =  
  Flow { candidate =>  
    askForAcceptance(candidate) switch {  
      case Left(x) =>  
        Report.declined(x)  
      case Right(personalId ** employmentHistory) =>  
        val crimi = checkCrimi(personalId)  
        val civil = checkCivil(personalId)  
        val verif = verify(employmentHistory)  
        Report.results(crimi ** civil ** verif)  
    }  
  }
```



User Code

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val backgroundCheck: Flow[EmailAddress, Report] =  
  Flow { candidate =>  
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- Lambdas



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```

- Lambdas
- Pattern matching



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```

- Lambdas
- Pattern matching
- Auxiliary variables



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val backgroundCheck: Flow[EmailAddress, Report] =  
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        Report.results(crimi ** civil ** verif)  
    }  
  }
```

- Lambdas
- Pattern matching
- Auxiliary variables



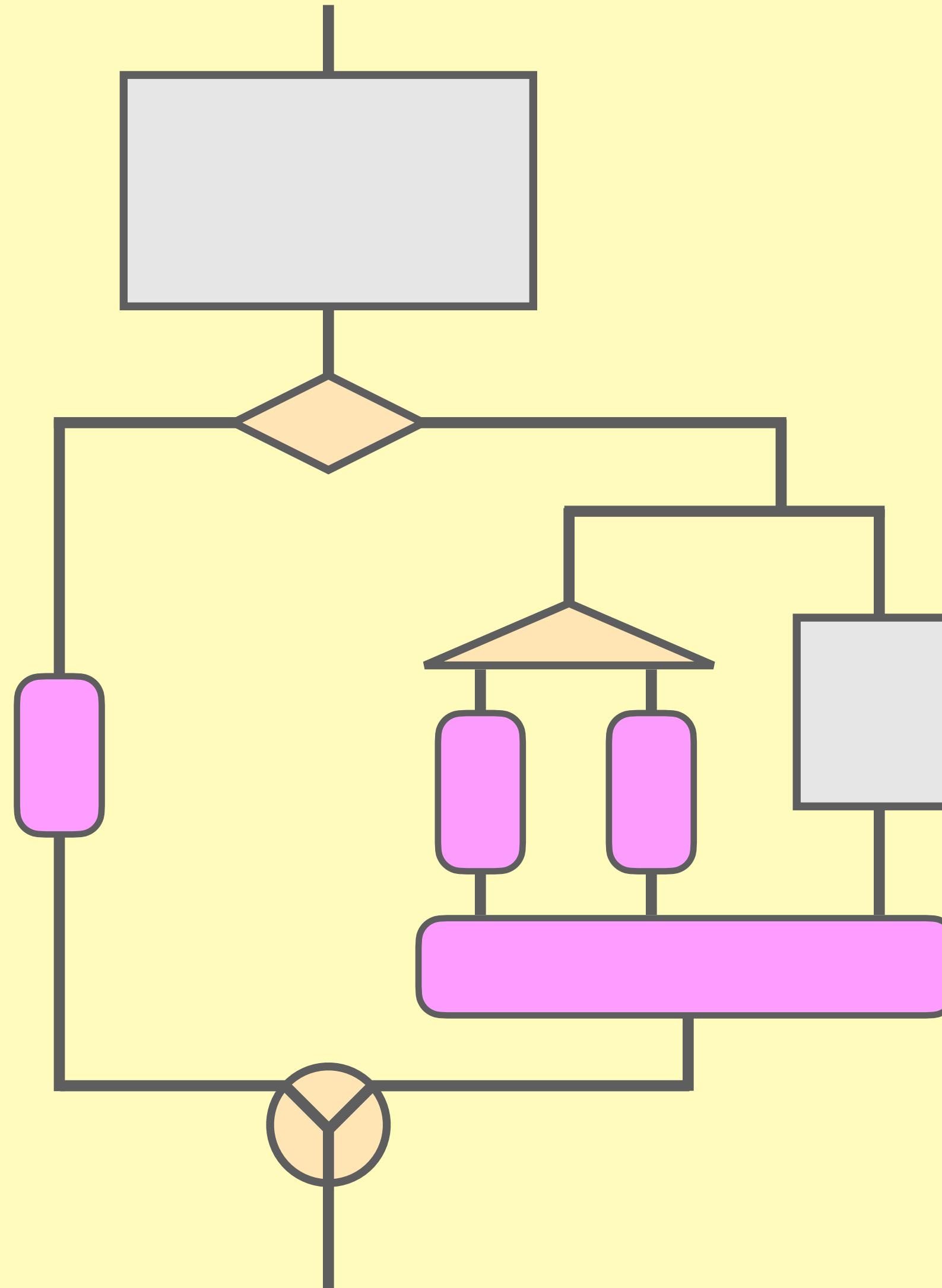
Internal Representation

```
AndThen(  
    askForAcceptance,  
    Switch(  
        Report.declined,  
        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            Report.results  
        )))
```



Internal Representation

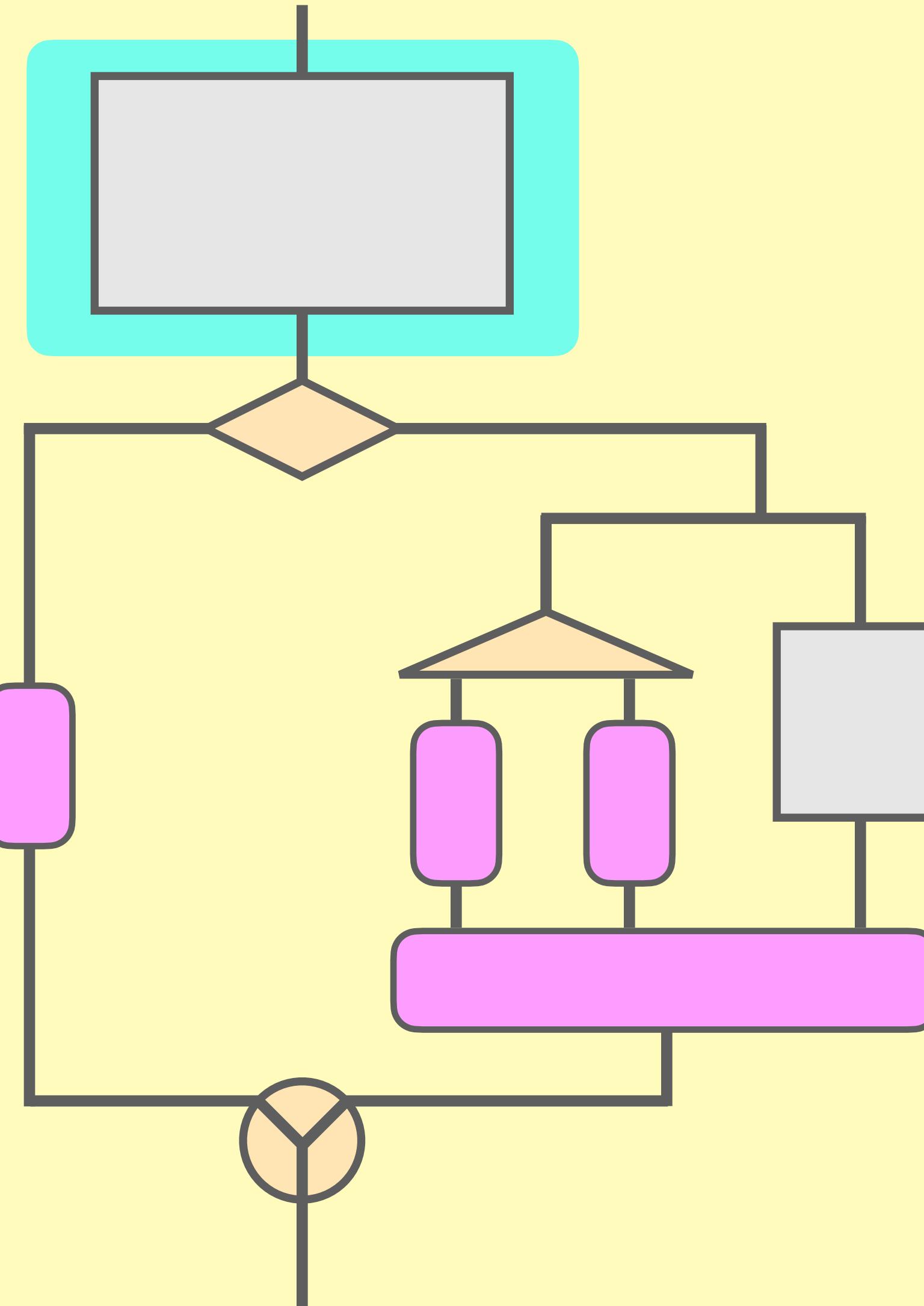
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        )))
```





Internal Representation

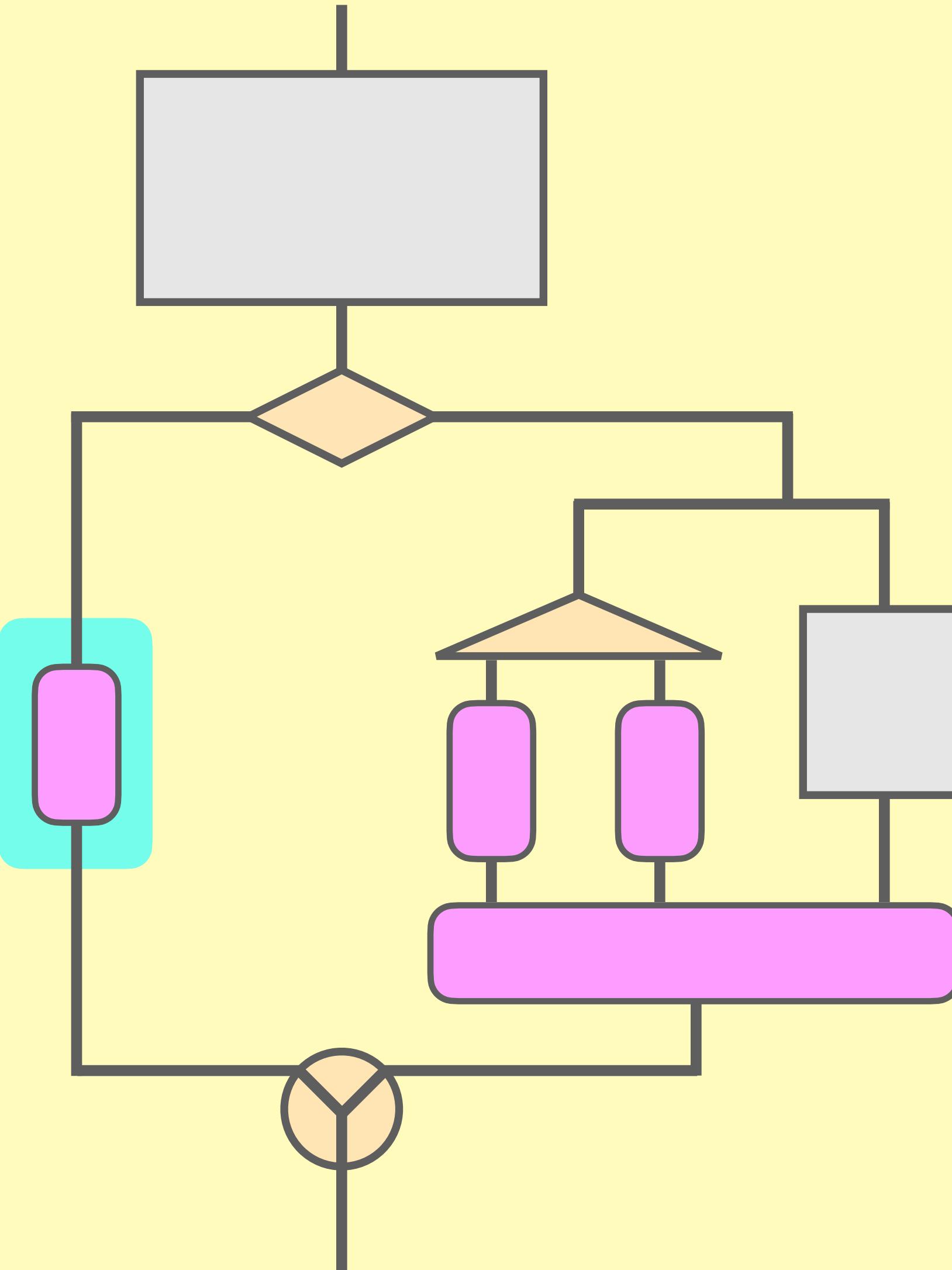
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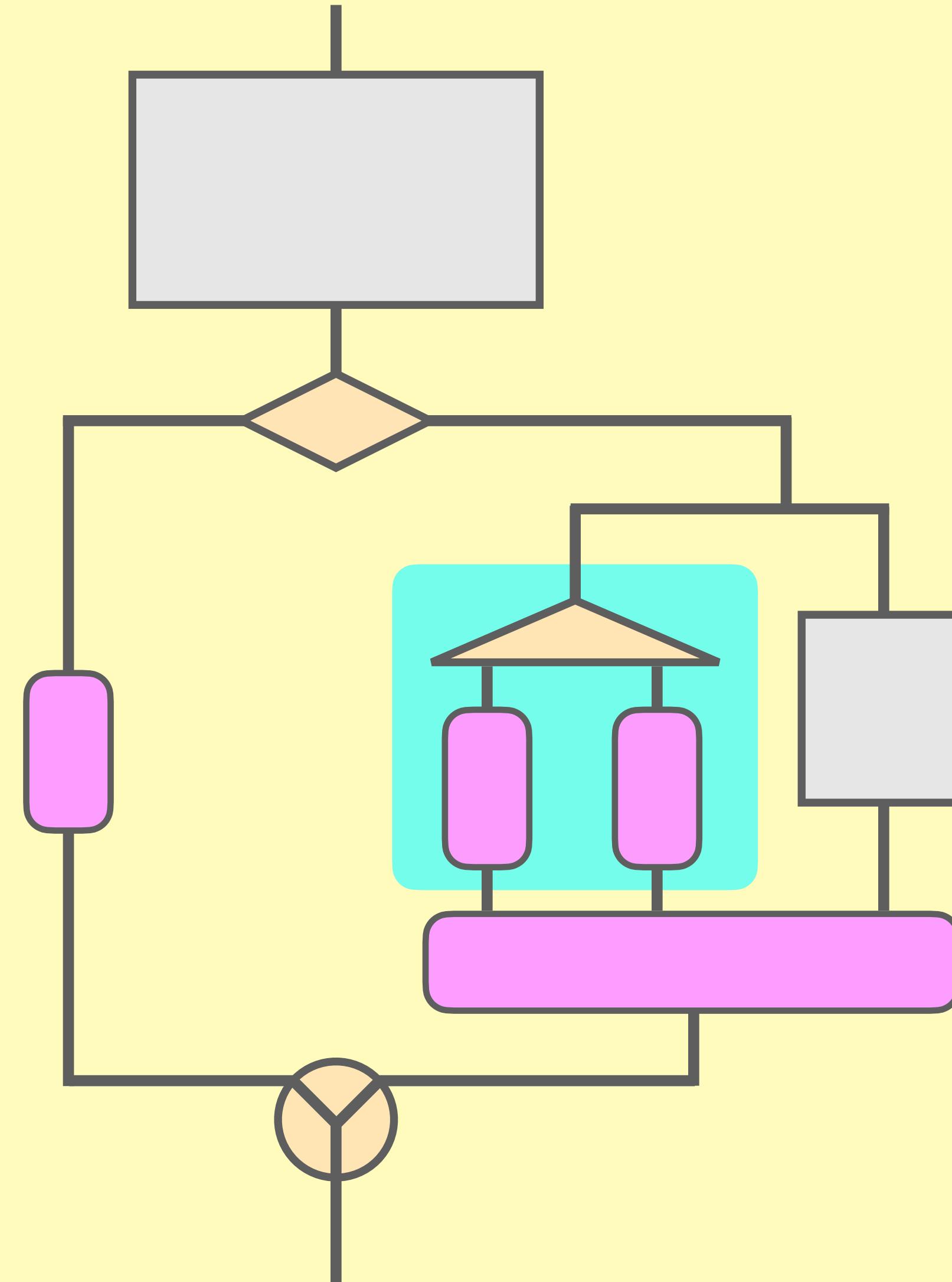
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Internal Representation

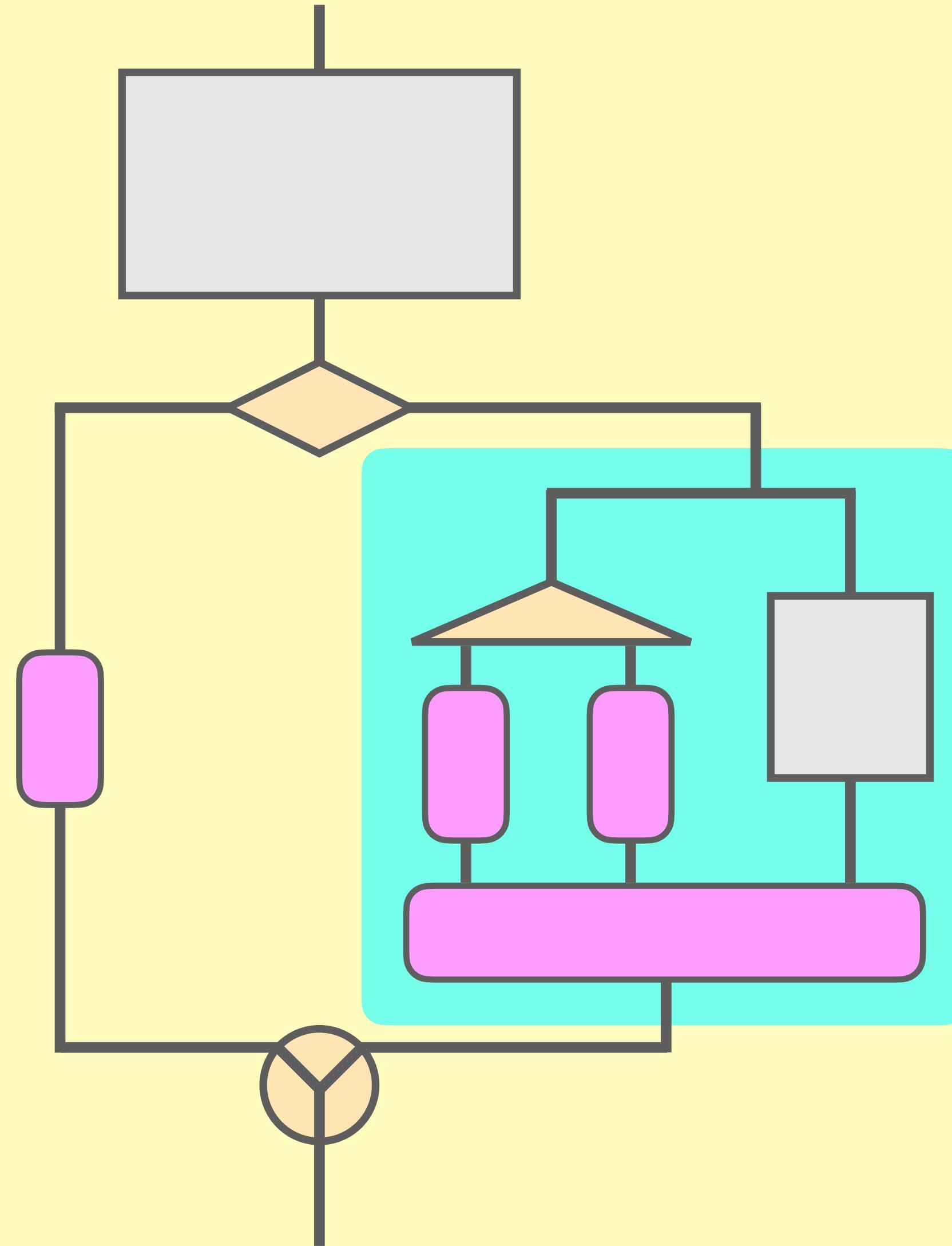
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Internal Representation

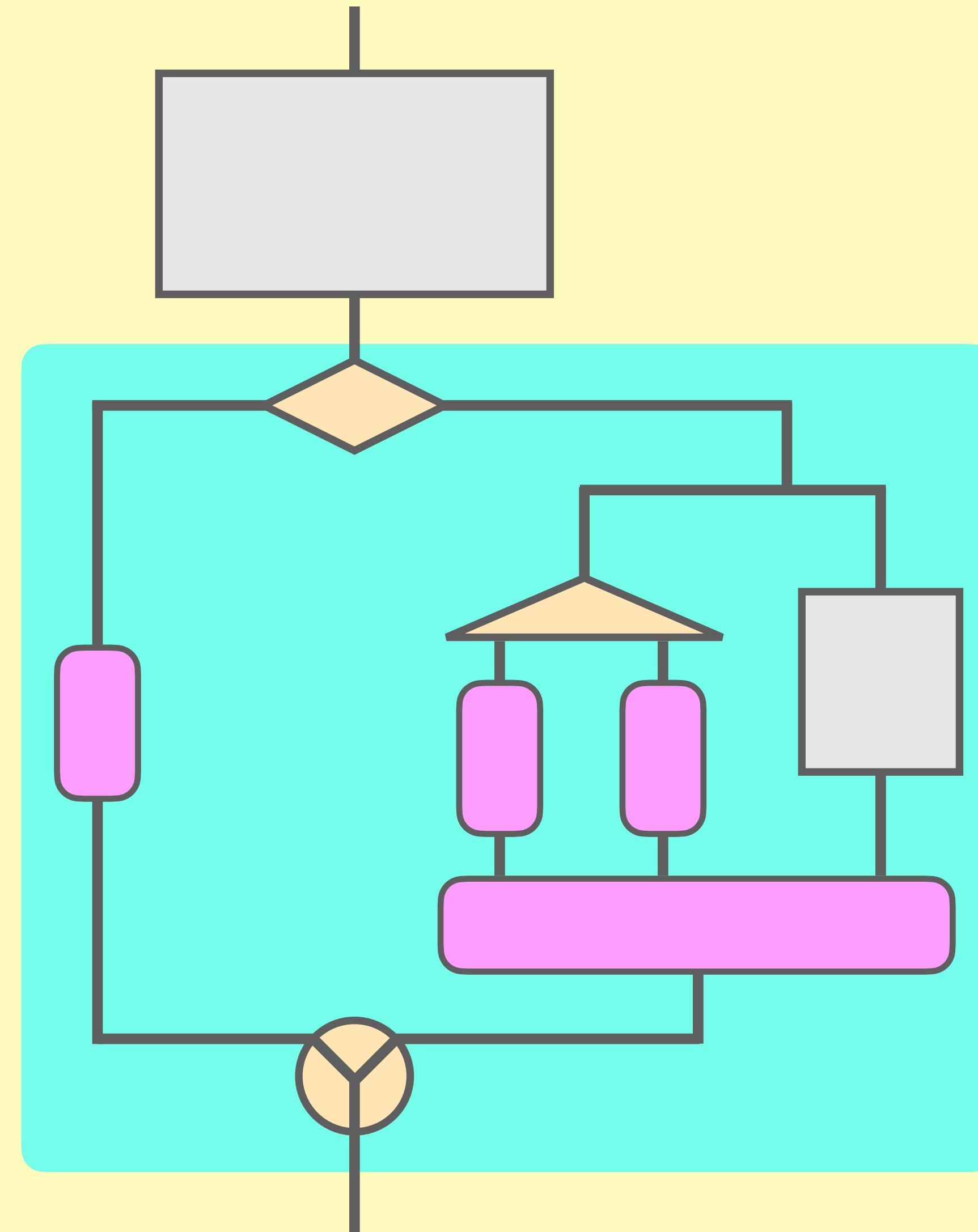
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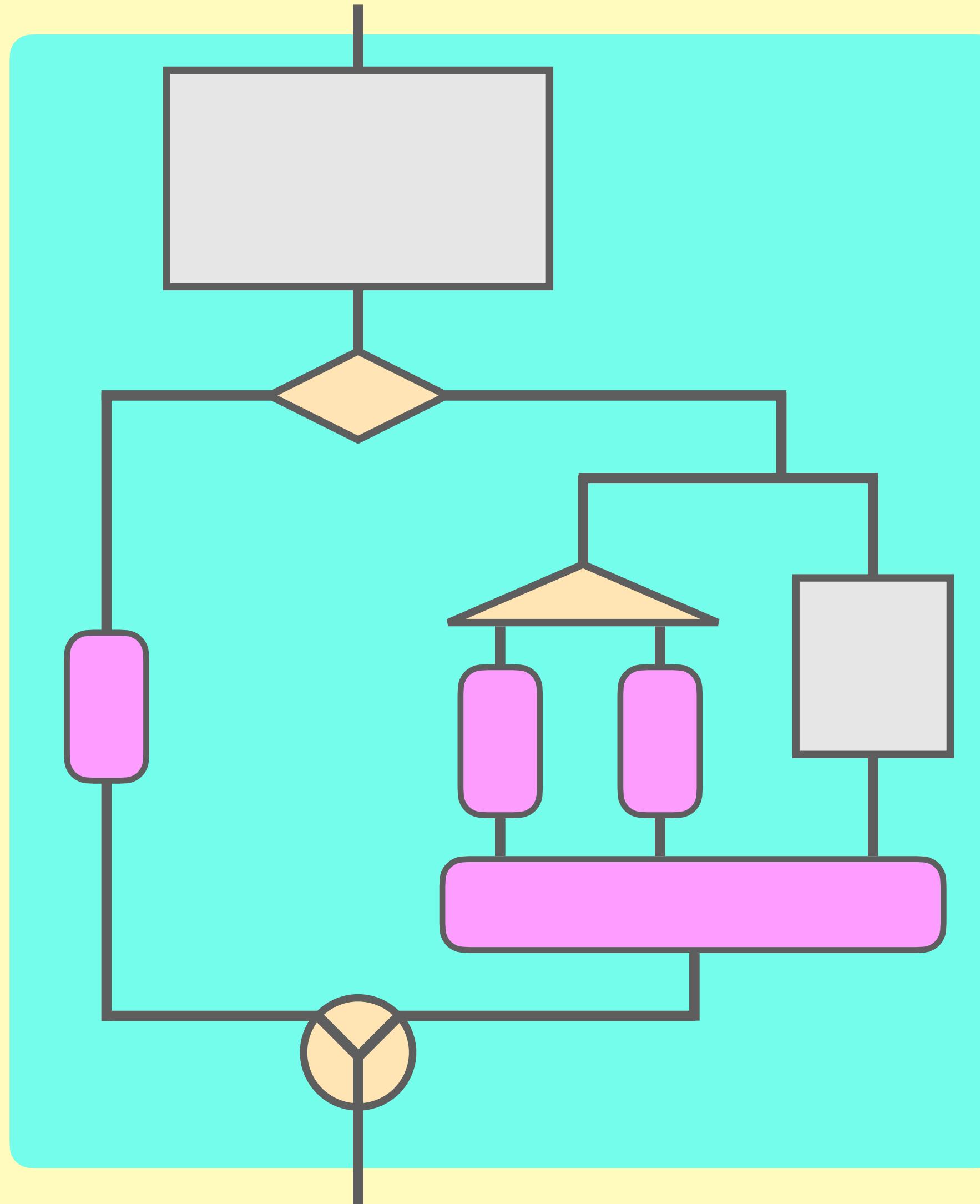
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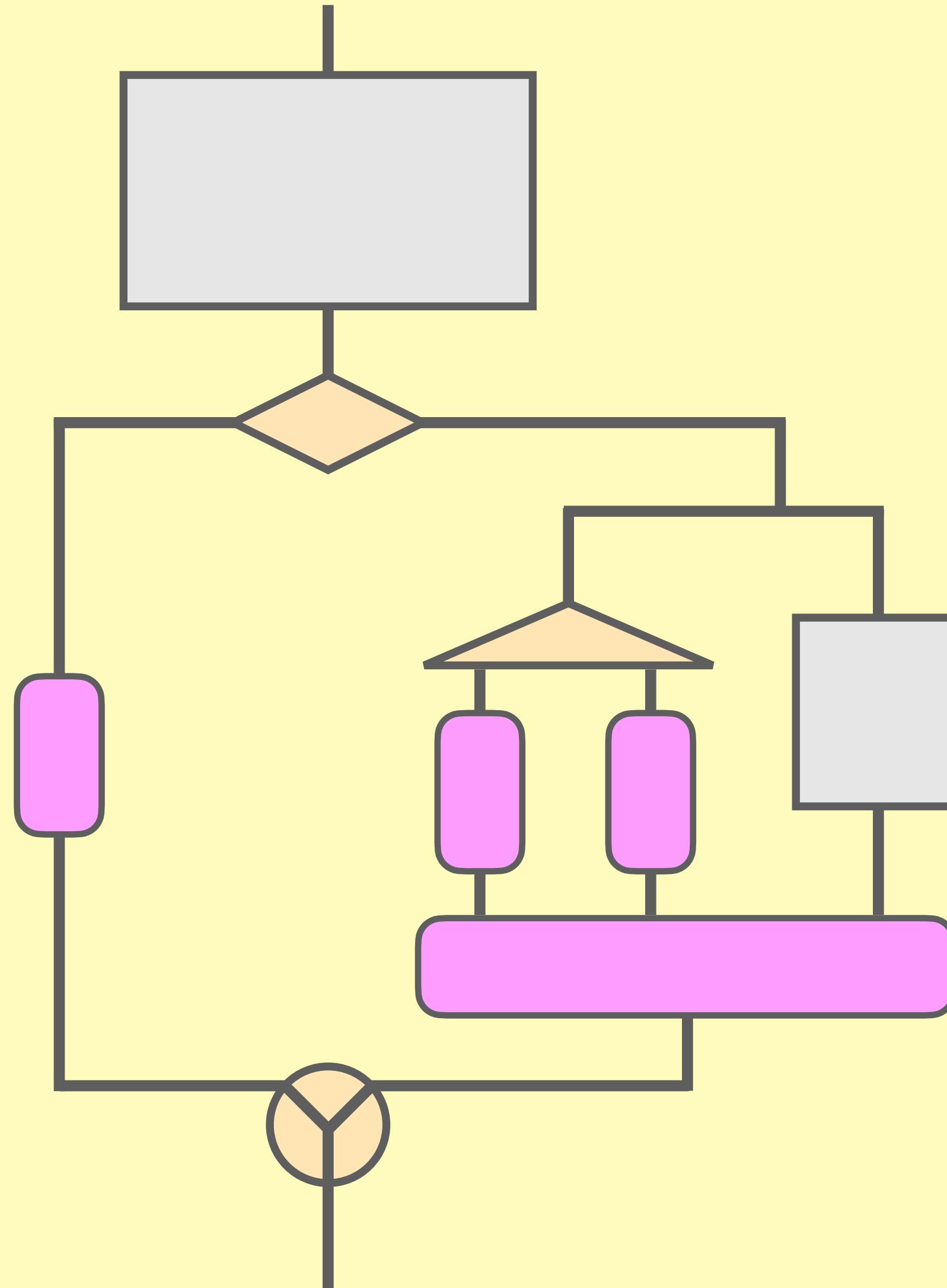
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        )))
```



Goal

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
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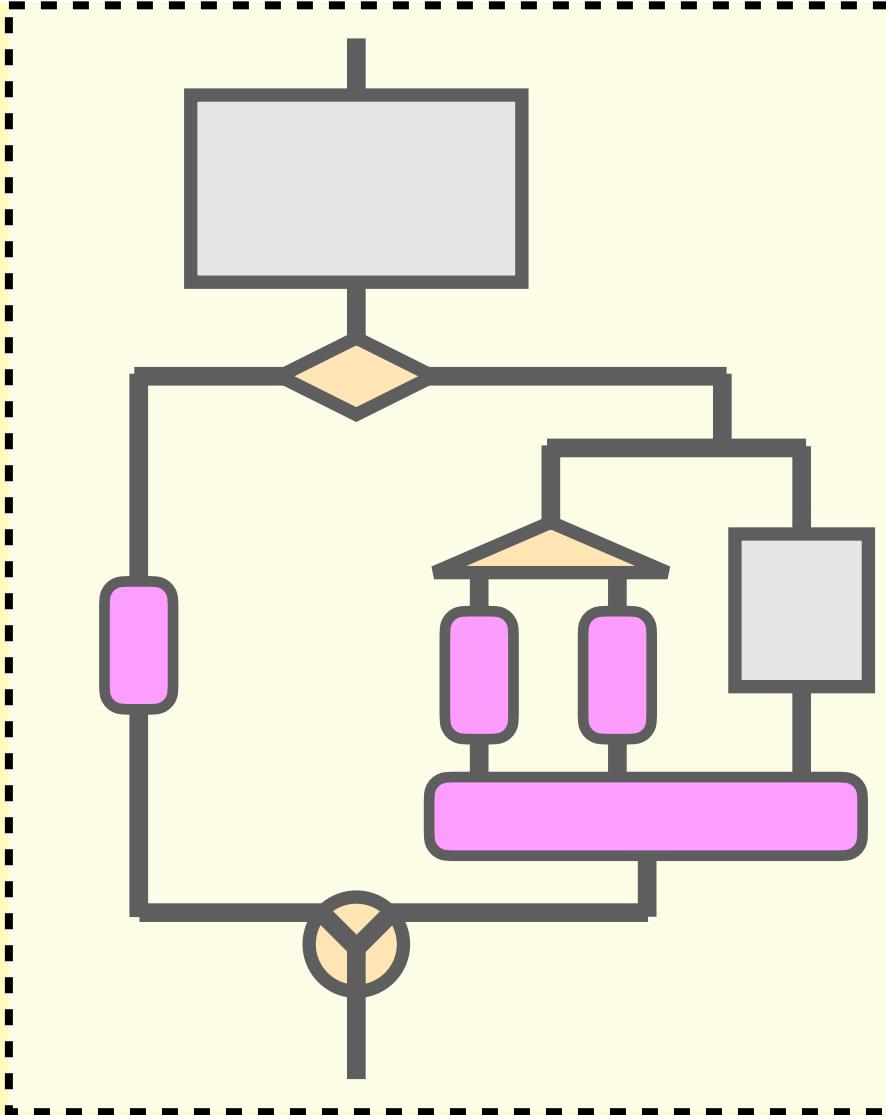


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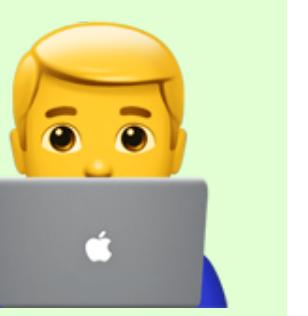


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```

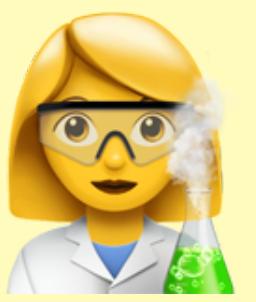
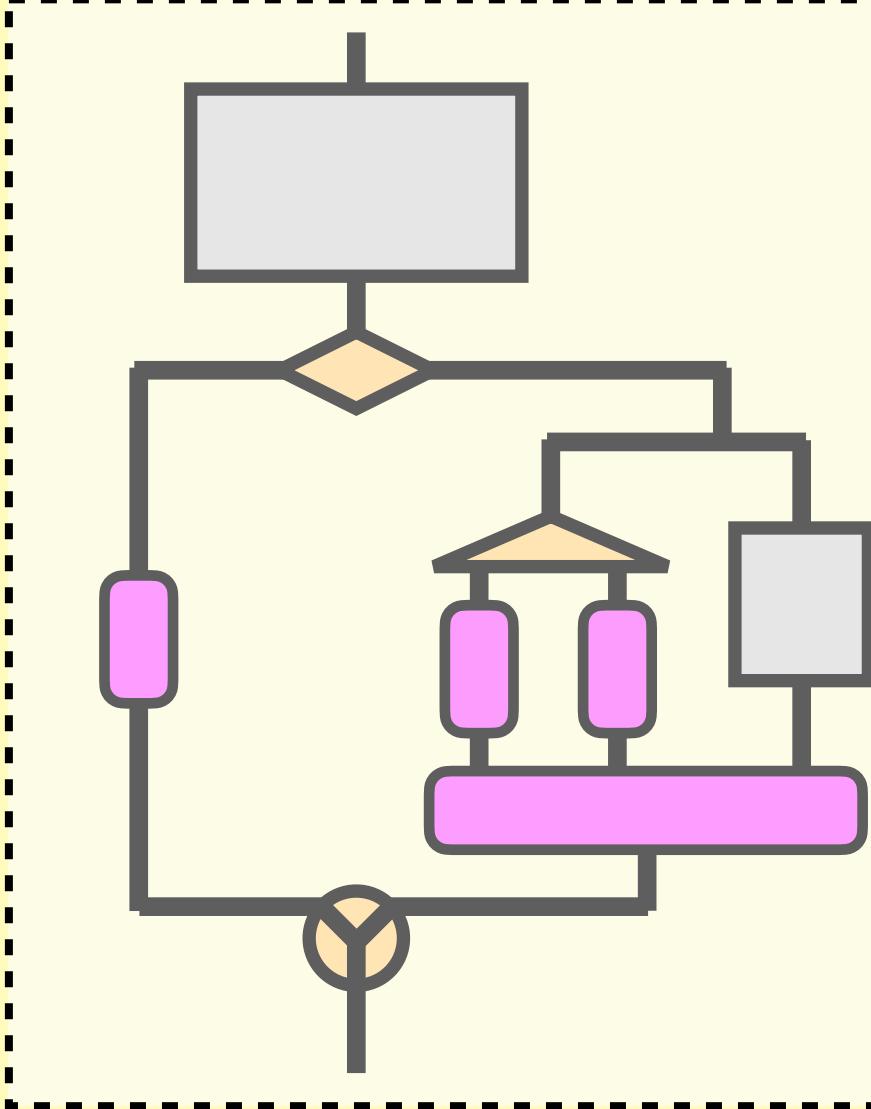


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```



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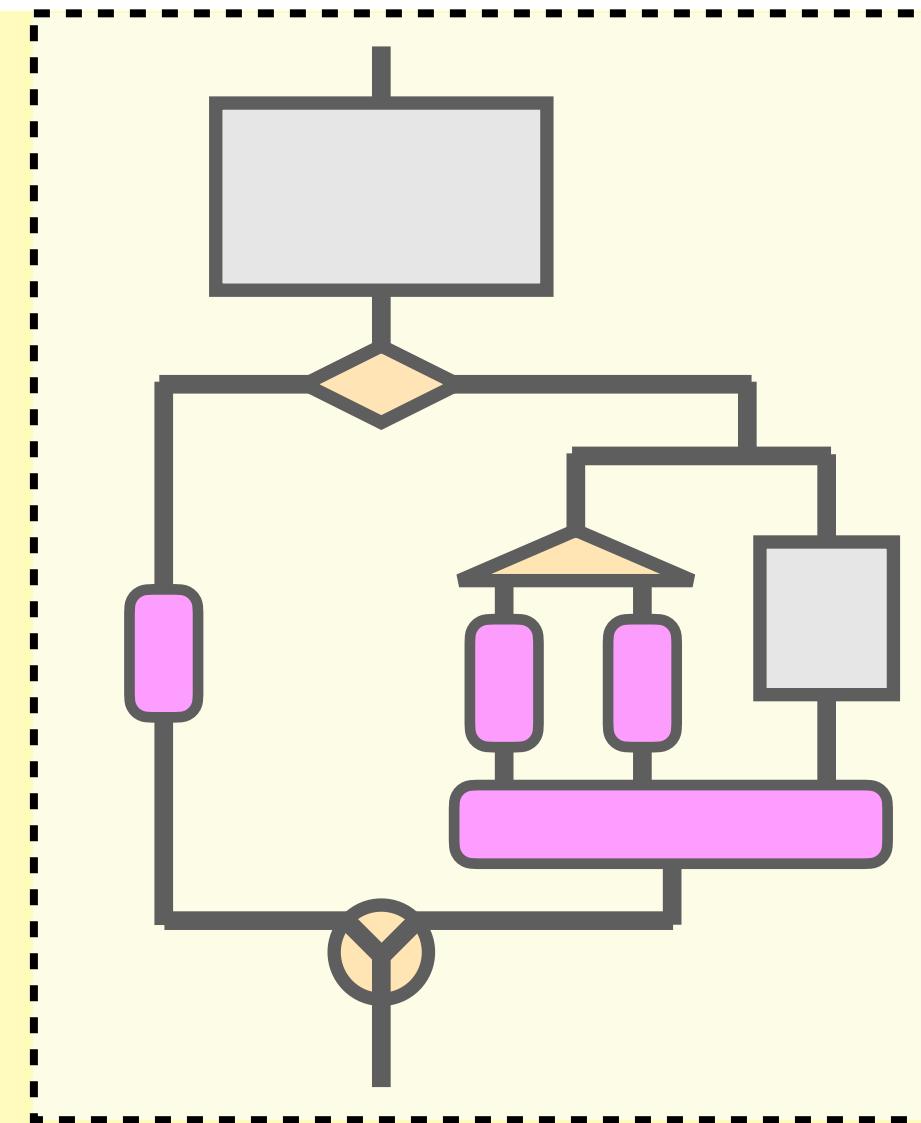


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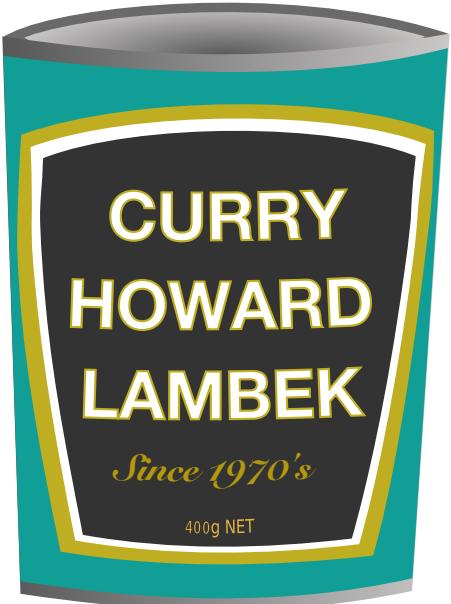
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        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            results  
        )))
```



```
case Right(id ** history) =>
  val crimi = checkCrimi(id)
  val civil = checkCivil(id)
  val verif = verify(history)
  results(crimi ** civil ** verif)
```

```
case      (id ** history) =>
  val crimi = checkCrimi(id)
  val civil = checkCivil(id)
  val verif = verify(history)
  results(crimi ** civil ** verif)
```

```
val onAccept: Expr[PersonalId ** EmploymentHistory] => Expr[Report] =  
  
  case (id ** history) =>  
    val crimi = checkCrimi(id)  
    val civil = checkCivil(id)  
    val verif = verify(history)  
    results(crimi ** civil ** verif)
```



```
val onAccept: Expr[PersonalId ** EmploymentHistory] => Expr[Report] =  
  
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  results(crimi ** civil ** verif)
```

```
def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B]
```

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  val crimi = checkCrimi(id)  
  val civil = checkCivil(id)  
  val verif = verify(history)  
  results(crimi ** civil ** verif)
```

```
delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]
```

```
def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
```

```
val onAccept: Expr[PersonalId ** EmploymentHistory] => Expr[Report] =  
  
case (id ** history) =>  
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```

```
delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]
```

```
def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =  
  val 🍅 : Expr[A] = freshVariable()
```

```
val onAccept: Expr[PersonalId ** EmploymentHistory] => Expr[Report] =  
  
  case (id ** history) =>  
    val crimi = checkCrimi(id)  
    val civil = checkCivil(id)  
    val verif = verify(history)  
    results(crimi ** civil ** verif)
```

```
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```

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def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =  
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val onAccept: Expr[PersonalId ** EmploymentHistory] => Expr[Report] =  
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```
delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]
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```
f := onAccept  
🍅 : Expr[PersonalId ** EmploymentHistory]
```

```
val onAccept: Expr[PersonalId ** EmploymentHistory] =  
  case _ (id ** history) =>  
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f := onAccept  
🍅 : Expr[PersonalId ** EmploymentHistory]
```

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val onAccept: Expr[PersonalId ** EmploymentHistory] =  
  case (id ** history) =>  
    val crimi = checkCrimi(id)  
    val civil = checkCivil(id)  
    val verif = verify(history)  
    results(crimi ** civil ** verif)
```

```
expr : Expr[Report] =
```

```
delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]
```

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)

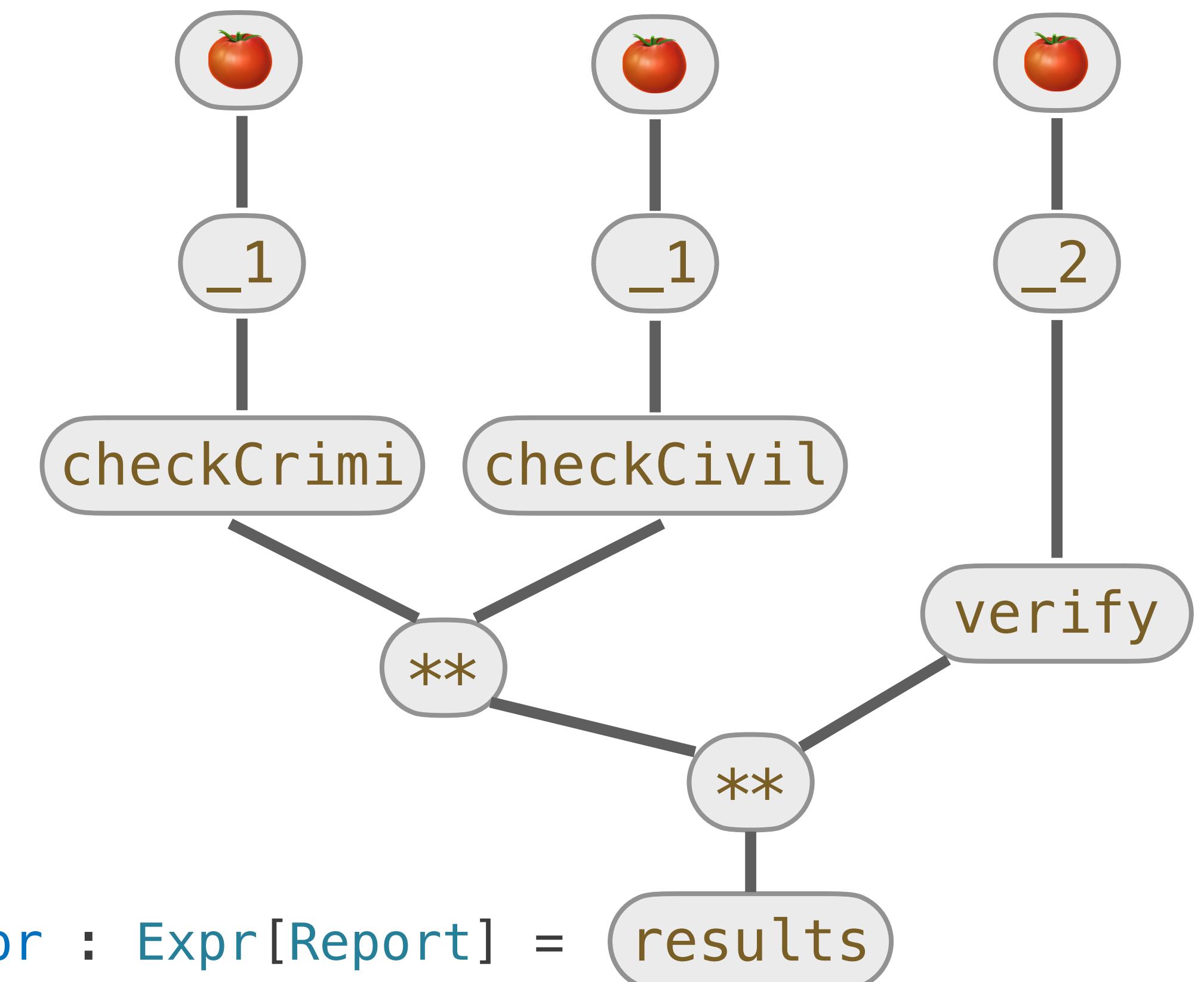
```

```

val onAccept: Expr[PersonalId ** EmploymentHistory] =
  case (id ** history) =>
    val crimi = checkCrimi(id)
    val civil = checkCivil(id)
    val verif = verify(history)
    results(crimi ** civil ** verif)

```

$f := \text{onAccept}$
 $\bullet : \text{Expr[PersonalId} ** \text{EmploymentHistory]}$



`delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]`

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  Lam(🍅, expr)

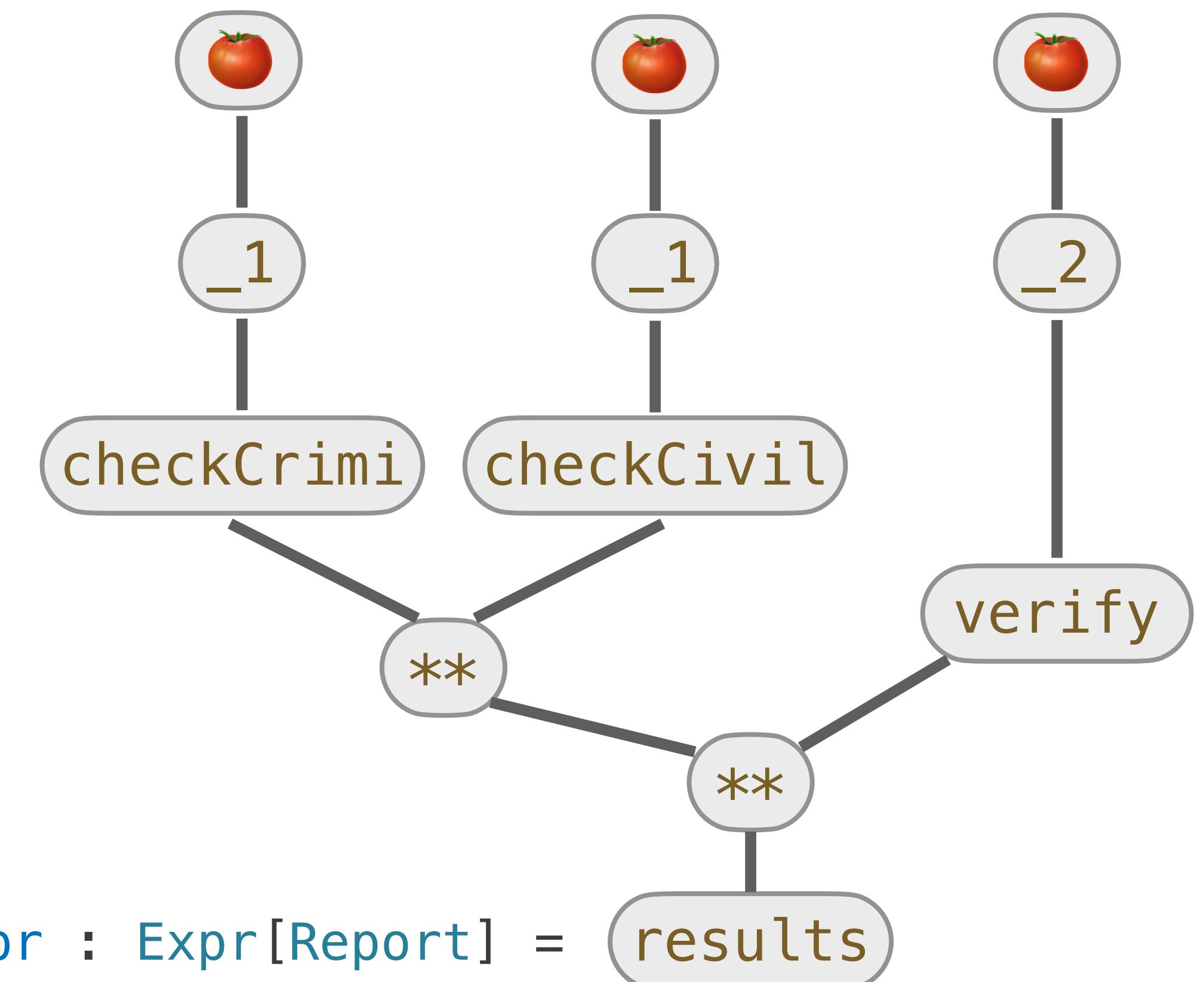
```

```

val onAccept: Expr[PersonalId ** EmploymentHistory] =
  case (id ** history) =>
    val crimi = checkCrimi(id)
    val civil = checkCivil(id)
    val verif = verify(history)
    results(crimi ** civil ** verif)

```

$f := \text{onAccept}$
 $\bullet : \text{Expr[PersonalId} ** \text{EmploymentHistory]}$



`delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]`

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  Lam(🍅 × expr)

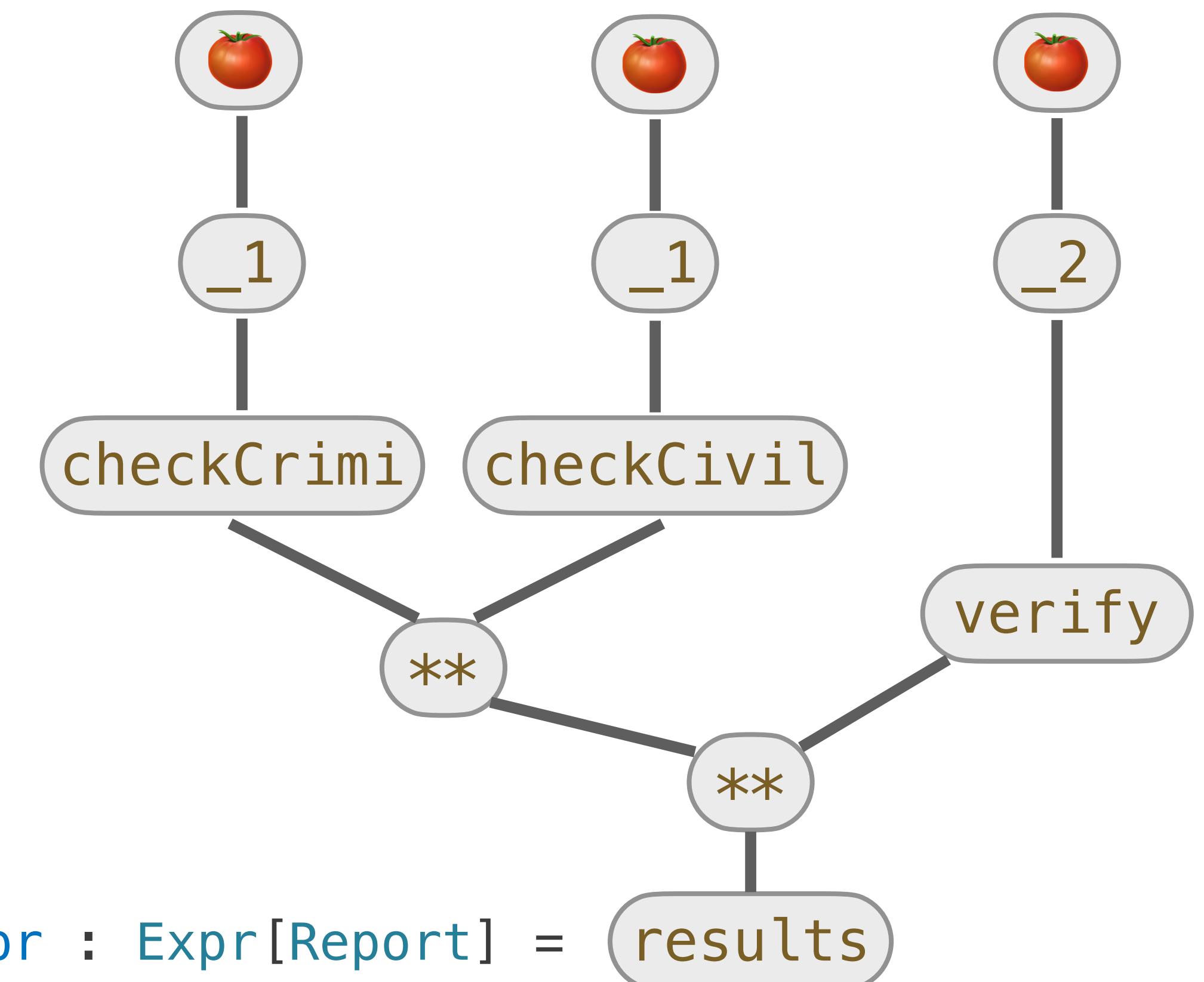
```

```

val onAccept: Expr[PersonalId ** EmploymentHistory] =
  case (id ** history) =>
    val crimi = checkCrimi(id)
    val civil = checkCivil(id)
    val verif = verify(history)
    results(crimi ** civil ** verif)

```

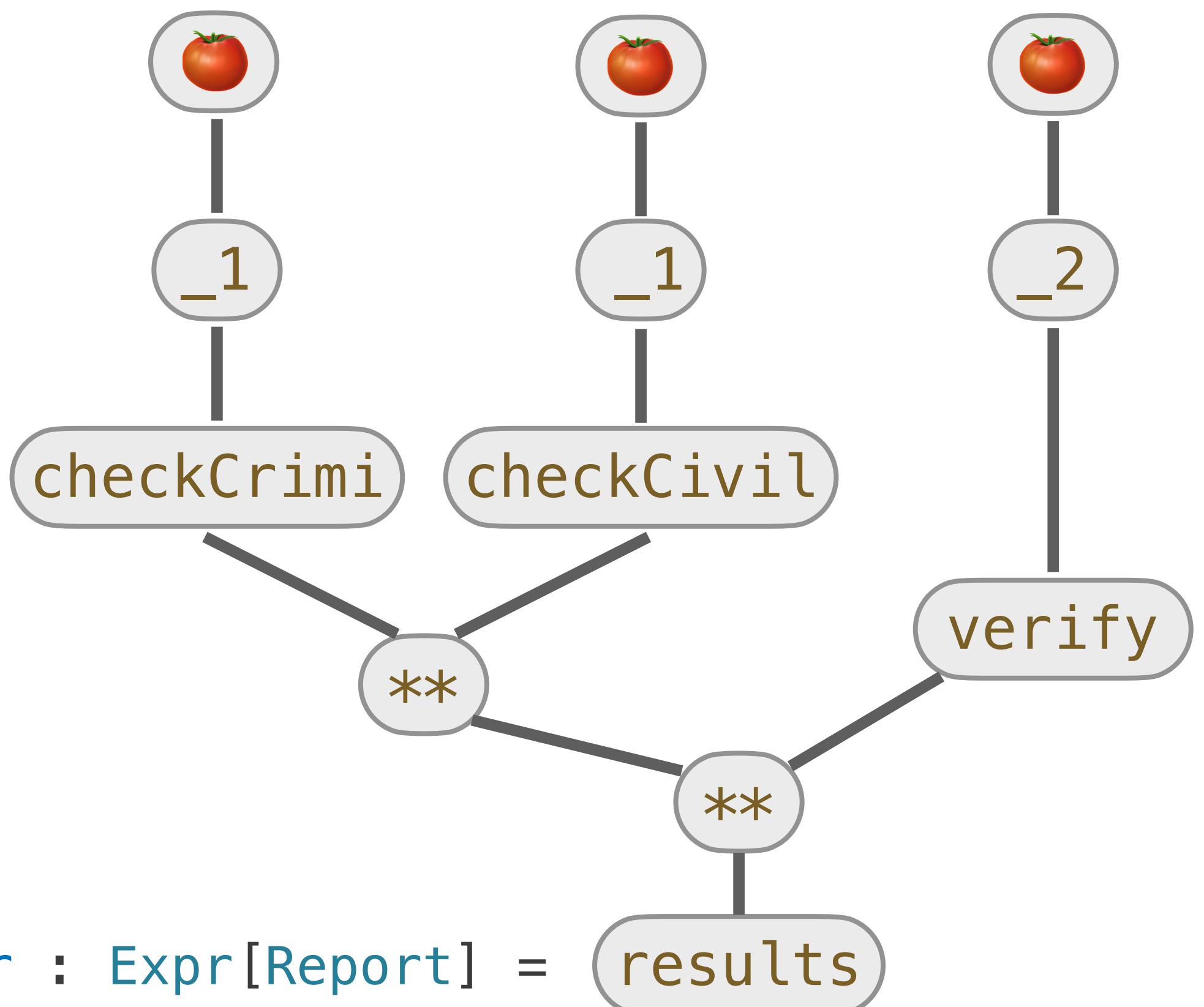
$f := \text{onAccept}$
 $\bullet : \text{Expr[PersonalId} ** \text{EmploymentHistory]}$



`delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]`

```
def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =  
  val 🍅 : Expr[A] = freshVariable  
  val expr : Expr[B] = f(🍅)  
  f := onAccept  
  🍅 : Expr[PersonalId *]
```

```
f := onAccept  
    : Expr[PersonalId ** EmploymentHistory]
```



```
al onAccept: Expr[PersonalId ** Employment]
case      (id ** history) =>
val crimi = checkCrimi(id)
val civil = checkCivil(id)
val verif = verify(history)
results(crimi ** civil ** verif)
```

```
delamdbify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]
```

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

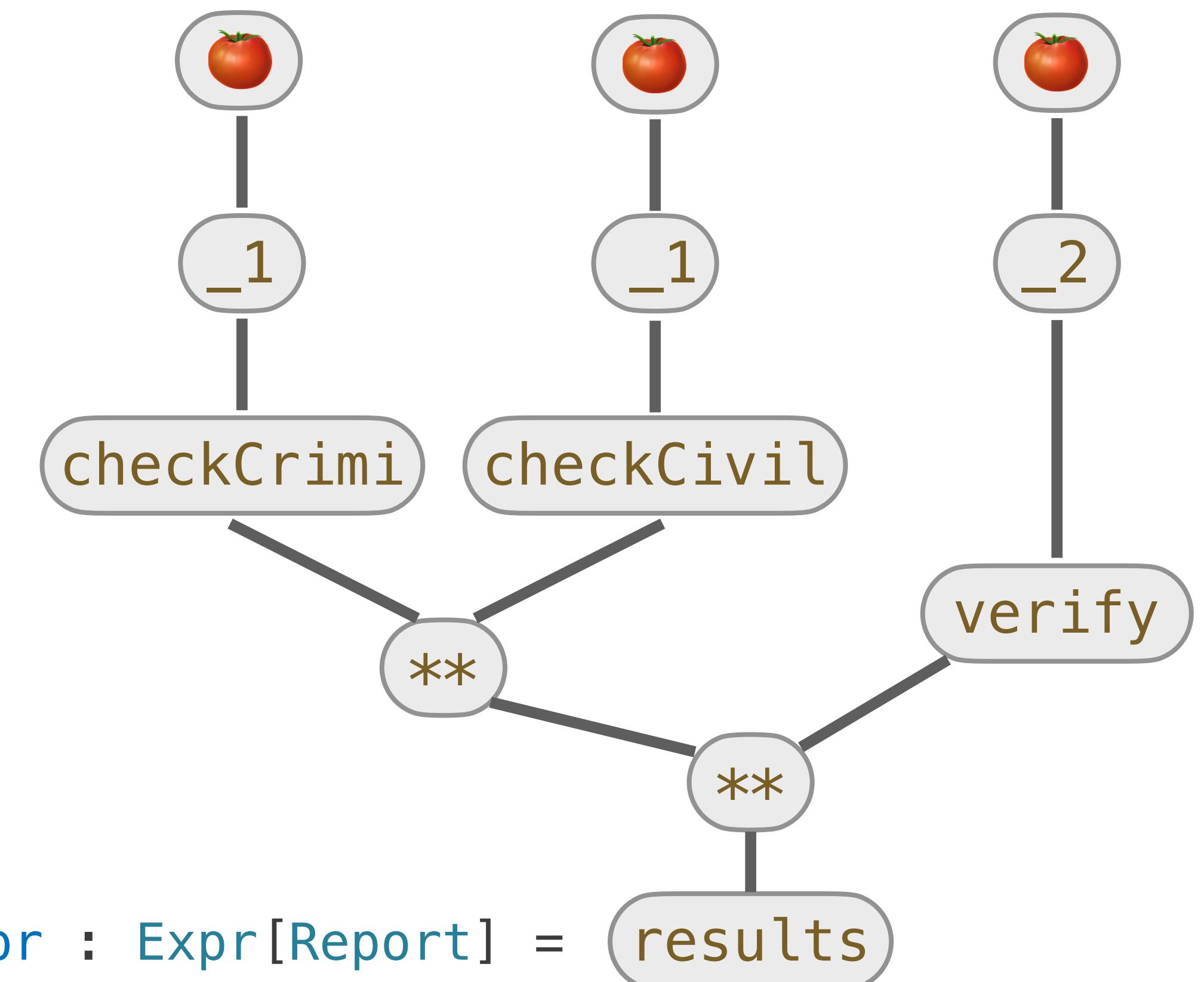
```

```

val onAccept: Expr[PersonalId ** EmploymentHistory] =
  case (id ** history) =>
    val crimi = checkCrimi(id)
    val civil = checkCivil(id)
    val verif = verify(history)
    results(crimi ** civil ** verif)

```

$f := \text{onAccept}$
 $\bullet : \text{Expr[PersonalId} ** \text{EmploymentHistory]}$



delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

```

```

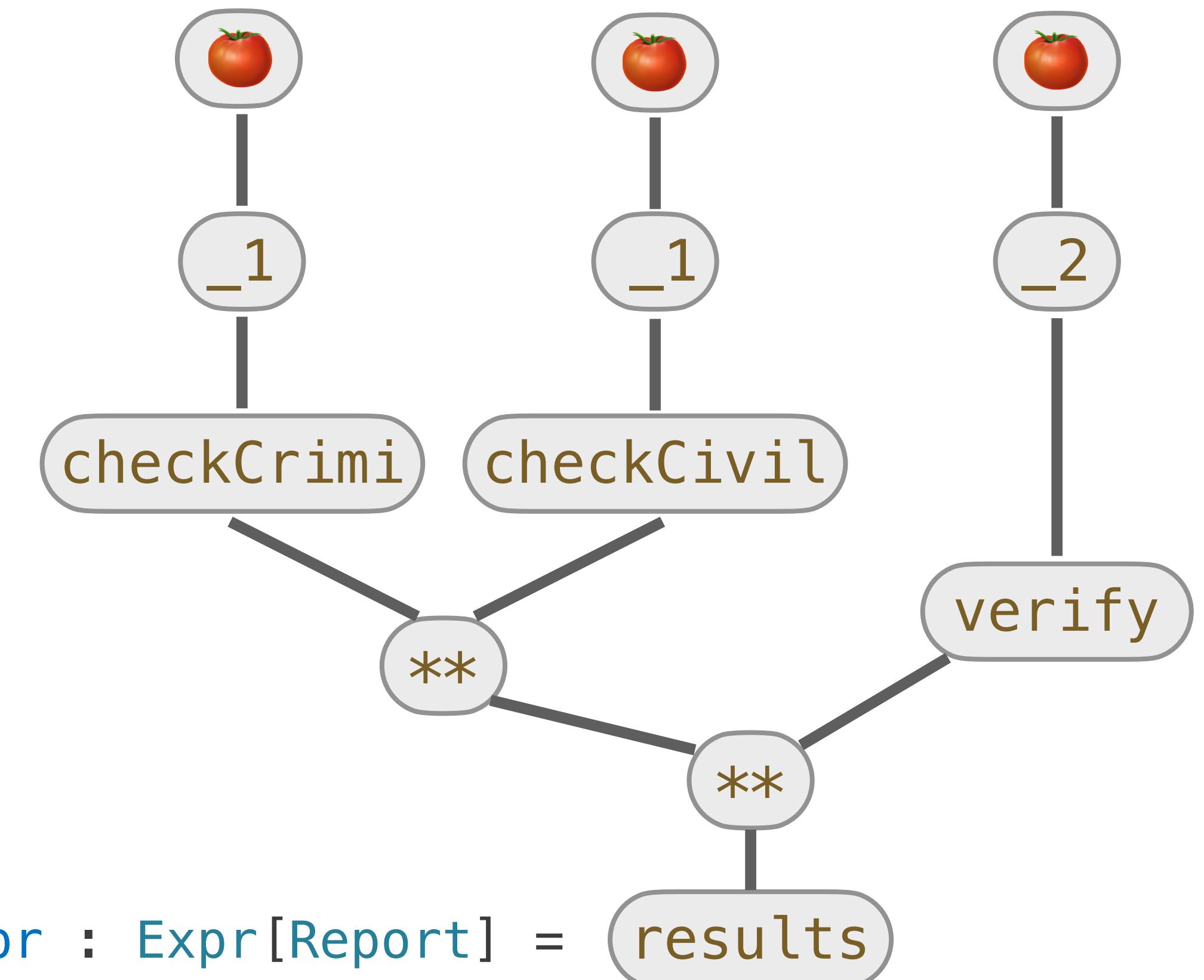
val onAccept: PersonalId => EmploymentHistory = ...
case object EmploymentHistory {
  val checkCriminal: PersonalId => EmploymentHistory = ...
  val checkCivil: PersonalId => EmploymentHistory = ...
  val verify: EmploymentHistory => PersonalId = ...
}
val results: EmploymentHistory = ...
results.onAccept(PersonalId("1"))

```

```

f := onAccept
🍅 : Expr[PersonalId ** EmploymentHistory]

```



delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

```

```

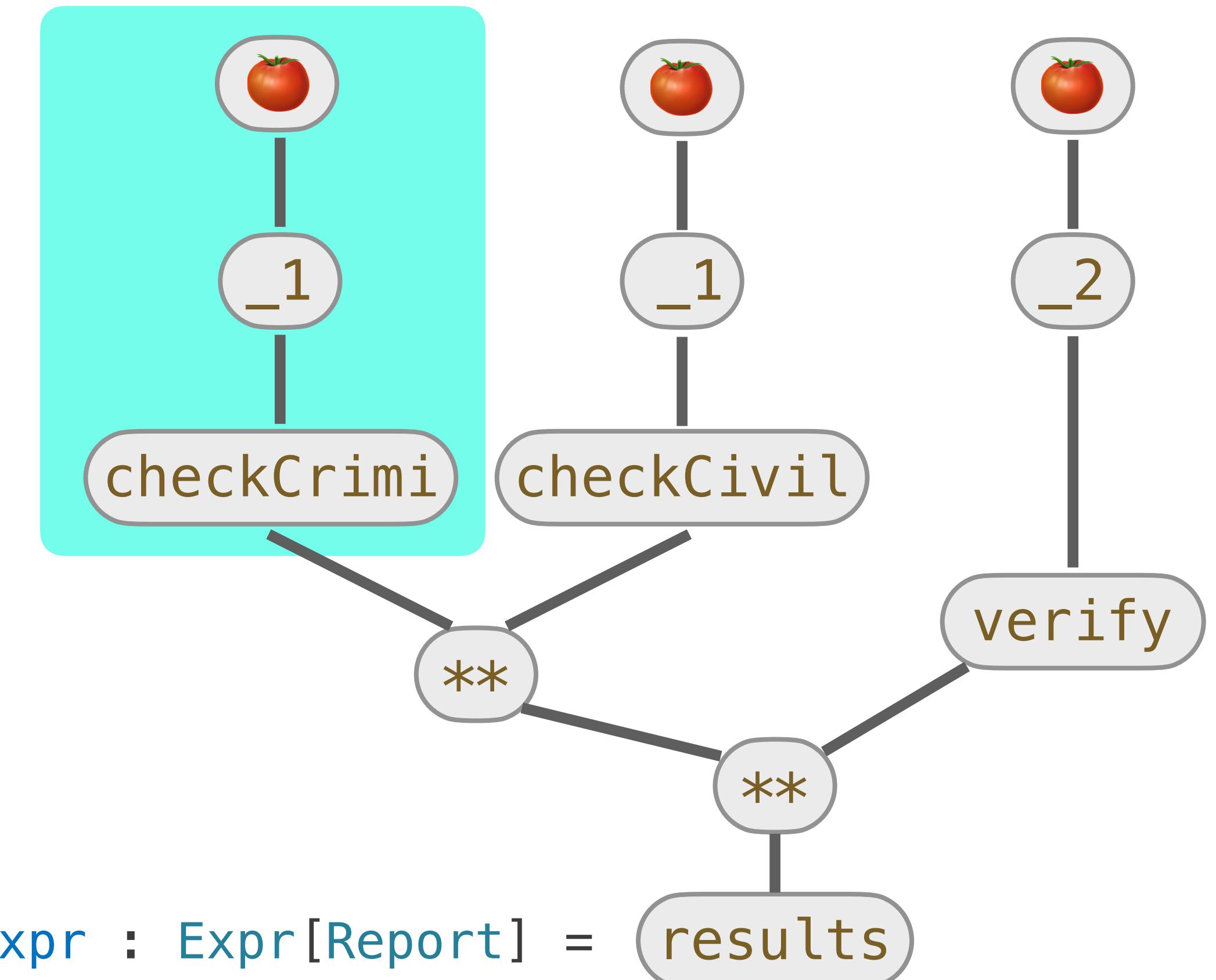
val onAccept: PersonalId ** EmploymentHistory => Flow[Expr[A], Expr[B]] = {
  case _1 >>> checkCrimi
  val _1 = checkCrimi
  val _2 = checkCivil
  val _3 = verify
  results
}

```

```

f := onAccept
🍅 : Expr[PersonalId ** EmploymentHistory]

```



delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

```

```

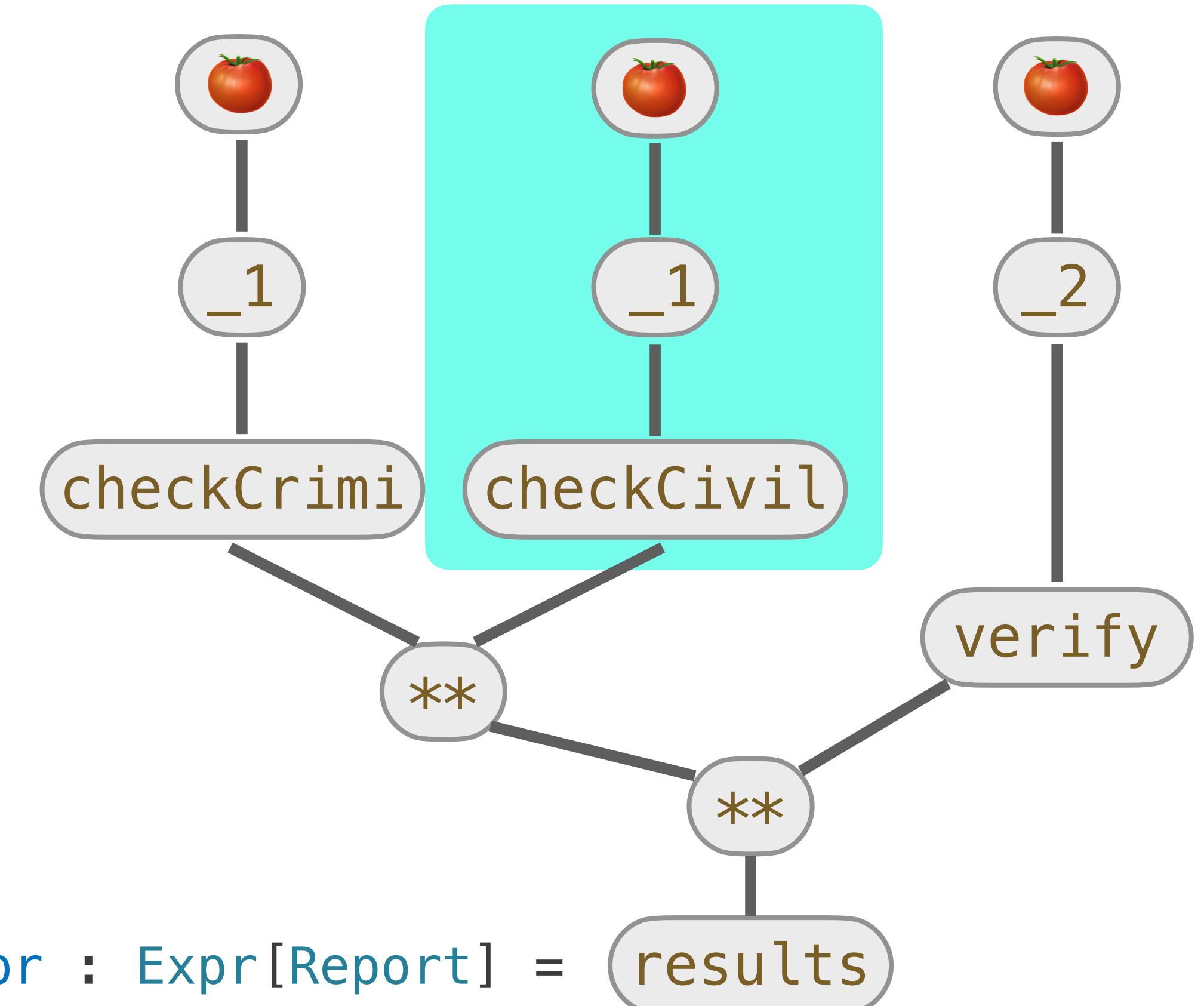
val onAccept: PersonalId => EmploymentHistory = {
  case _1 >>> checkCriminal
  case _1 >>> checkCivil
  val results = checkCriminal :: checkCivil :: Nil
  val report = Report(results)
  results
}

```

```

f := onAccept
🍅 : Expr[PersonalId ** EmploymentHistory]

```



delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

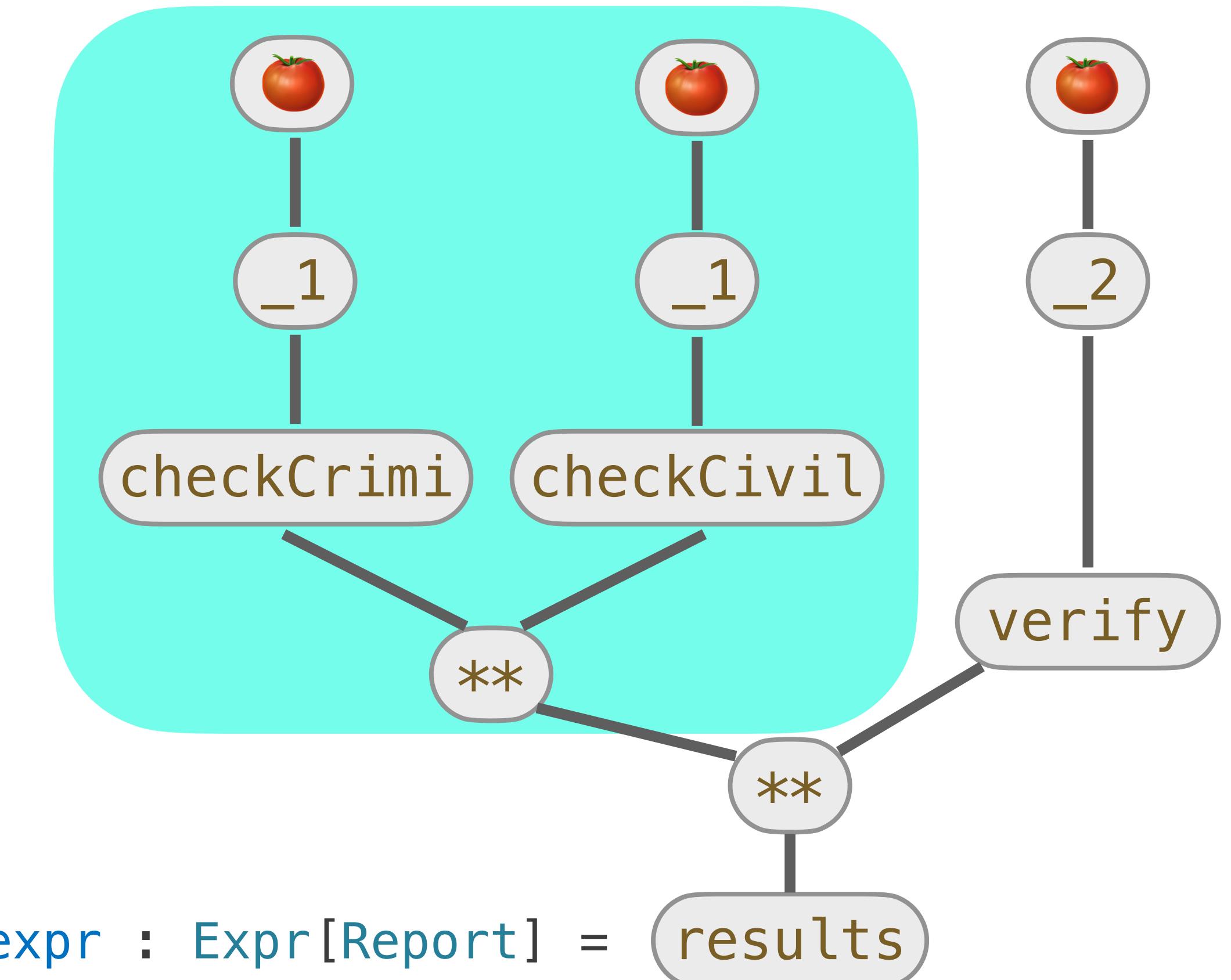
```

```

val onAccept: Dup() => Par(
  case _1 =>>> checkCrimi,
  case _1 =>>> checkCivil
)
val expr: Expr[Report] = results
val verify: Expr[Report] = results

```

$f := \text{onAccept}$
 $\bullet : \text{Expr[PersonalId} ** \text{EmploymentHistory]}$



$\text{delambdify(onAccept)} : \text{Flow[PersonalId} ** \text{EmploymentHistory}, \text{Report}]$

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

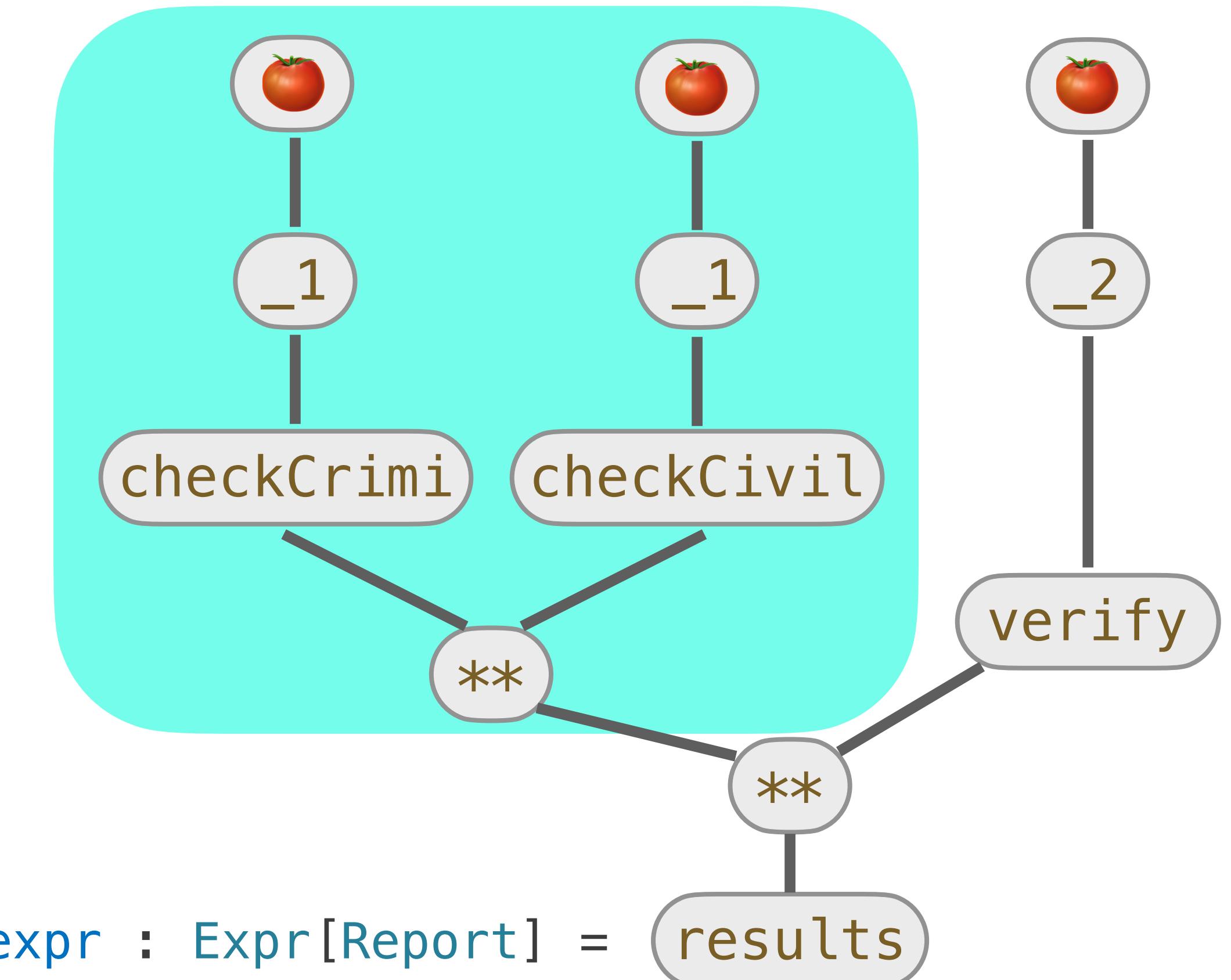
```

```

val onAccept: Dup() =>>> Par(
  case _1 =>>> checkCrimi,
  case _1 =>>> checkCivil
)
val verify: EmploymentHistory => Report
val results: EmploymentHistory => Report
val expr: Expr[Report] = results(f)

```

$f := \text{onAccept}$
 $\bullet : \text{Expr[PersonalId} ** \text{EmploymentHistory]}$



$\text{delambdify(onAccept)} : \text{Flow[PersonalId} ** \text{EmploymentHistory}, \text{Report}]$

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

```

```

val onAccept: Par[Expr[Report]] = Par(
  _1 >>> Dup() >>> Par(
    checkCrimi,
    checkCivil
  )
)

```

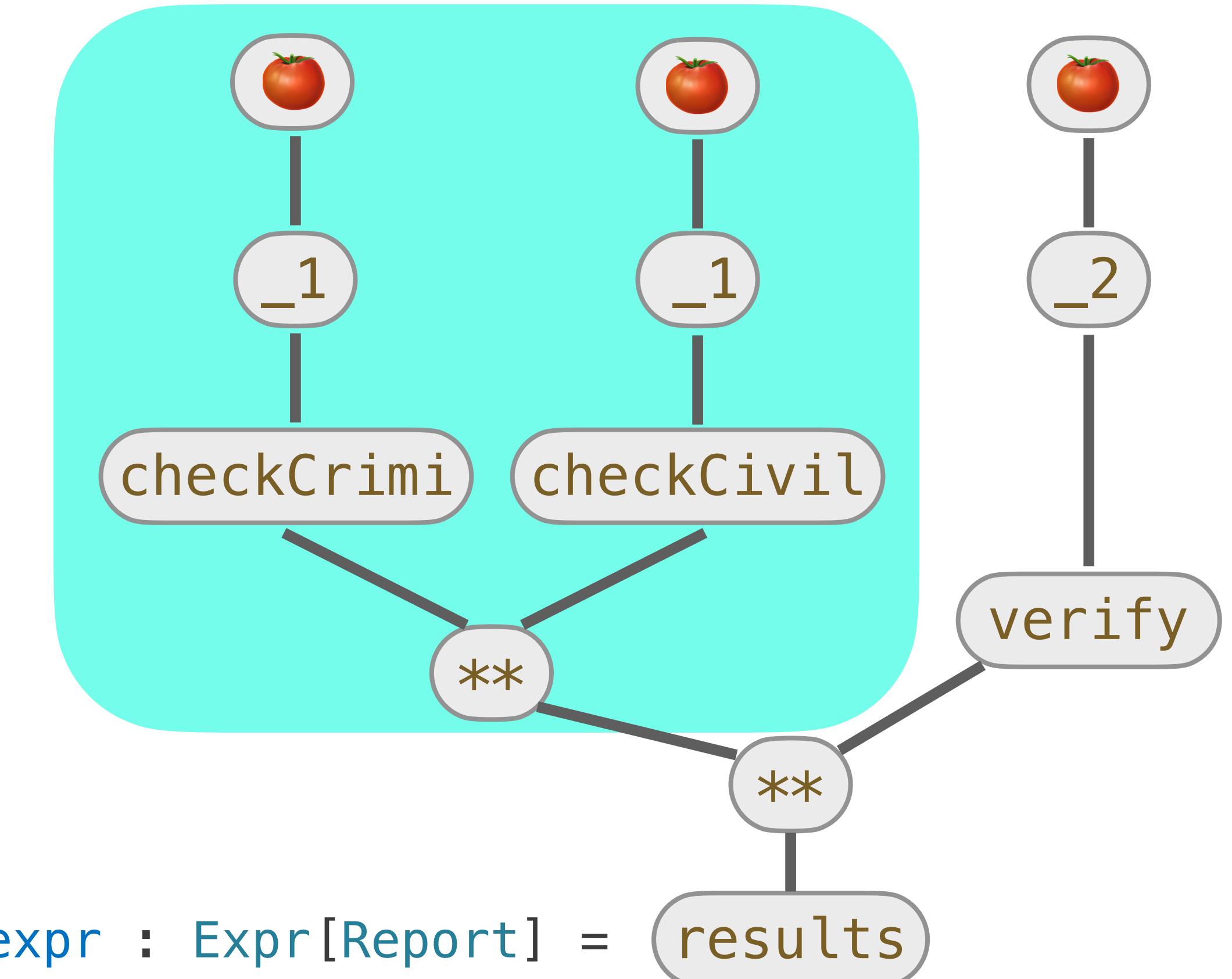
EmploymentHistory

delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]

```

f := onAccept
🍅 : Expr[PersonalId ** EmploymentHistory]

```



```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

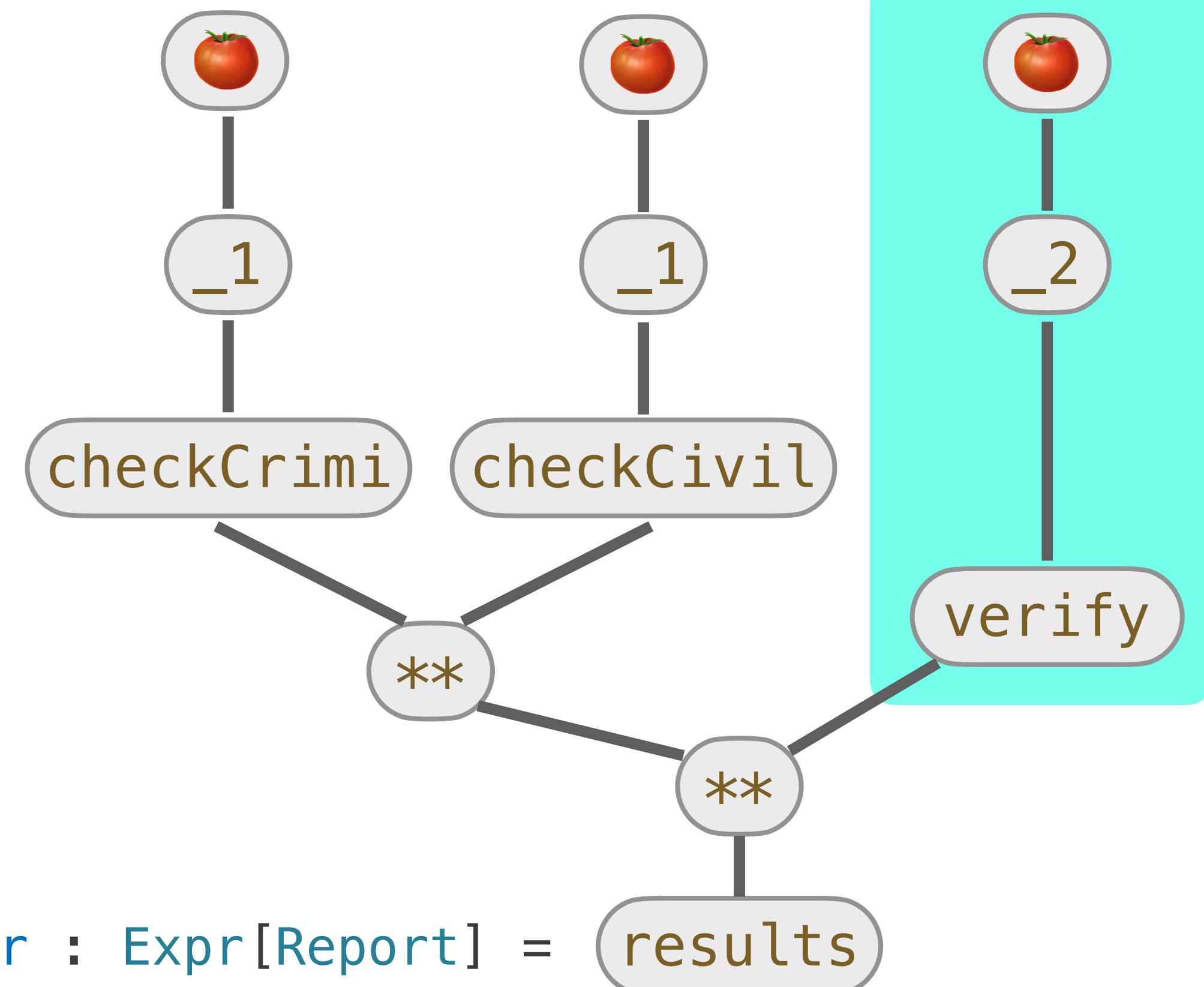
```

```

val onAccept: Par[Expr[PersonalId]] = Par(
  _1 >>> Dup() >>> Par(
    checkCrimi,
    checkCivil
  )
  val _1 = _1
  val _2 = _2
  results = _2 >>> verify
)

```

$f := \text{onAccept}$
 $\bullet : \text{Expr[PersonalId} ** \text{EmploymentHistory]}$



delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

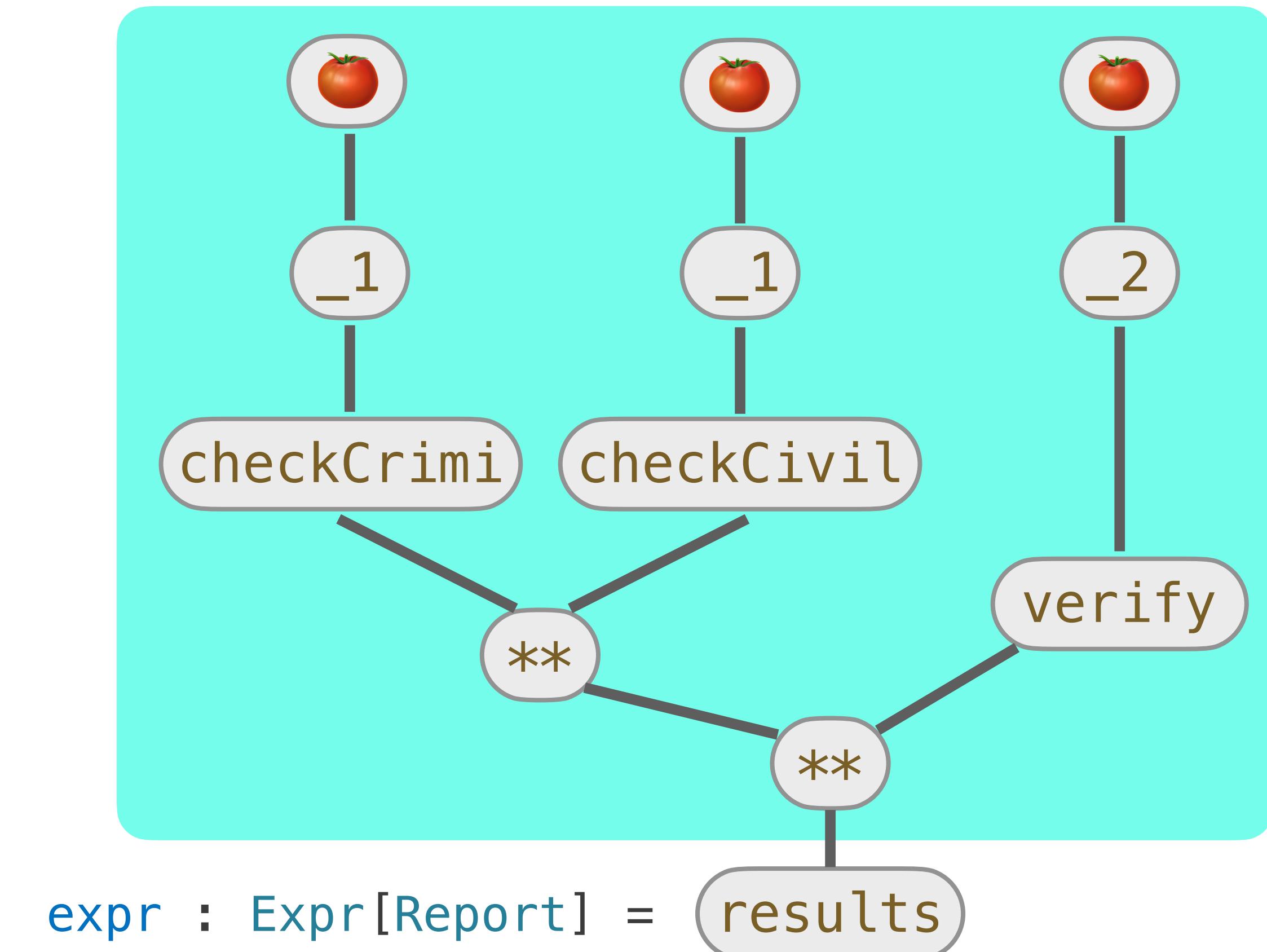
```

```

val onAccept: Dup() >>> Par(
  _1 >>> Dup() >>> Par(
    checkCrimi,
    checkCivil
  ),
  _2 >>> verify
) >>> f

```

$f := \text{onAccept}$
 $\bullet : \text{Expr[PersonalId} ** \text{EmploymentHistory]}$



`delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]`

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

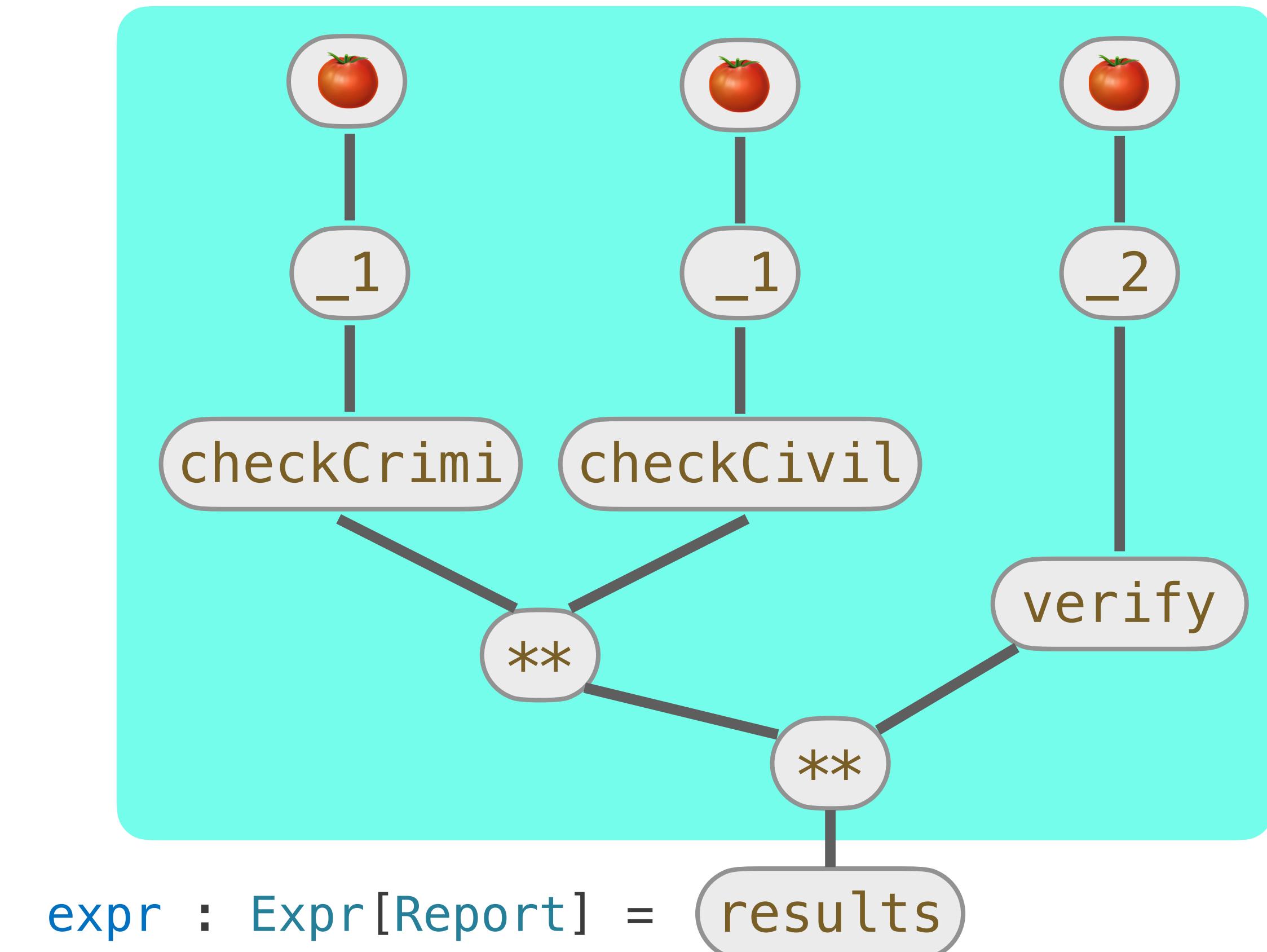
```

```

val onAccept: Dup() >>> Par(
  _1 >>> Dup() >>> Par(
    checkCrimi,
    checkCivil
  ),
  _2 >>> verify
)
val expr: Expr[Report] = results(f)

```

`f := onAccept`
`🍅 : Expr[PersonalId ** EmploymentHistory]`



`delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]`

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

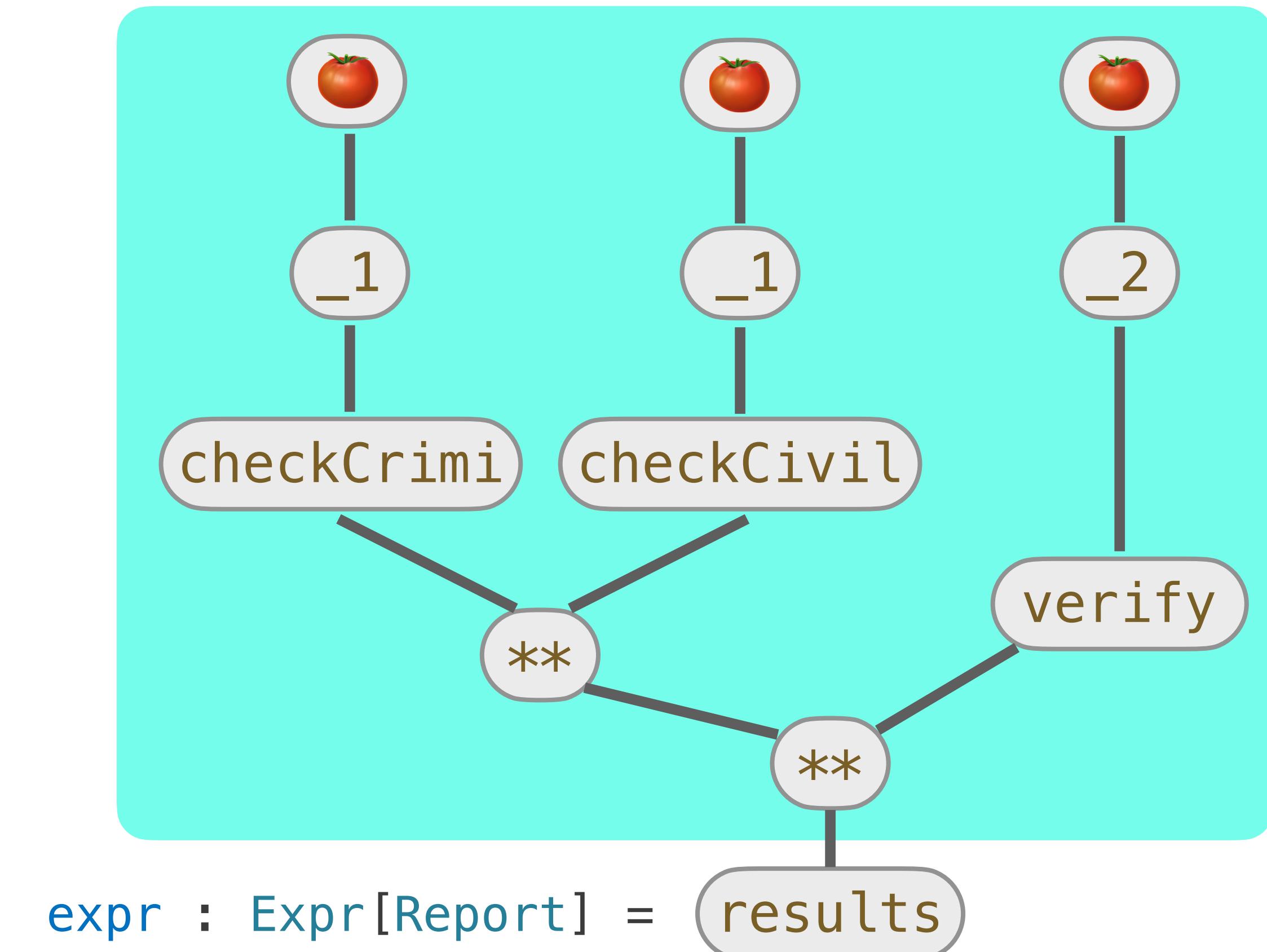
```

```

val onAccept: Par[Expr[Report]] = Par(
  Dup() >>> Par(
    checkCrimi,
    checkCivil
  ),
  verify
)
val expr: Expr[Report] = onAccept(f)
val results: Expr[Report] = expr

```

$f := \text{onAccept}$
 $\bullet : \text{Expr[PersonalId} ** \text{EmploymentHistory]}$



`delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]`

```

def delambdify[A, B](f: Expr[A] => Expr[B]): Flow[A, B] =
  val 🍅 : Expr[A] = freshVariable
  val expr : Expr[B] = f(🍅)
  eliminate(🍅, from = expr)

```

```

val onAccept: Par(
  Dup() >>> Par(
    checkCrimi,
    checkCivil
  ),
  verify
) >>> results

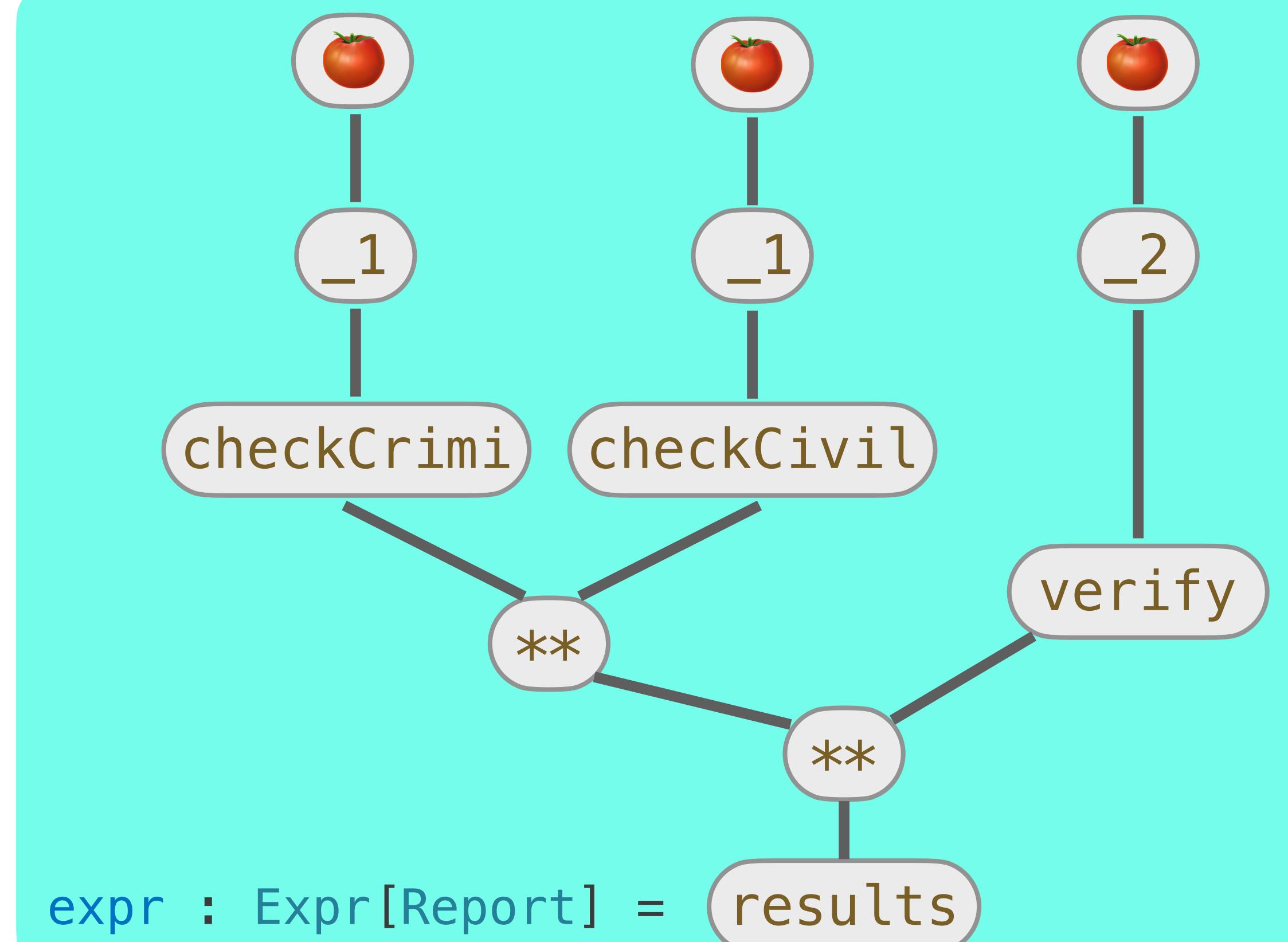
```

EmploymentHistory

```

f := onAccept
🍅 : Expr[PersonalId ** EmploymentHistory]

```



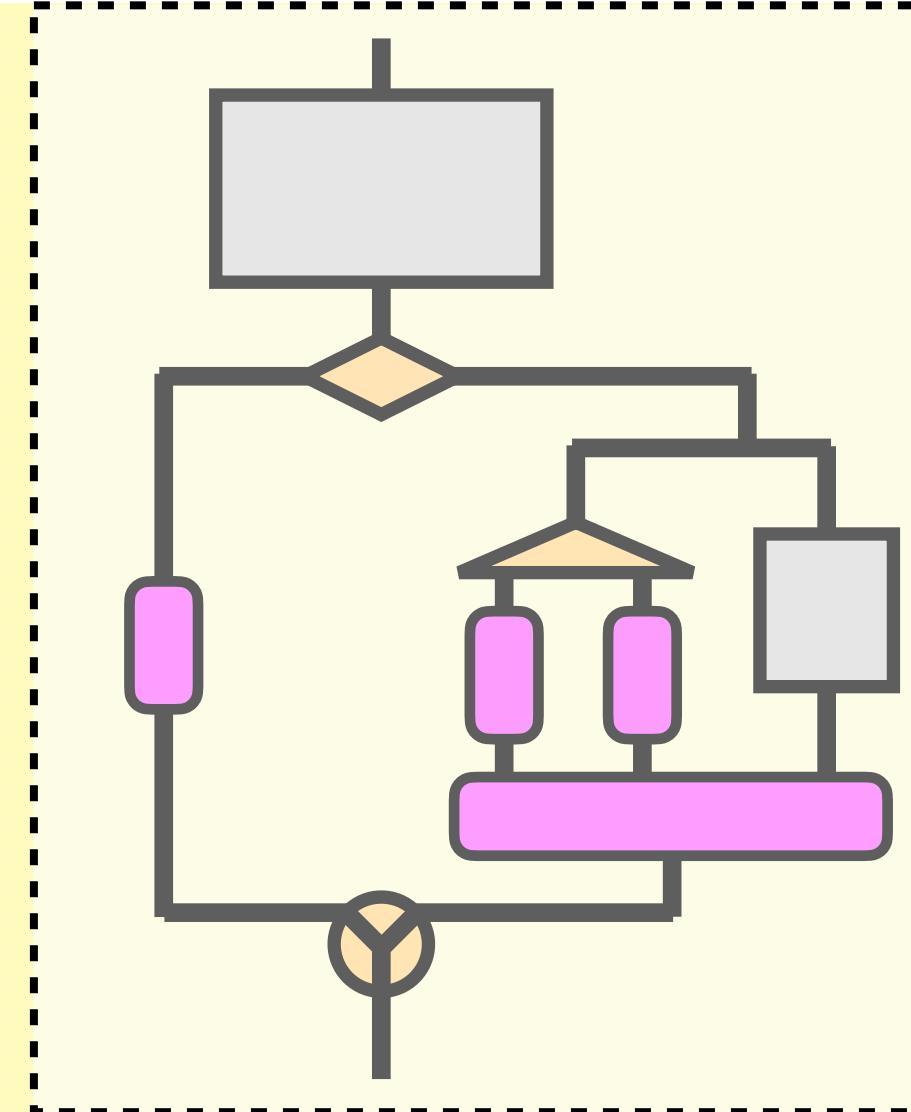
delambdify(onAccept): Flow[PersonalId ** EmploymentHistory, Report]

... delambdified so far ...

```
Flow { candidate =>  
  askForAccept(candidate) switch {  
    case Left(x) =>  
      declined(x)  
    case Right(id ** history) =>  
      val crimi = checkCrimi(id)  
      val civil = checkCivil(id)  
      val verif = verify(history)  
      results(crimi ** civil ** verif)  
  }  
}
```

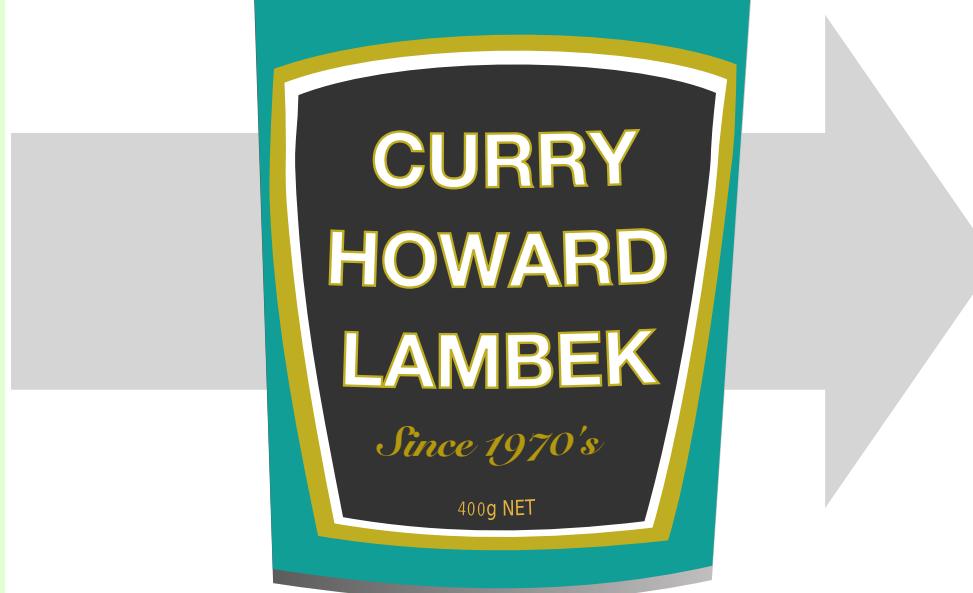


```
AndThen(  
  askForAccept,  
  Switch(  
    declined,  
    AndThen(  
      Par(  
        AndThen(  
          Dup(),  
          Par(checkCrimi, checkCivil)  
        ),  
        verify  
      ),  
      results  
    )) )
```

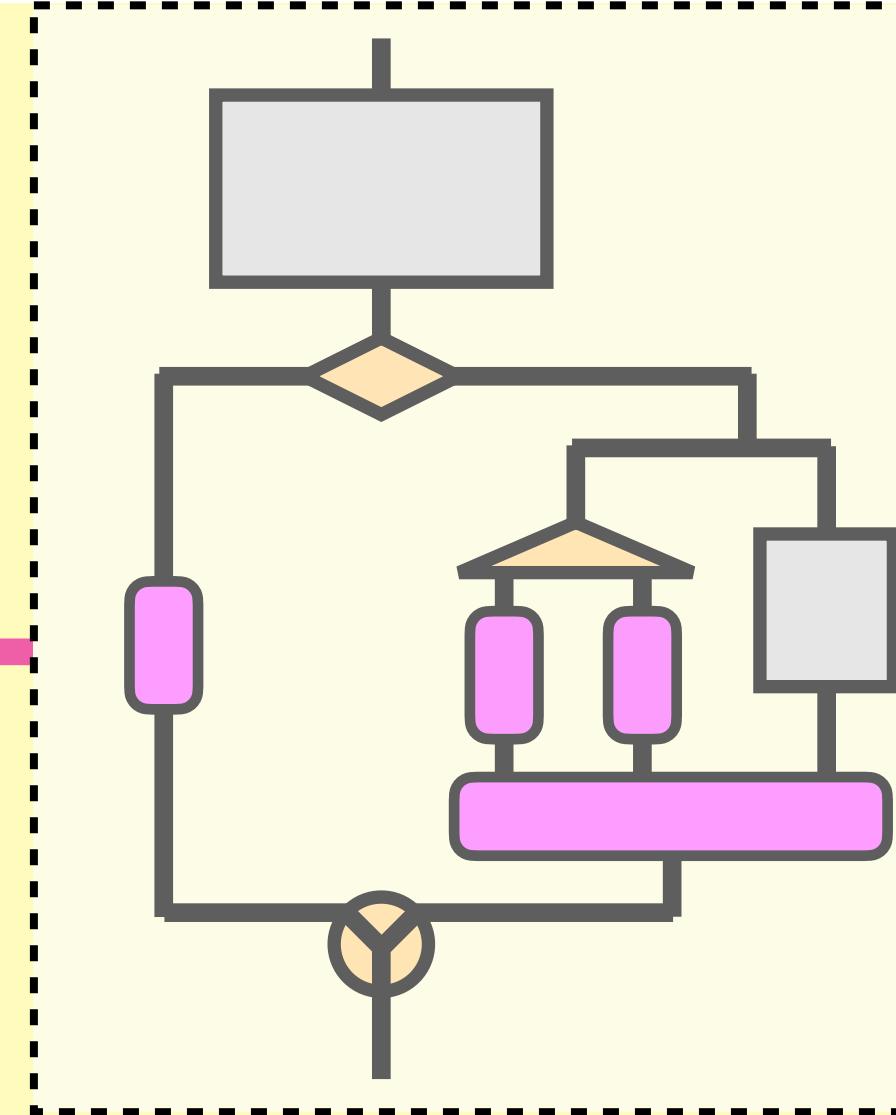


... delambdified so far ...

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
```



```
AndThen(  
    askForAccept,  
    Switch(  
        declined,  
        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            results  
        )))
```



... delambdified so far ...

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
```



```
AndThen(  
    askForAccept,  
    Switch(  
        declined,  
        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            results  
        )))
```

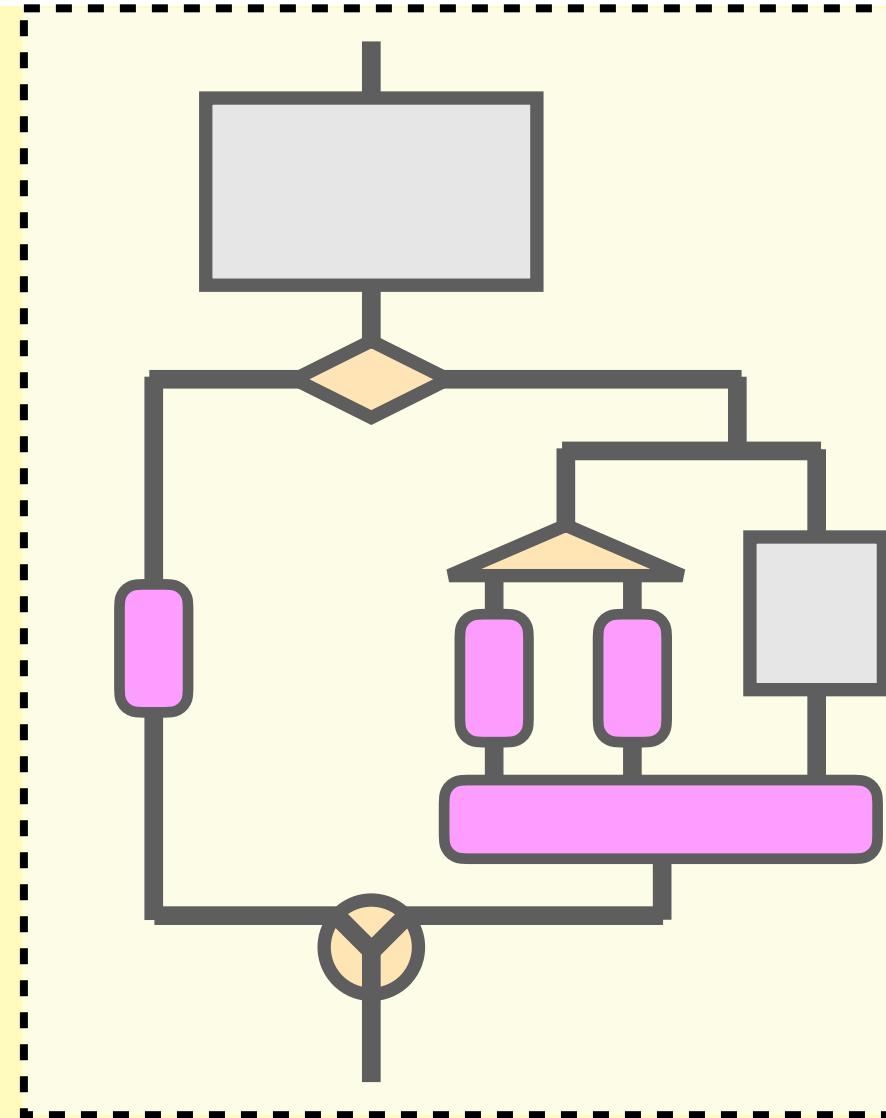


... delambdified so far ...

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
```



```
AndThen(  
    askForAccept,  
    Switch(  
        declined,  
        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            results  
        )))
```

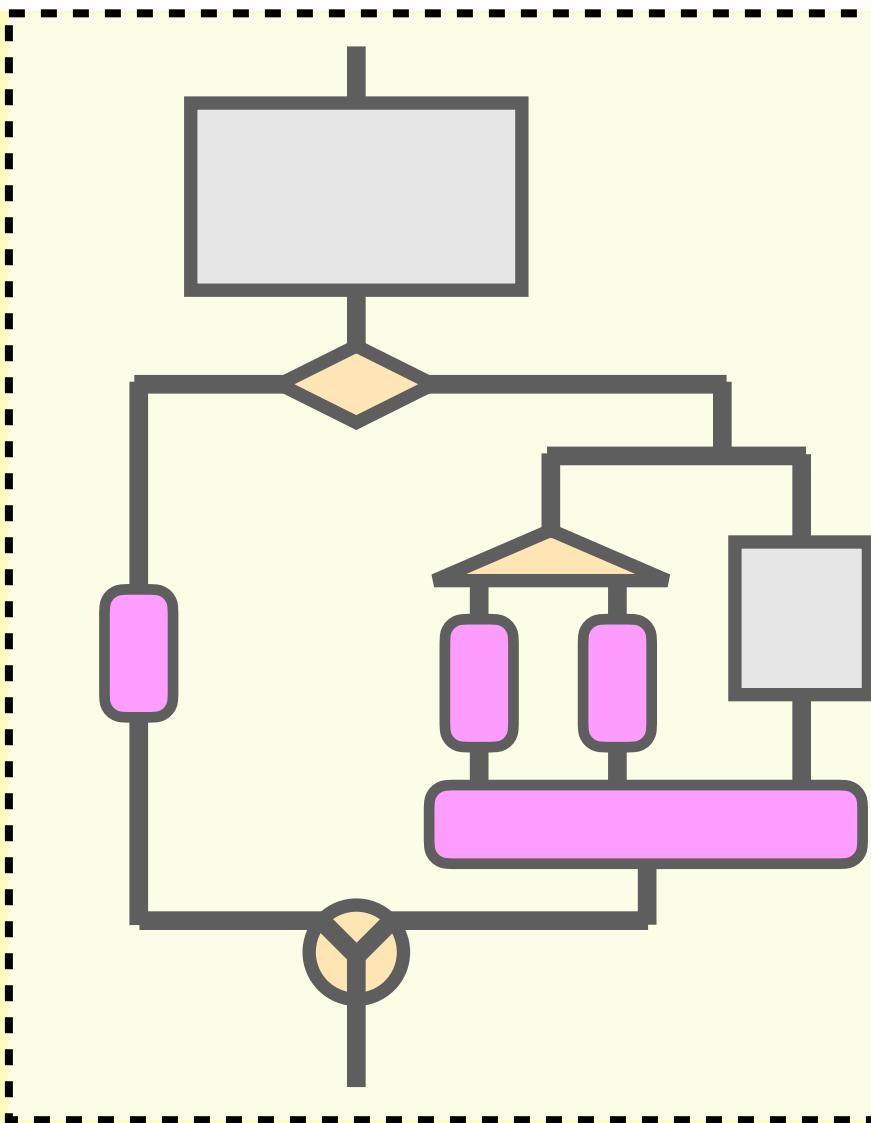


... delambdified so far ...

```
Flow { candidate =>  
  askForAccept(candidate) switch {  
    case Left(x) =>  
      declined(x)  
    case Right(id ** history) =>  
      val crimi = checkCrimi(id)  
      val civil = checkCivil(id)  
      val verif = verify(history)  
      results(crimi ** civil ** verif)  
  }  
}
```



AndThen(
 askForAccept,
 Switch(
 declined,
 AndThen(
 Par(
 AndThen(
 Dup(),
 Par(checkCrimi, checkCivil)
),
 verify
),
 results
)))

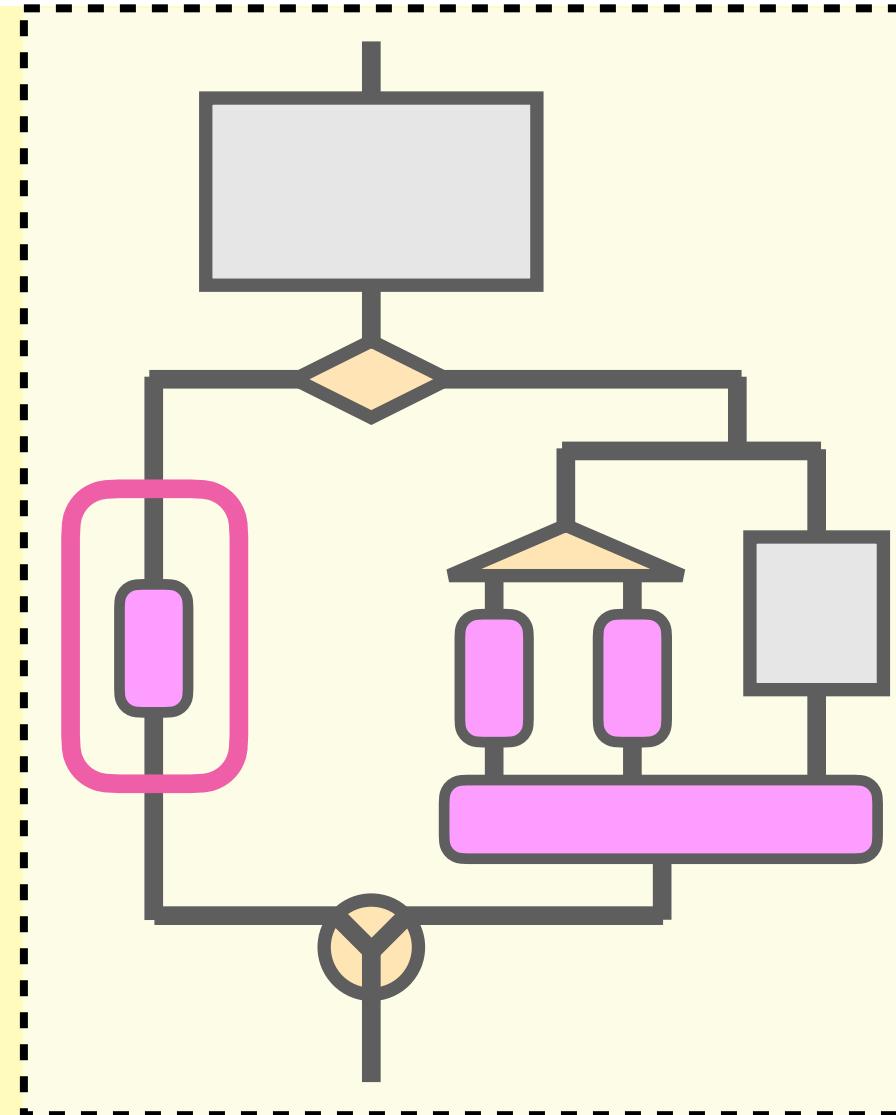


... delambdified so far ...

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
```



```
AndThen(  
    askForAccept,  
    Switch(  
        declined,  
        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            results  
        )))
```

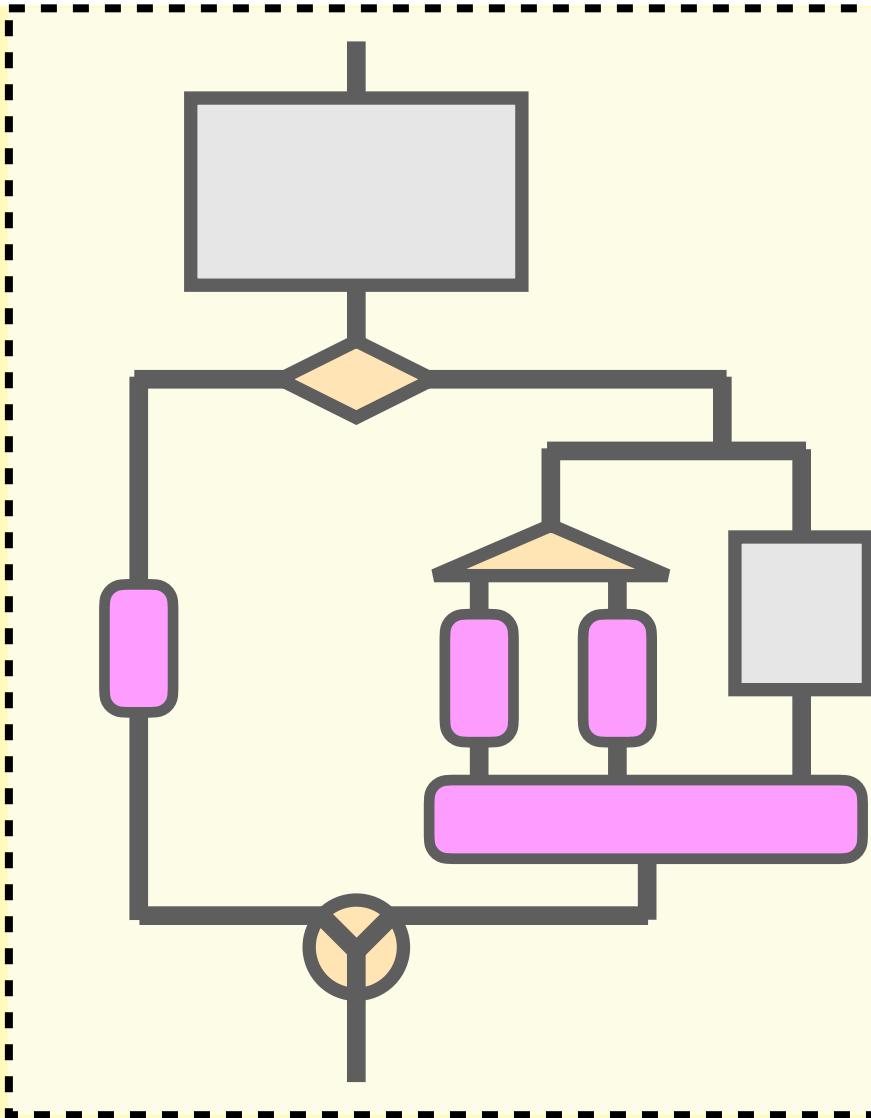


... delambdified so far ...

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
```



```
AndThen(  
    askForAccept,  
    Switch(  
        declined,  
        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            results  
        )))
```

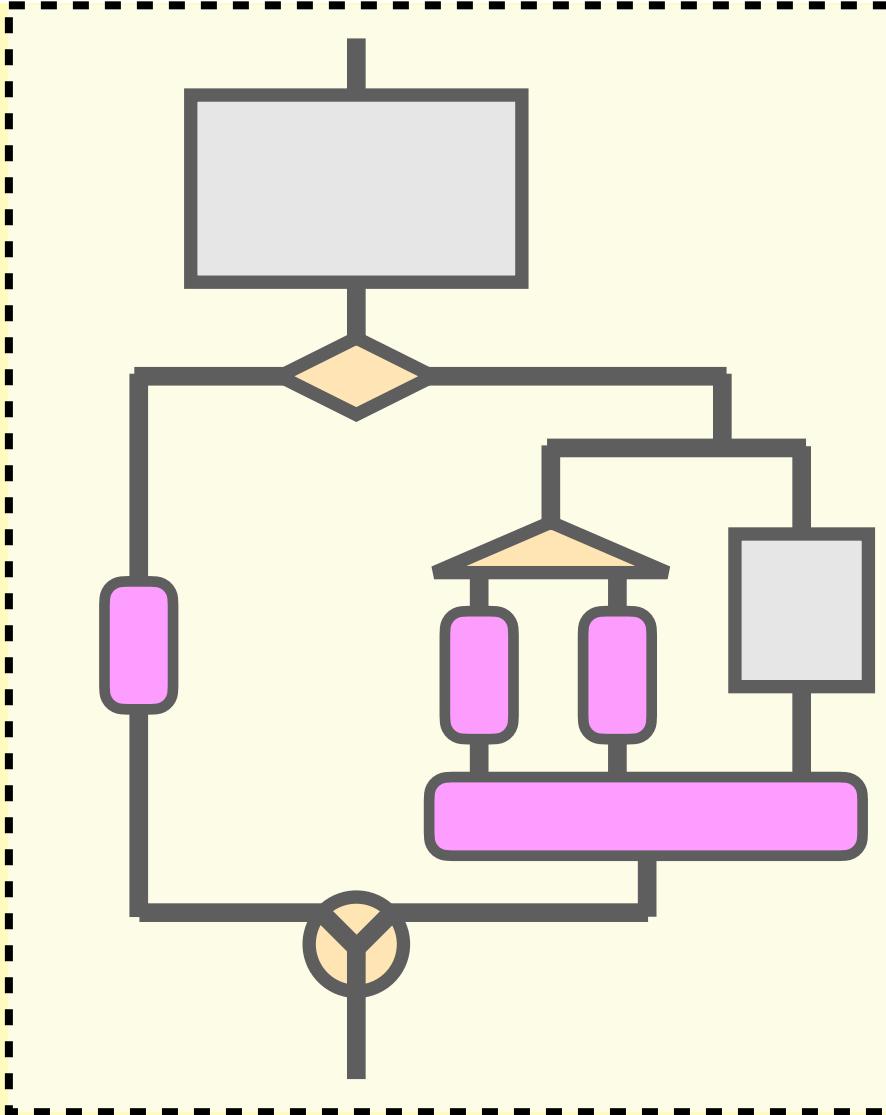


... delambdified so far ...

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
```



```
AndThen(  
    askForAccept,  
    Switch(  
        declined,  
        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            results  
        )))
```



switch : the easy case

```
Flow { candidate =>
    askForAccept(candidate) switch {
        case Left(x) =>
            declined(x)
        case Right(id ** history) =>
            val crimi = checkCrimi(id)
            val civil = checkCivil(id)
            val verif = verify(history)
            results(crimi ** civil ** verif)
    }
}
```



switch : the easy case

non-capturing

```
Flow { candidate =>
    askForAccept(candidate) switch {
        case Left(x) =>
            declined(x)
        case Right(id ** history) =>
            val crimi = checkCrimi(id)
            val civil = checkCivil(id)
            val verif = verify(history)
            results(crimi ** civil ** verif)
    }
}
```



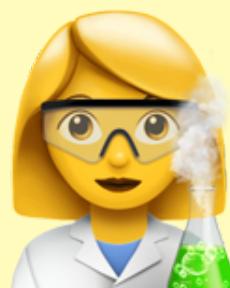
switch : the easy case

non-capturing

```
Flow { candidate =>
  askForAccept(candidate) switch {
    case Left(x) =>
      declined(x)
    case Right(id ** history) =>
      val crimi = checkCrimi(id)
      val civil = checkCivil(id)
      val verif = verify(history)
      results(crimi ** civil ** verif)
  }
}
```

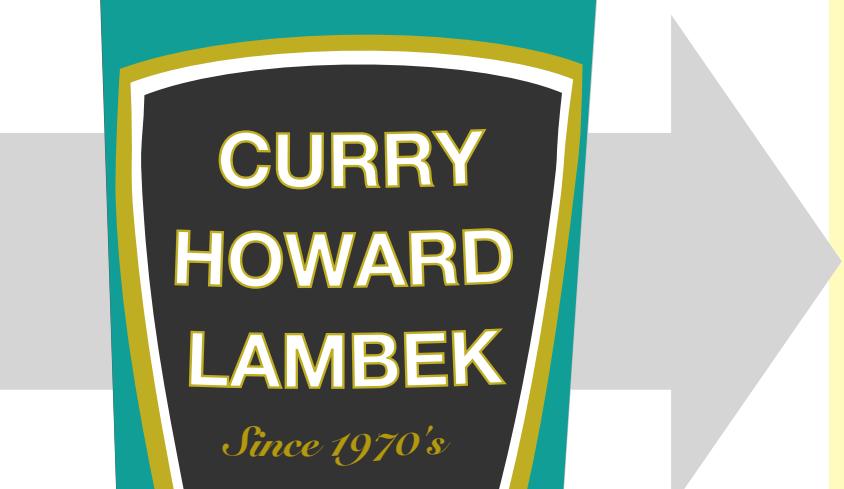


```
extension [A, B](expr: Expr[A ++ B])
  def switch[R](
    f: Either[Expr[A], Expr[B]] => Expr[R],
  ): Expr[R] =
    val f1: Flow[A, R] = delambdify(a => f(Left(a)))
    val f2: Flow[B, R] = delambdify(b => f(Right(b)))
    val ff: Flow[A ++ B, R] = Switch(f1, f2)
    ff(expr)
```

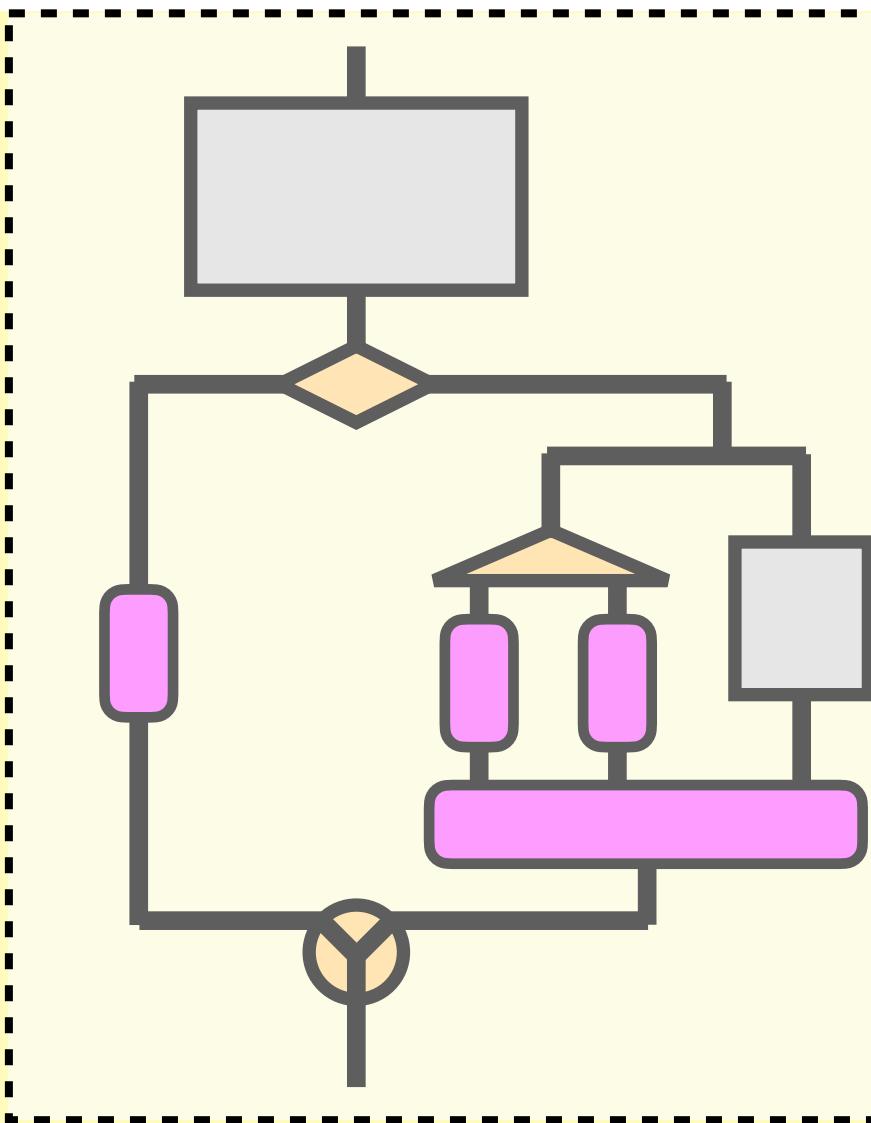


... delambdified so far ...

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
```



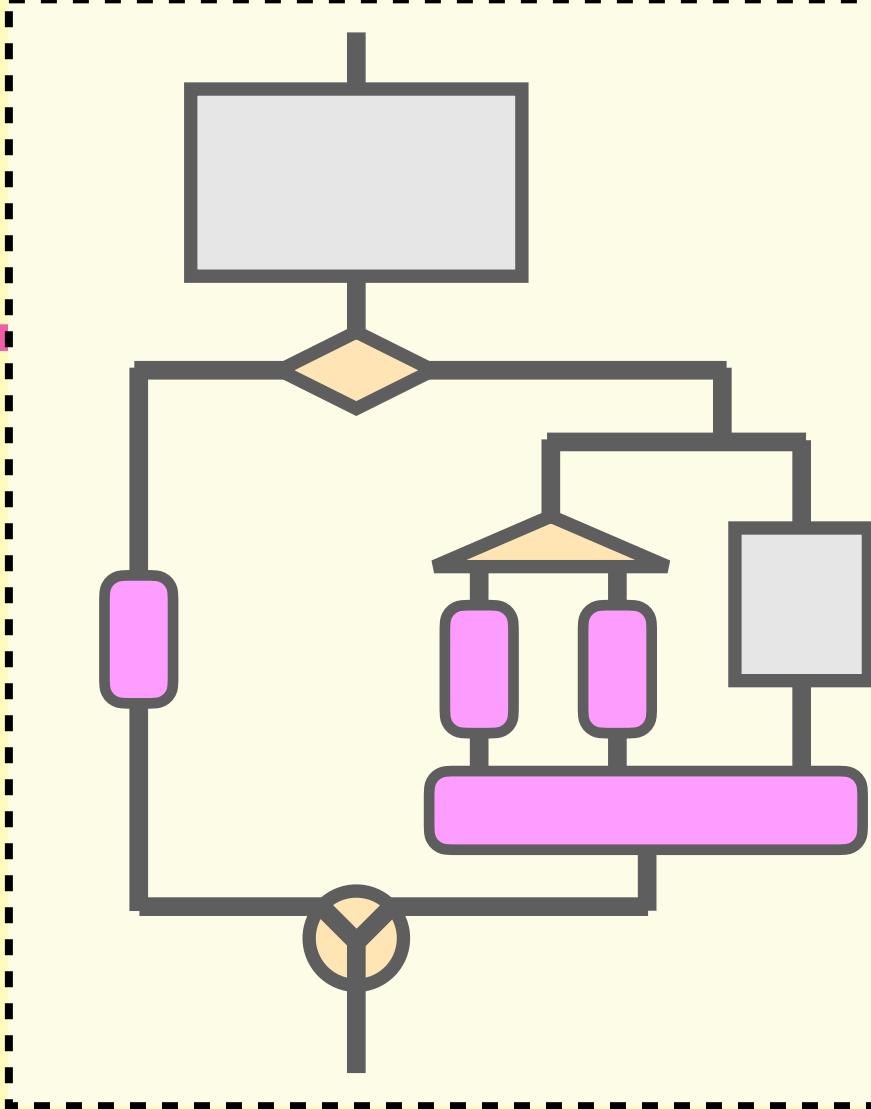
```
AndThen(  
    askForAccept,  
    Switch(  
        declined,  
        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            results  
        )))
```



... delambdified so far ...

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
```

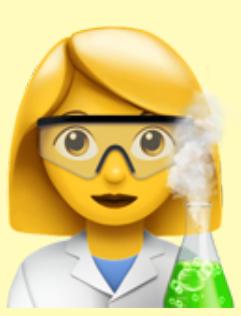


```
AndThen(  
    askForAccept,  
    Switch(  
        declined,  
        AndThen(  
            Par(  
                AndThen(  
                    Dup(),  
                    Par(checkCrimi, checkCivil)  
                ),  
                verify  
            ),  
            results  
        )))  

```

... delambdified so far ...

```
Flow { candidate =>  
    askForAccept(candidate) switch {  
        case Left(x) =>  
            declined(x)  
        case Right(id ** history) =>  
            val crimi = checkCrimi(id)  
            val civil = checkCivil(id)  
            val verif = verify(history)  
            results(crimi ** civil ** verif)  
    }  
}
```



```
    AndThen(  
        askForAccept,  
        Switch(  
            declined,  
            AndThen(  
                Par(  
                    AndThen(  
                        Dup(),  
                        Par(checkCrimi, checkCivil)  
                    ),  
                    verify  
                ),  
                results  
            )  
        )))  

```

switch : the capturing case

```
def switch[A, B, ..., R] (
```

switch : the capturing case

```
def switch[A, B, ..., R] (
```

```
  fa: Expr[A] => Expr[R],
```

```
  fb: Expr[B] => Expr[R],
```

```
  ...
```

switch : the capturing case

```
def switch[A, B, ..., R] (   
    fa: Expr[A] => Expr[R],   
    fb: Expr[B] => Expr[R],   
    ...   
    sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R],
```

switch : the capturing case

```
def switch[A, B, ..., R] (fa: Expr[A] => Expr[R], fb: Expr[B] => Expr[R], ...sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R],  
case Switch[X, Y, R] (l: Flow[X, R], r: Flow[Y, R], ) extends Flow[X ++ Y, R]
```



switch : the capturing case

```
def switch[A, B, ..., R] (fa: Expr[A] => Expr[R], fb: Expr[B] => Expr[R], ...sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R], distrib: [X, Y, Z] => Flow[X ** (Y ++ Z), (X ** Y) ++ (X ** Z)]  
case Switch[X, Y, R] (l: Flow[X, R], r: Flow[Y, R], ) extends Flow[X ++ Y, R]
```



switch : the capturing case

```
def switch[A, B, ..., R] (fa: Expr[A] => Expr[R], fb: Expr[B] => Expr[R], ...sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R], distrib: [X, Y, Z] => Flow[X ** (Y ++ Z), (X ** Y) ++ (X ** Z)]
```

```
case Switch[X, Y, R] (l: Flow[X, R], r: Flow[Y, R], ) extends Flow[X ++ Y, R]
```



```
case Distribute[X, Y, Z] ()  
extends Flow[  
  X ** (Y ++ Z),  
  (X ** Y) ++ (X ** Z)
```



switch : the capturing case

```
def switch[A, B, ..., R] (fa: Expr[A] => Expr[R], fb: Expr[B] => Expr[R], ...sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R], distrib: [X, Y, Z] => Flow[X ** (Y ++ Z), (X ** Y) ++ (X ** Z)]) : (
```

```
case Switch[X, Y, R] (l: Flow[X, R], r: Flow[Y, R], ) extends Flow[X ++ Y, R]
```



```
case Distribute[X, Y, Z] ()  
extends Flow[  
X ** (Y ++ Z),  
(X ** Y) ++ (X ** Z)]
```



switch : the capturing case

```
def switch[A, B, ..., R] (fa: Expr[A] => Expr[R], fb: Expr[B] => Expr[R], ...sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R], distrib: [X, Y, Z] => Flow[X ** (Y ++ Z), (X ** Y) ++ (X ** Z)]) : (Expr[Q],
```

```
case Switch[X, Y, R] (l: Flow[X, R], r: Flow[Y, R], ) extends Flow[X ++ Y, R]
```



```
case Distribute[X, Y, Z] ()  
extends Flow[  
X ** (Y ++ Z),  
(X ** Y) ++ (X ** Z)]
```



switch : the capturing case

```
def switch[A, B, ..., R] (fa: Expr[A] => Expr[R], fb: Expr[B] => Expr[R], ...sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R], distrib: [X, Y, Z] => Flow[X ** (Y ++ Z), (X ** Y) ++ (X ** Z)]) : (Expr[Q],
```

Captured

```
case Switch[X, Y, R] (l: Flow[X, R], r: Flow[Y, R], ) extends Flow[X ++ Y, R]
```



```
case Distribute[X, Y, Z] ()  
extends Flow[  
X ** (Y ++ Z),  
(X ** Y) ++ (X ** Z)]
```



switch : the capturing case

```
def switch[A, B, ..., R] (fa: Expr[A] => Expr[R], fb: Expr[B] => Expr[R], ...sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R], distrib: [X, Y, Z] => Flow[X ** (Y ++ Z), (X ** Y) ++ (X ** Z)]) : (Expr[Q], Flow[Q ** (A ++ B ++ ...), R])
```

Captured

```
case Switch[X, Y, R] (l: Flow[X, R], r: Flow[Y, R], ) extends Flow[X ++ Y, R]
```



```
case Distribute[X, Y, Z] ()  
extends Flow[X ** (Y ++ Z), (X ** Y) ++ (X ** Z)]
```



switch : the capturing case

```
def switch[A, B, ..., R] (fa: Expr[A] => Expr[R], fb: Expr[B] => Expr[R], ...sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R], distrib: [X, Y, Z] => Flow[X ** (Y ++ Z), (X ** Y) ++ (X ** Z)]) : (Expr[Q], Flow[Q ** (A ++ B ++ ...), R]) // for some type Q
```

Captured

```
case Switch[X, Y, R] (l: Flow[X, R], r: Flow[Y, R], ) extends Flow[X ++ Y, R]
```

```
case Distribute[X, Y, Z] () extends Flow[X ** (Y ++ Z), (X ** Y) ++ (X ** Z)]
```



Also Applicable To

- Loops

```
case DoWhile[A, B]( iteration: Flow[A, A ++ B] ) extends Flow[A, B]
```

- Recursion

- incl. recursive types

- Higher-order functions

- Including closures

- Linearly typed DSLs

... status so far ...

... status so far ...

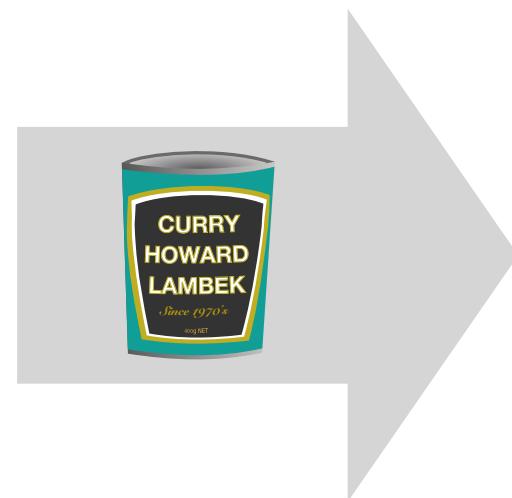
```
Flow { x =>
  ...
  switch {
    case ... =>
      ...
    case ... =>
      val y = ...
      ...
  }
}
```



code

... status so far ...

```
Flow { x =>
  ...
  switch {
    case ... =>
      ...
    case ... =>
      val y = ...
      ...
  }
}
```



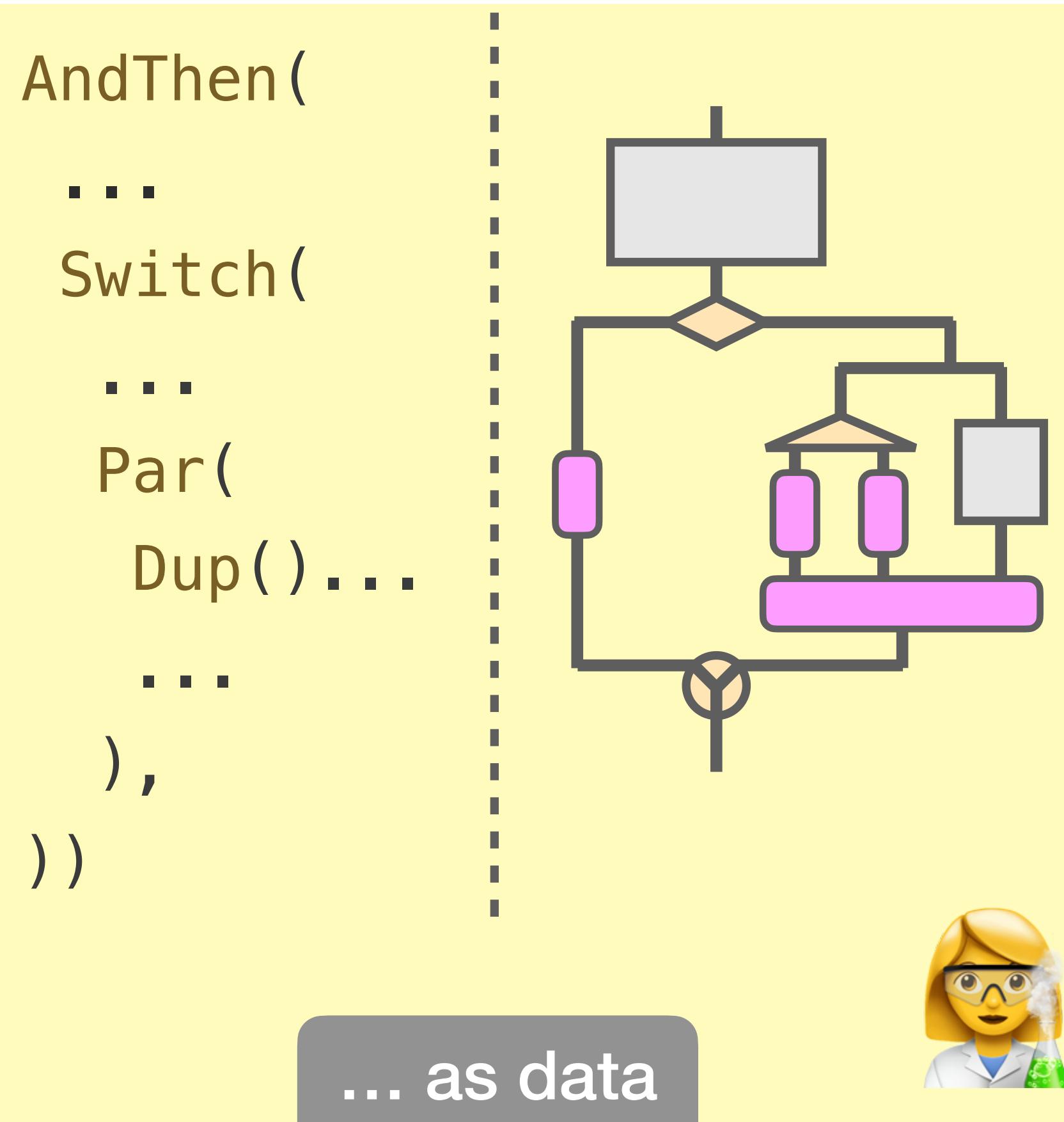
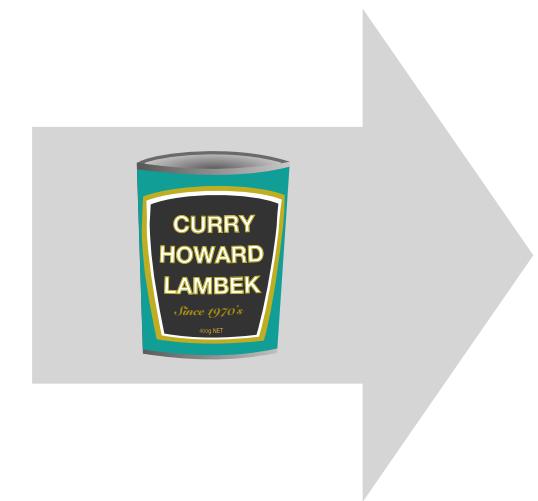
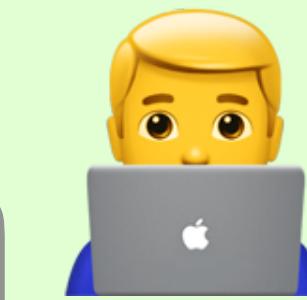
code



... status so far ...

```
Flow { x =>
  ...
  switch {
    case ... =>
      ...
    case ... =>
      val y = ...
      ...
  }
}
```

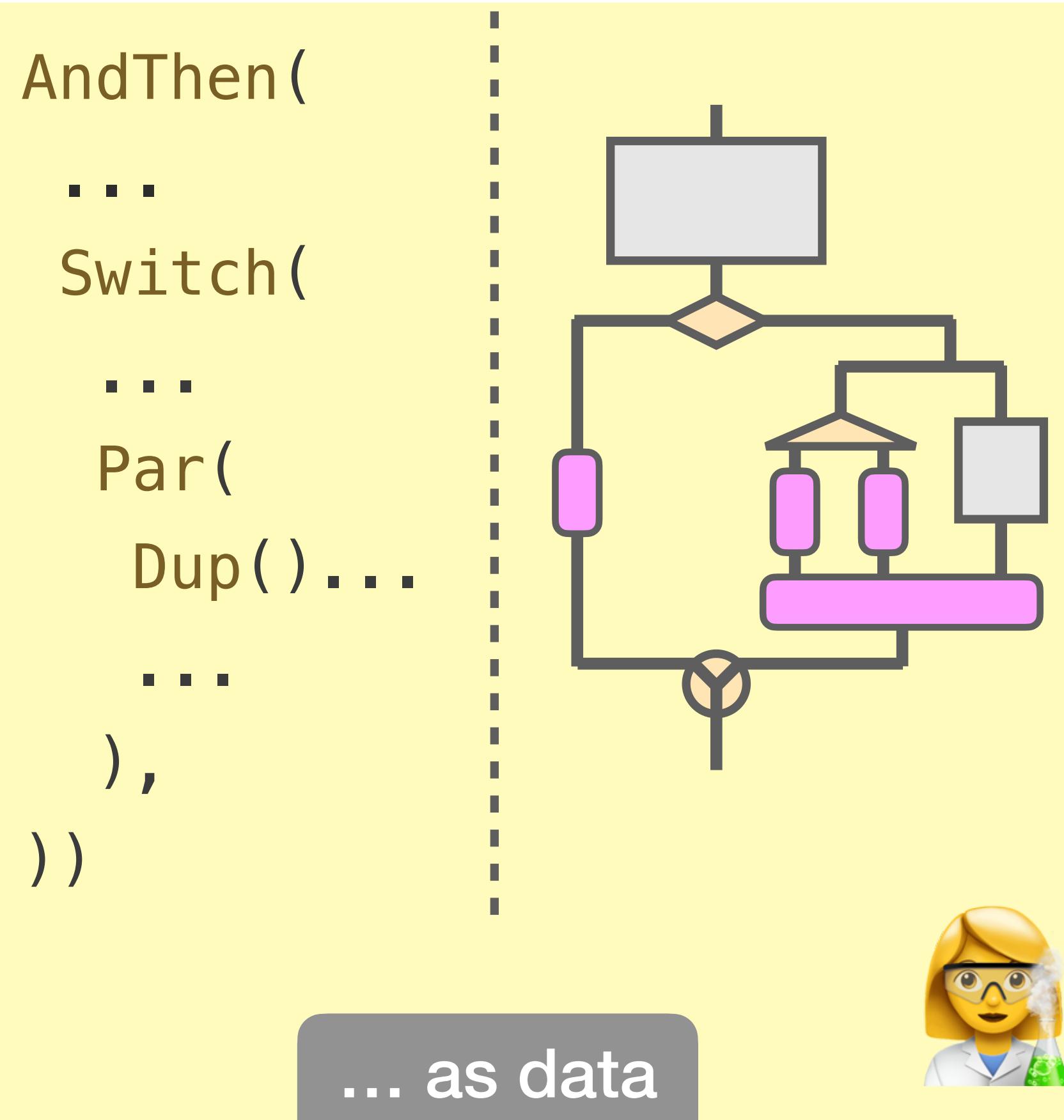
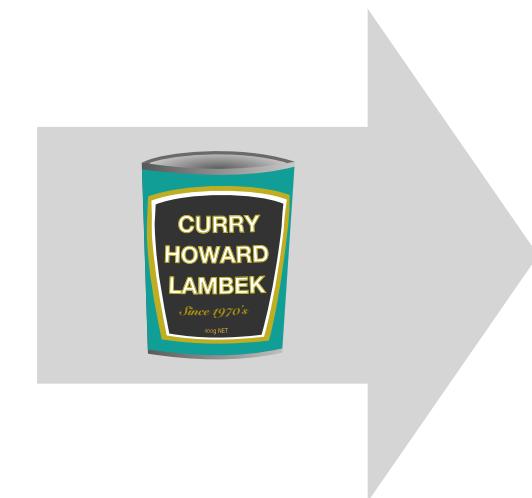
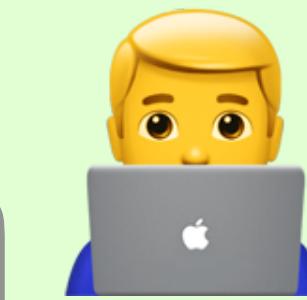
code



... status so far ...

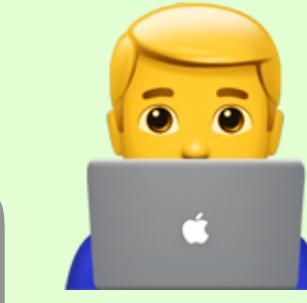
```
Flow { x =>
  ...
  switch {
    case ... =>
      ...
    case ... =>
      val y = ...
      ...
  }
}
```

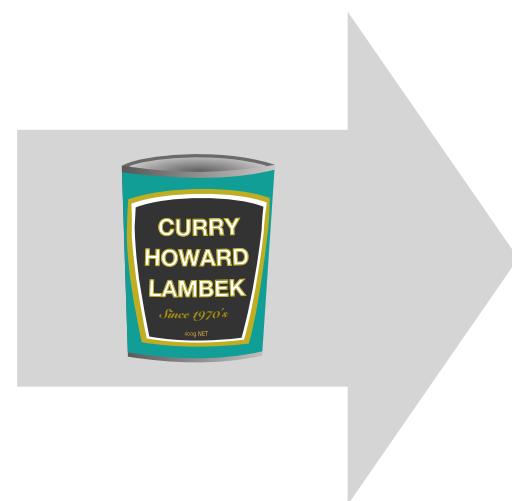
code



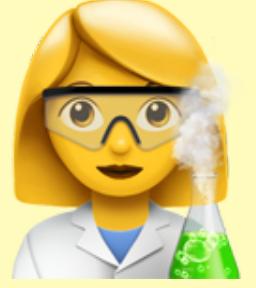
... status so far ...

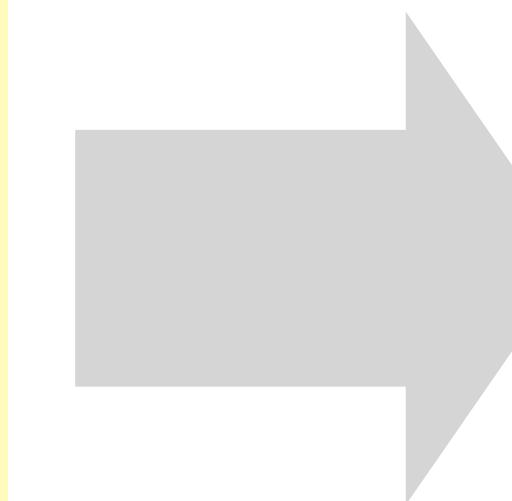
```
Flow { x =>
  ...
  switch {
    case ... =>
      ...
    case ... =>
      val y = ...
      ...
  }
}
```

code 



```
AndThen(
  ...
  Switch(
    ...
    Par(
      Dup(...),
      ...
    );
  )
)
```

... as data 

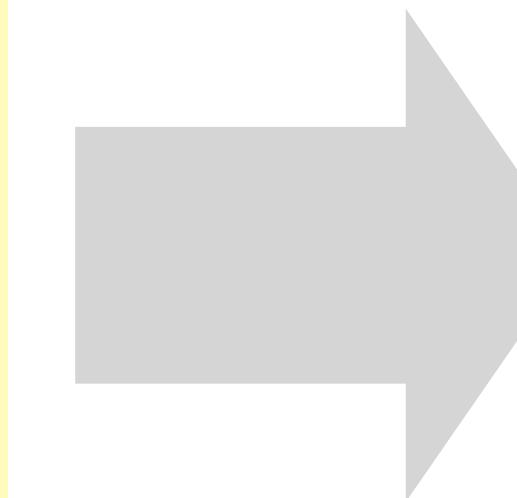
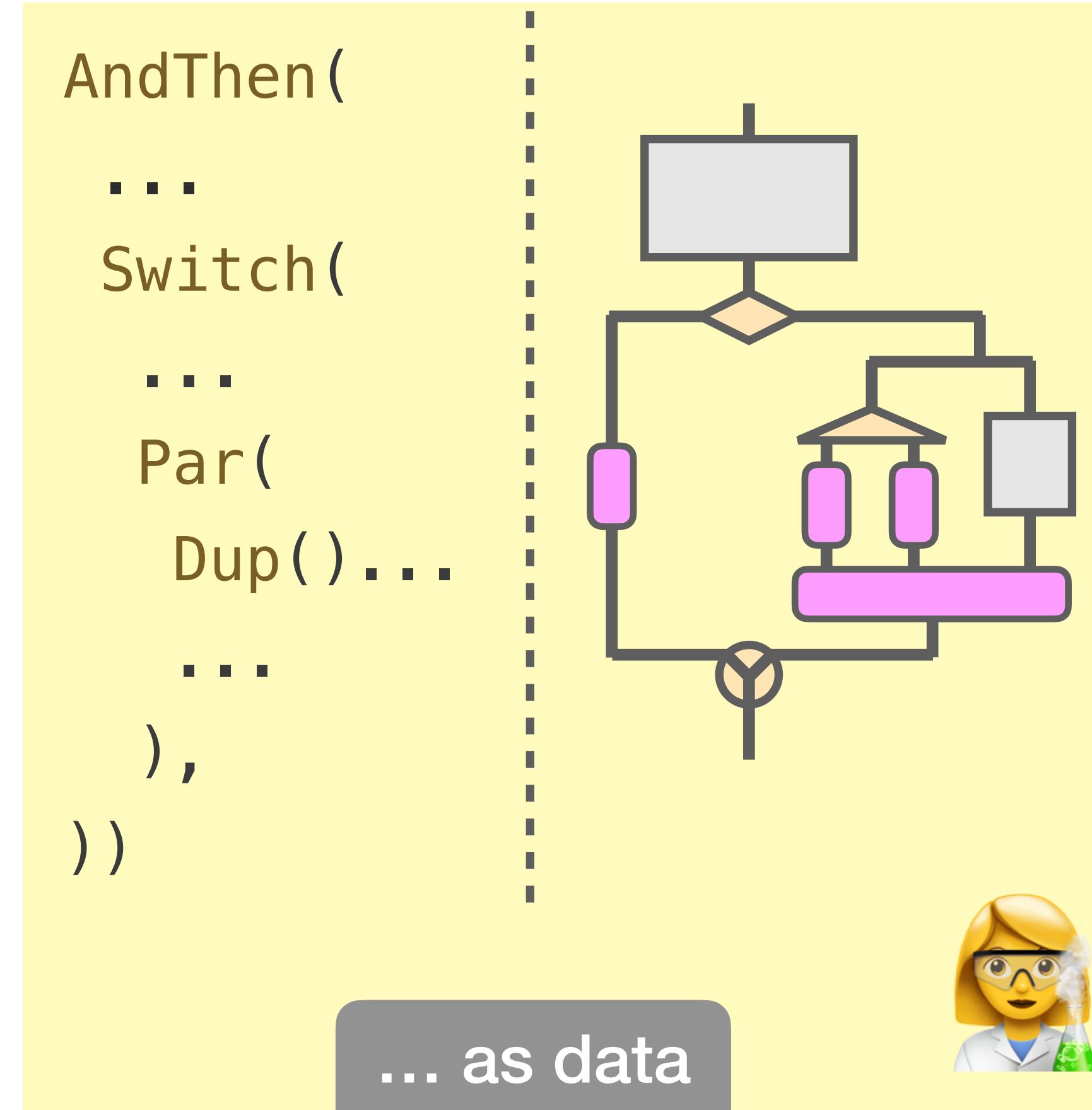


?

... status so far ...

```
Flow { x =>
  ...
  switch {
    case ... =>
      ...
    case ... =>
      val y = ...
      ...
  }
}
```

code 

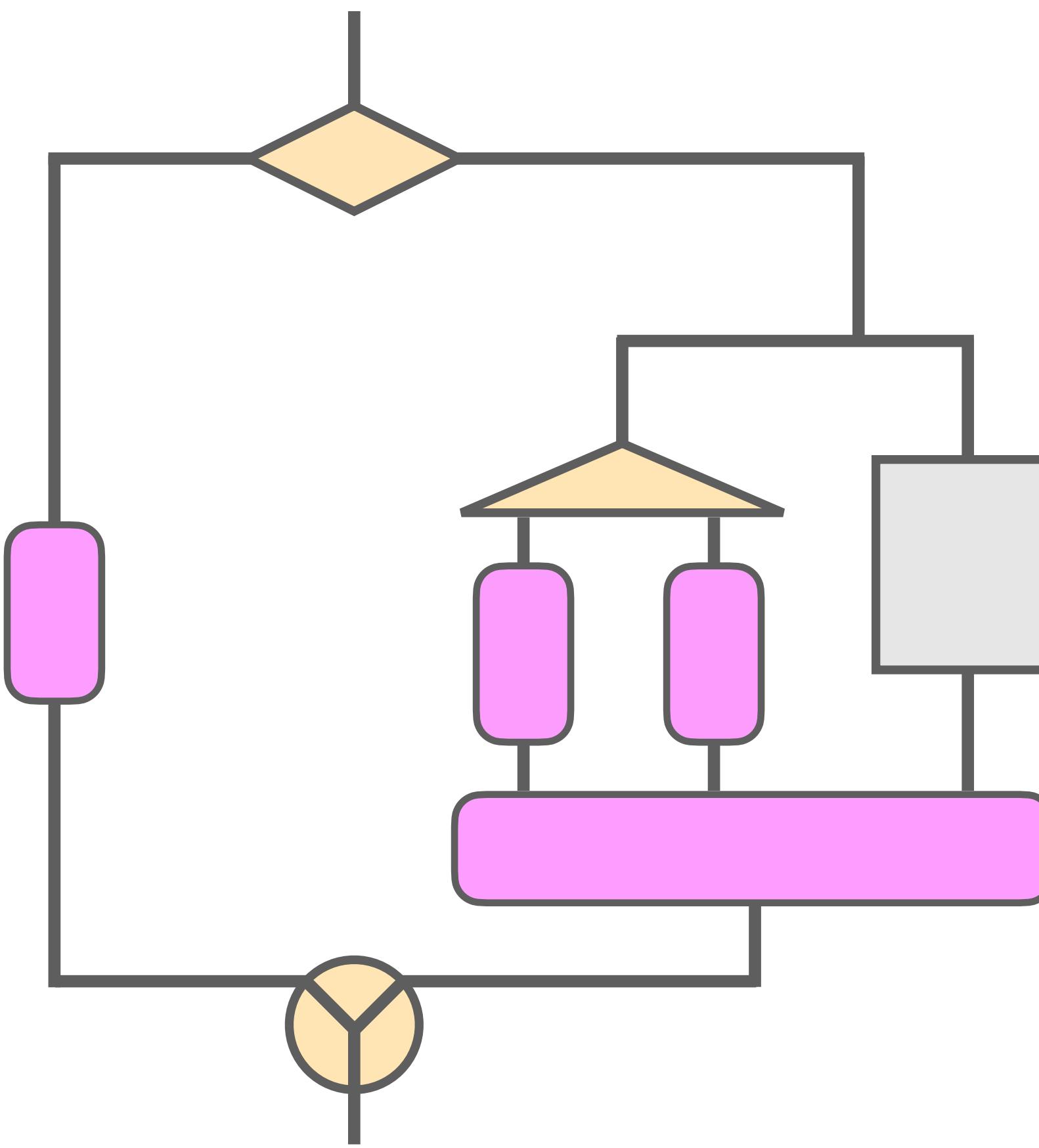


?

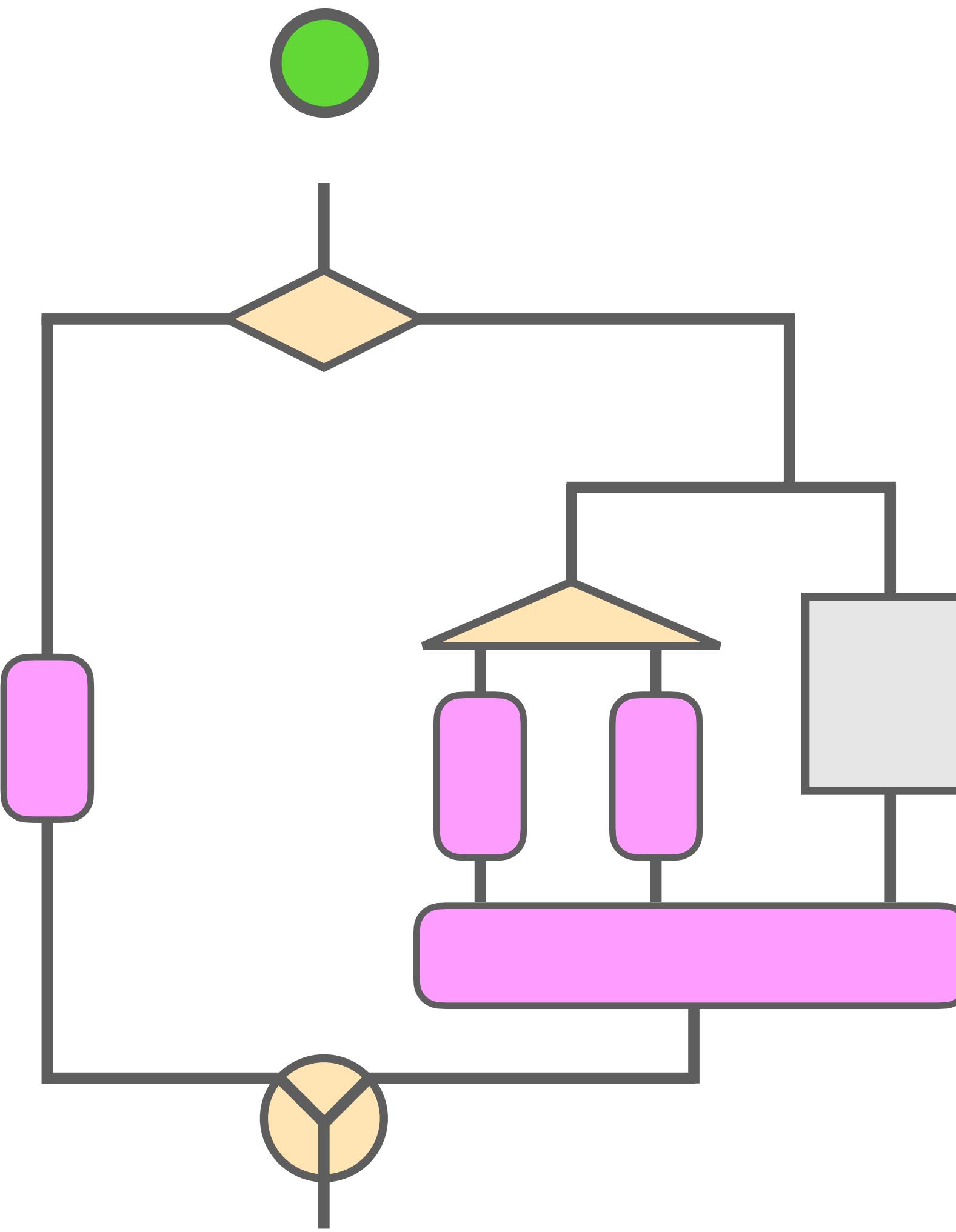
Where's the (*durable*) execution?

Durable Execution

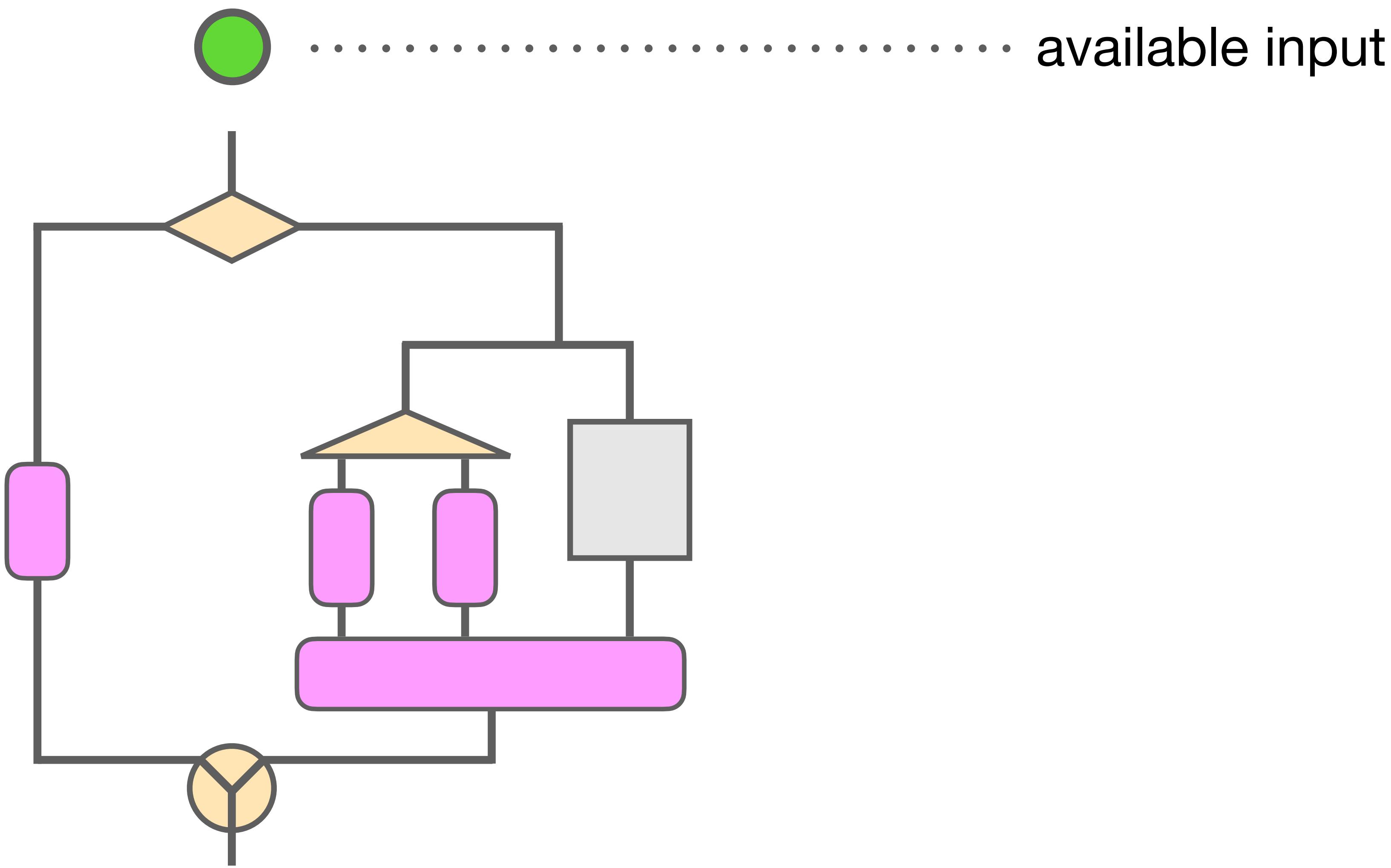
Durable Execution



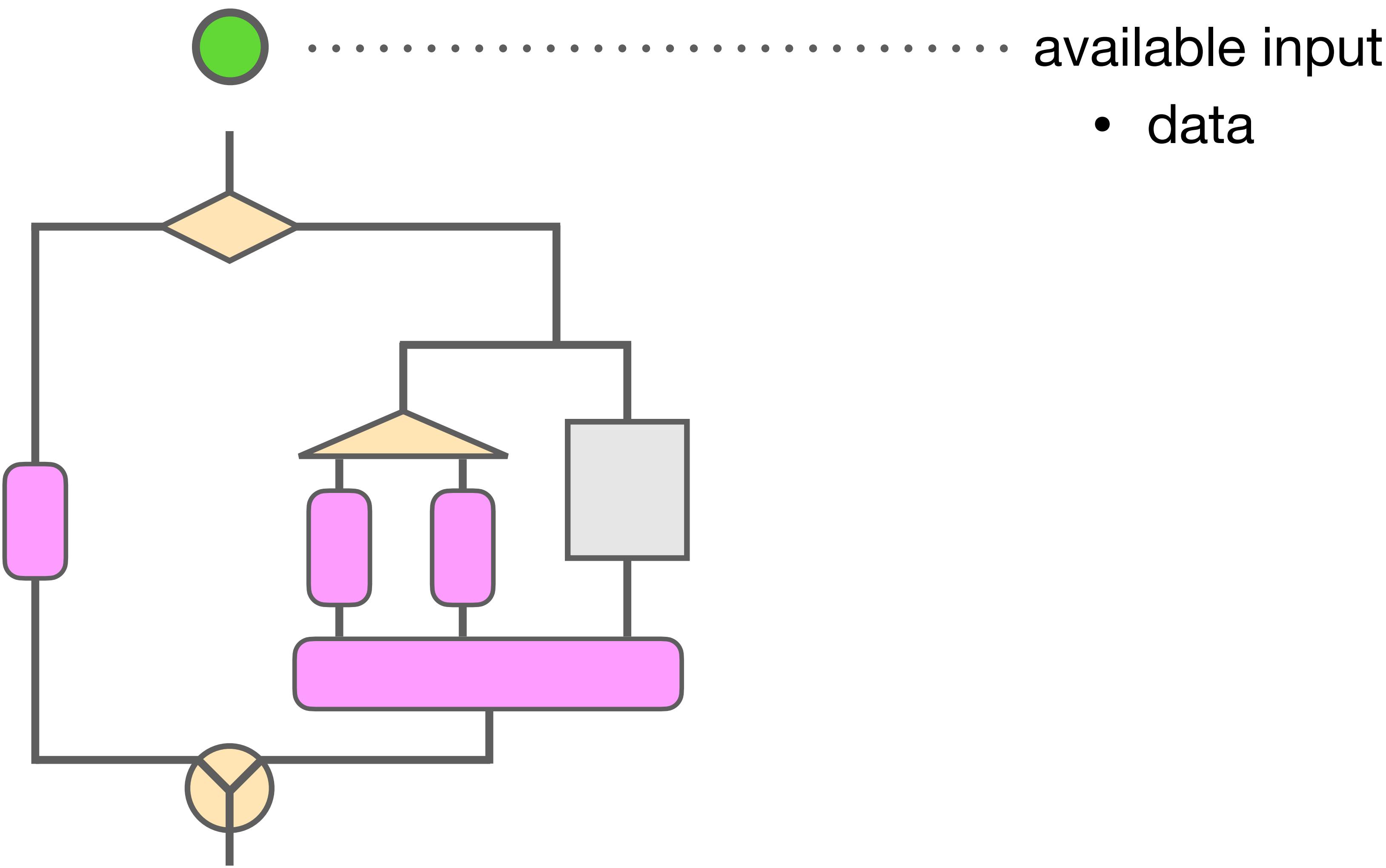
Durable Execution



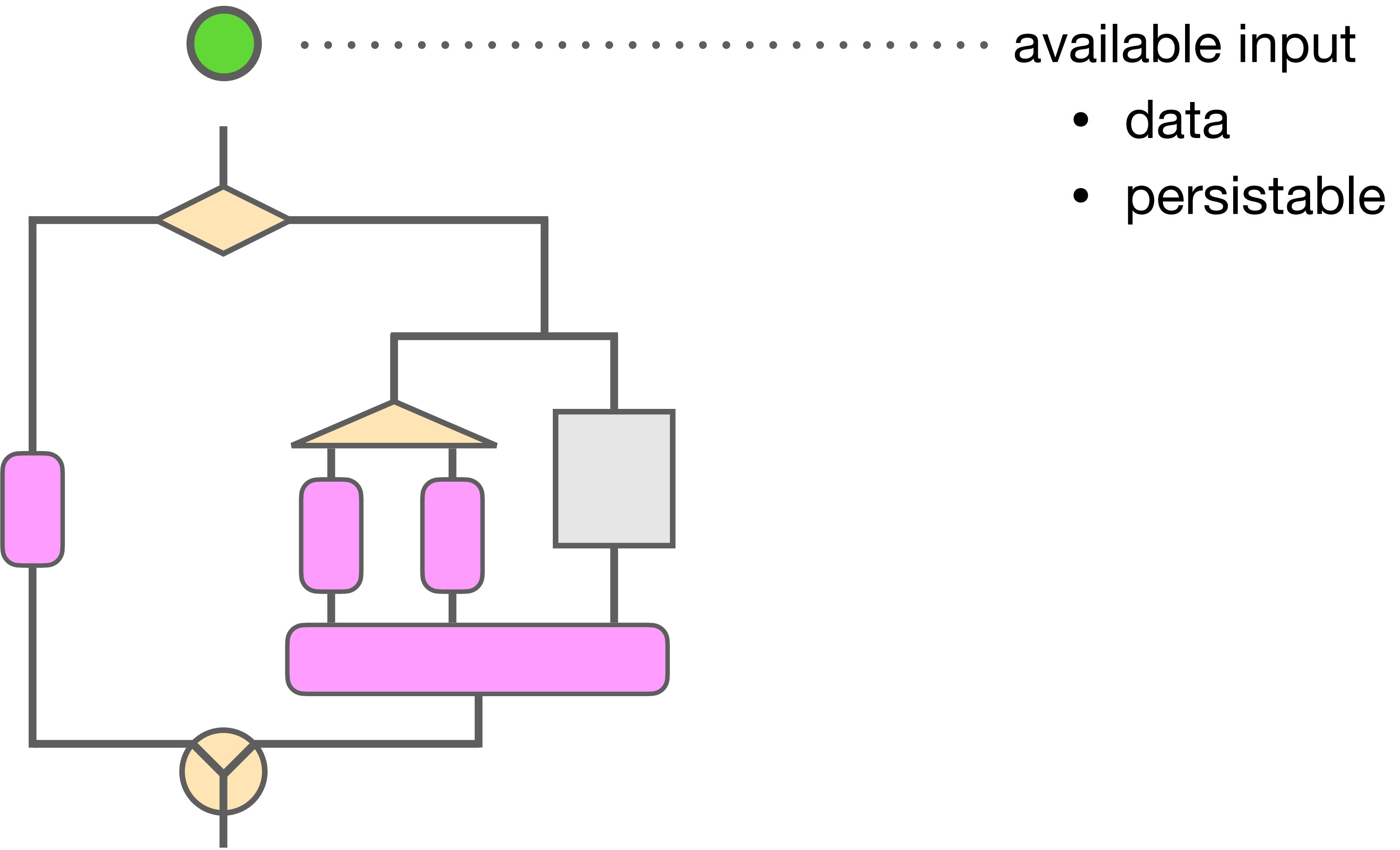
Durable Execution



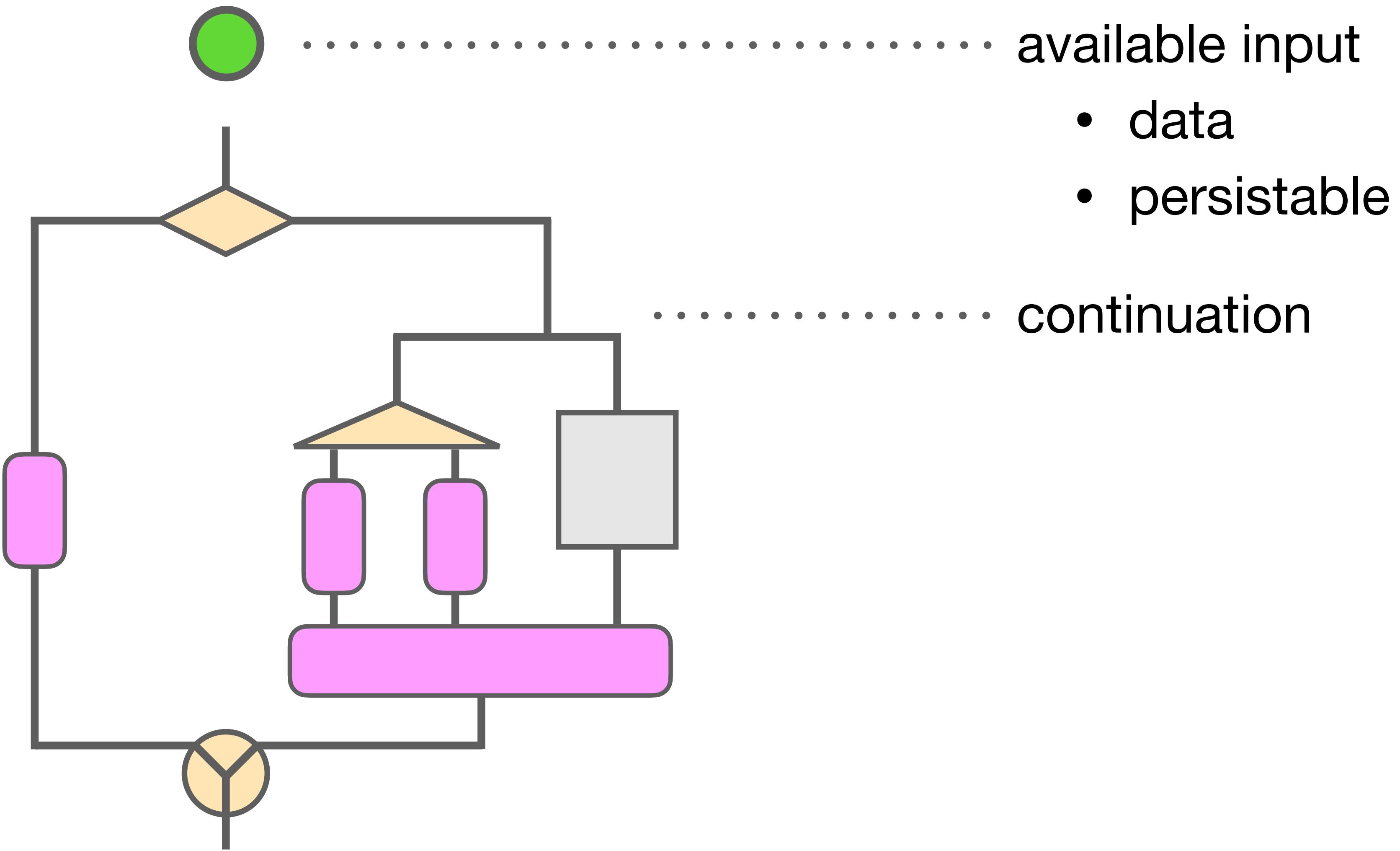
Durable Execution



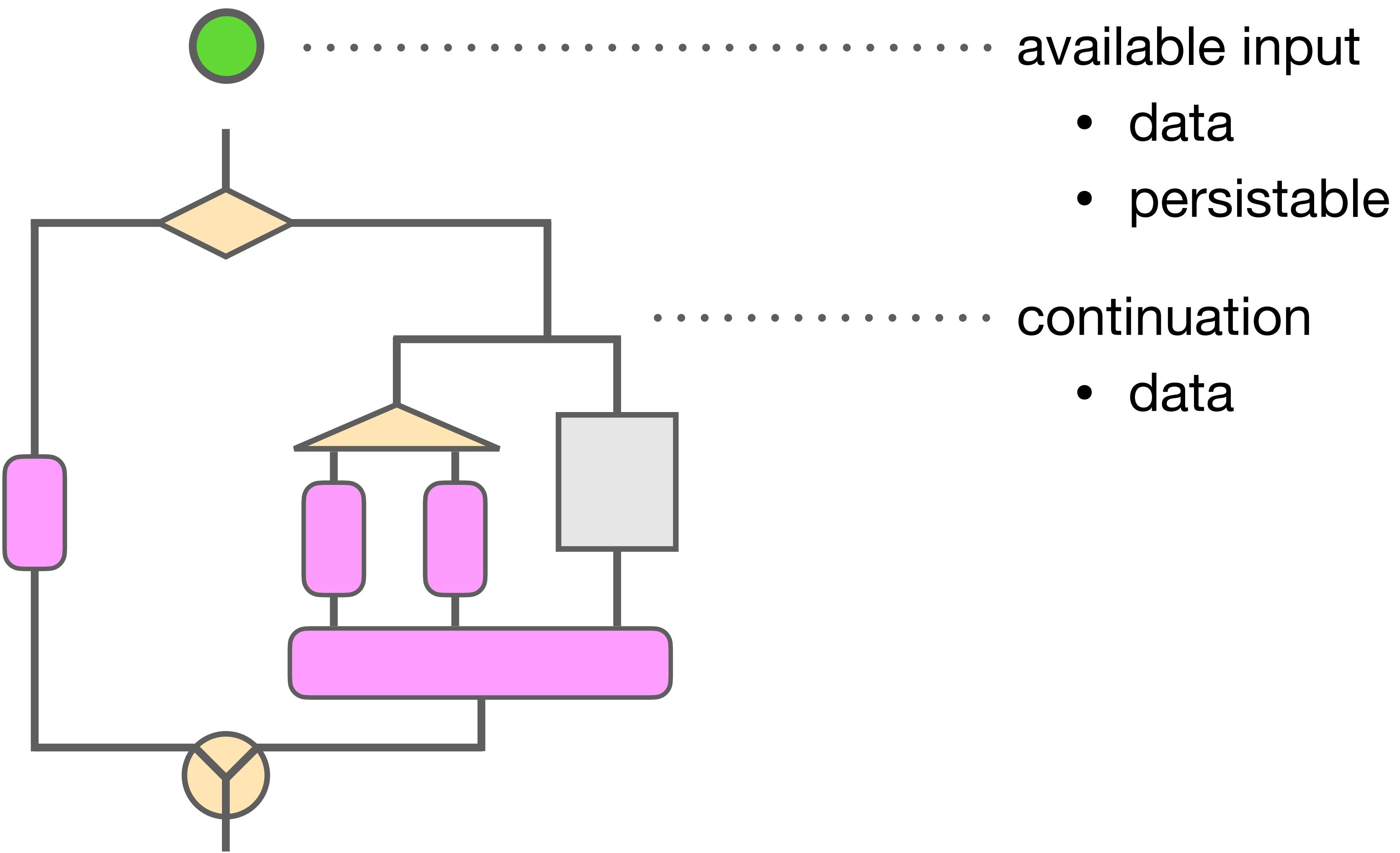
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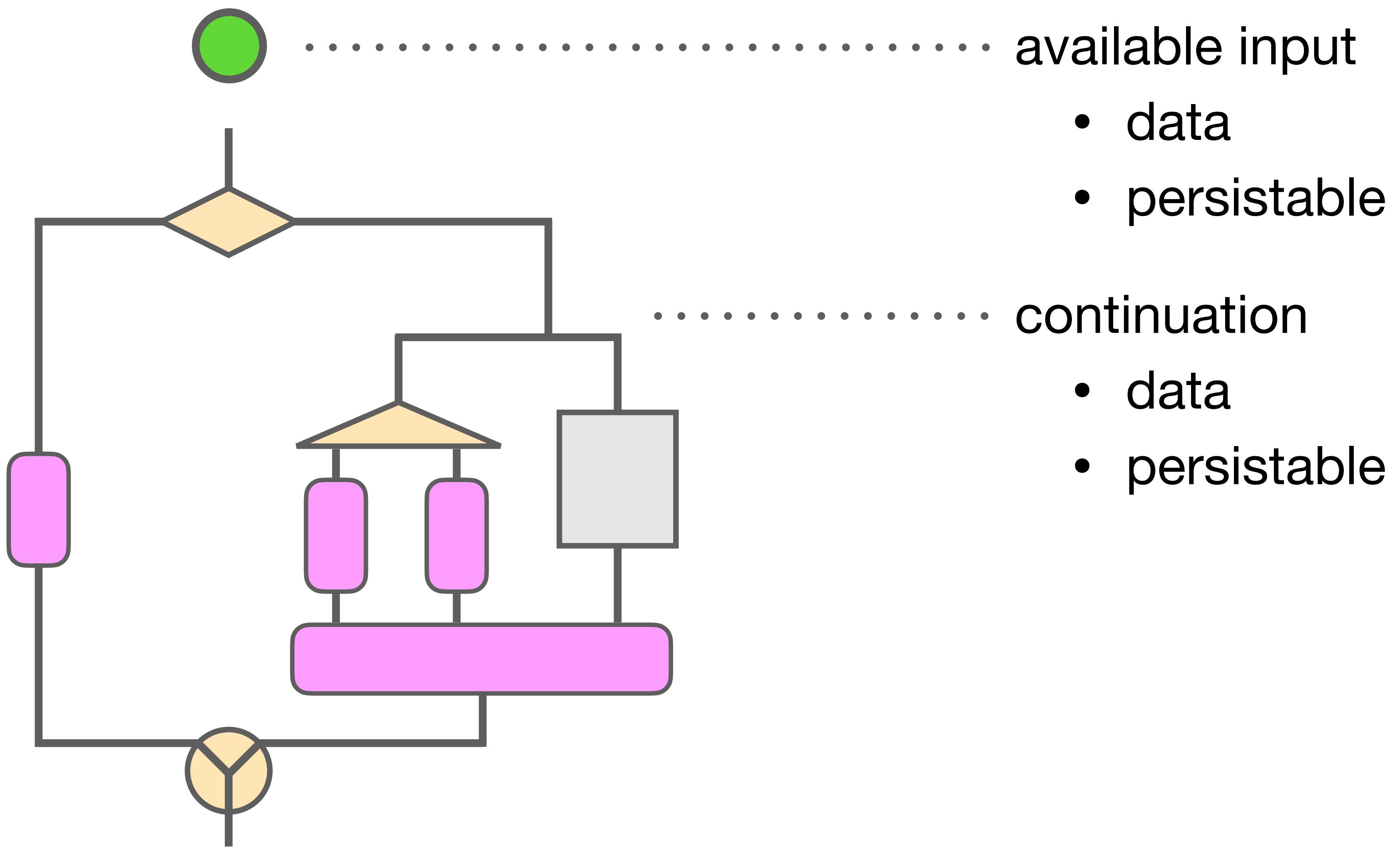
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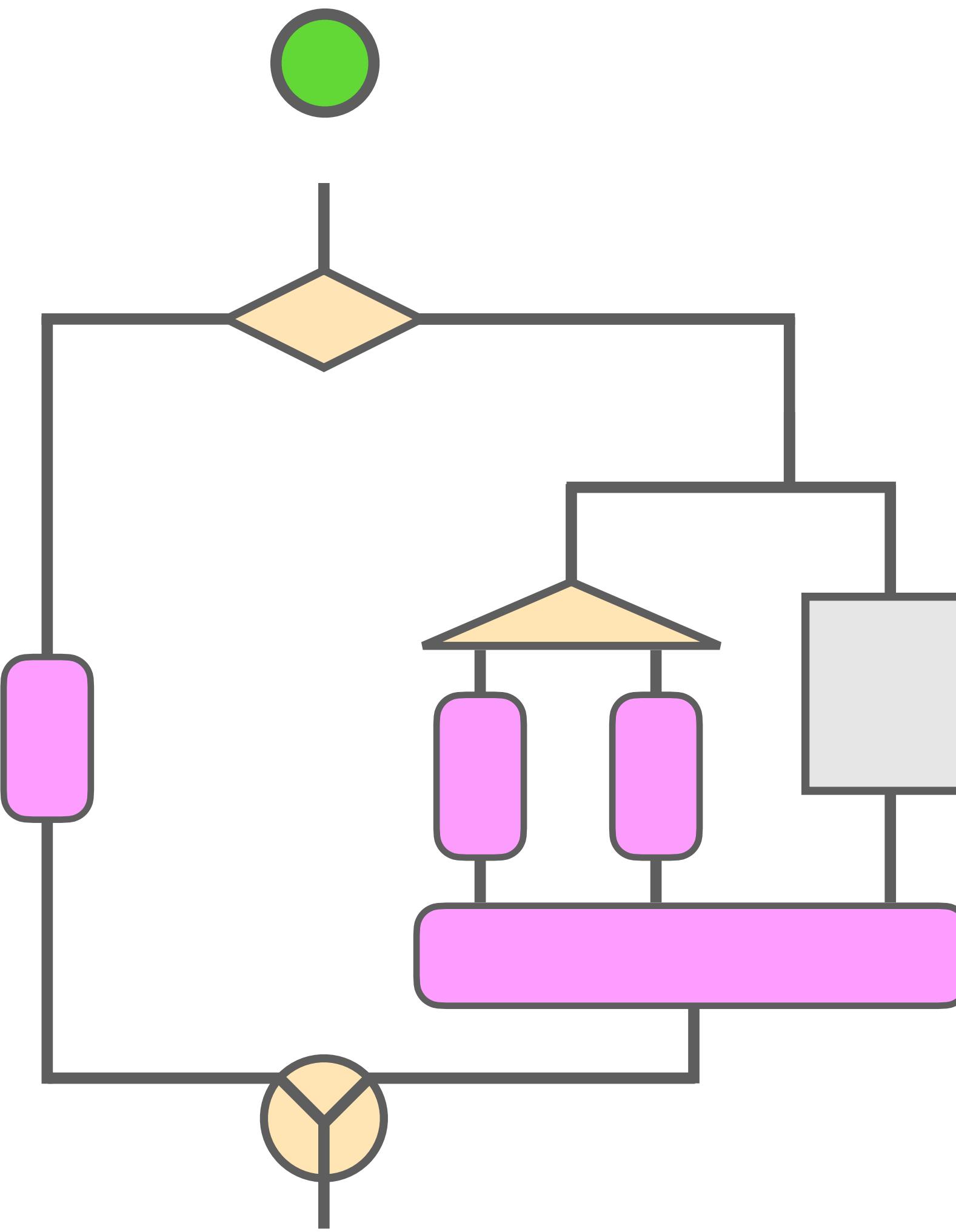
Durable Execution



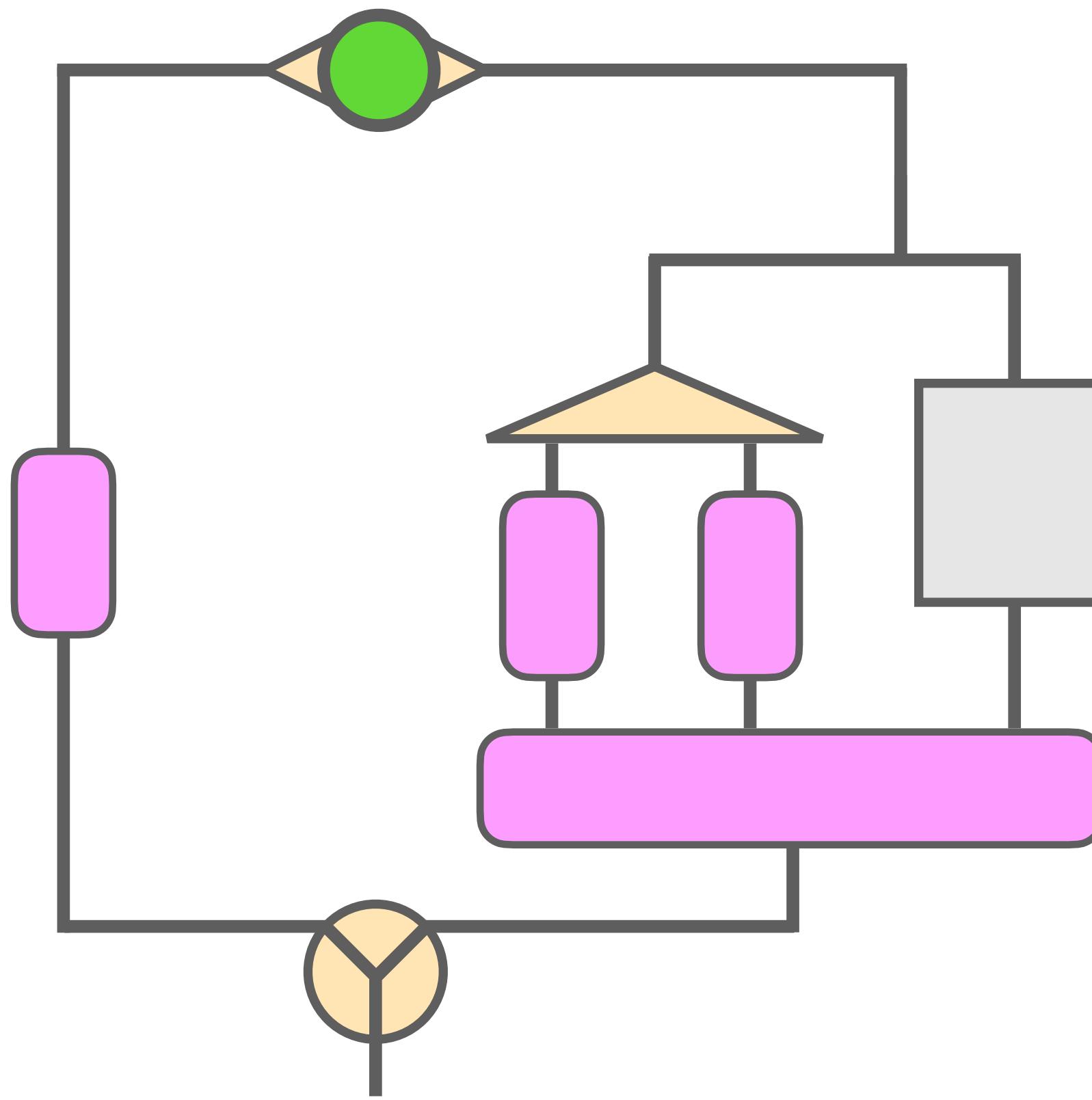
Durable Execution



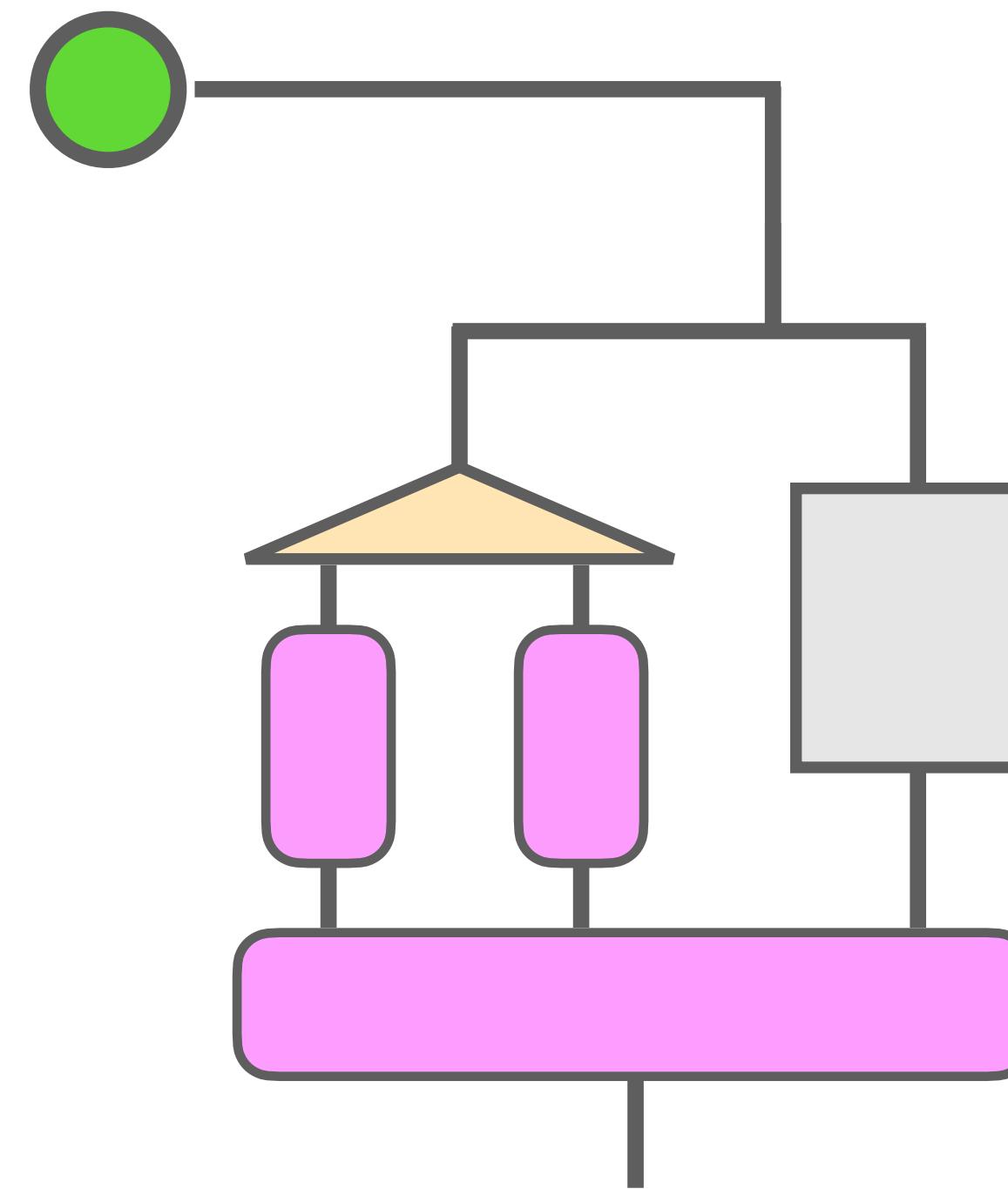
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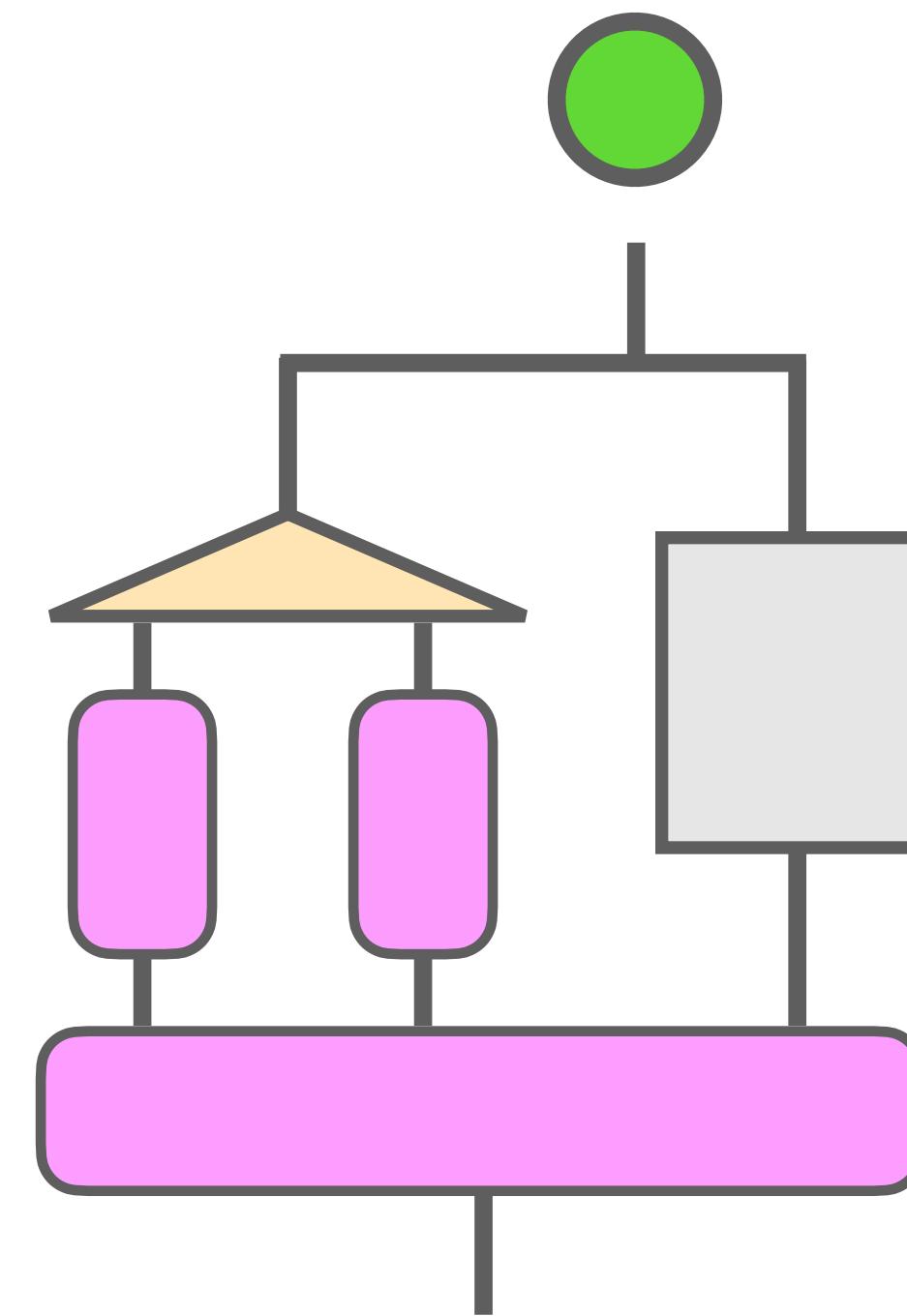
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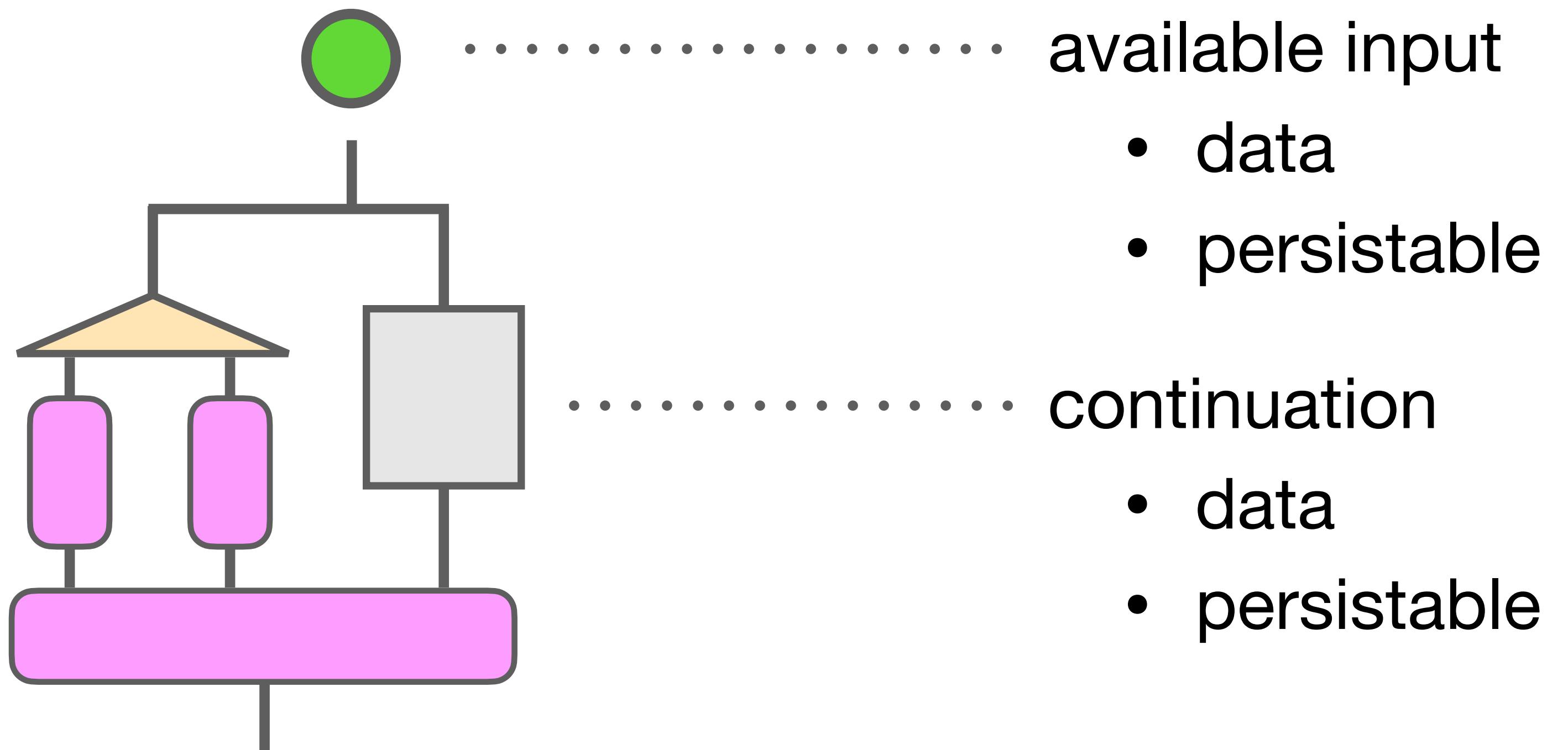
Durable Execution



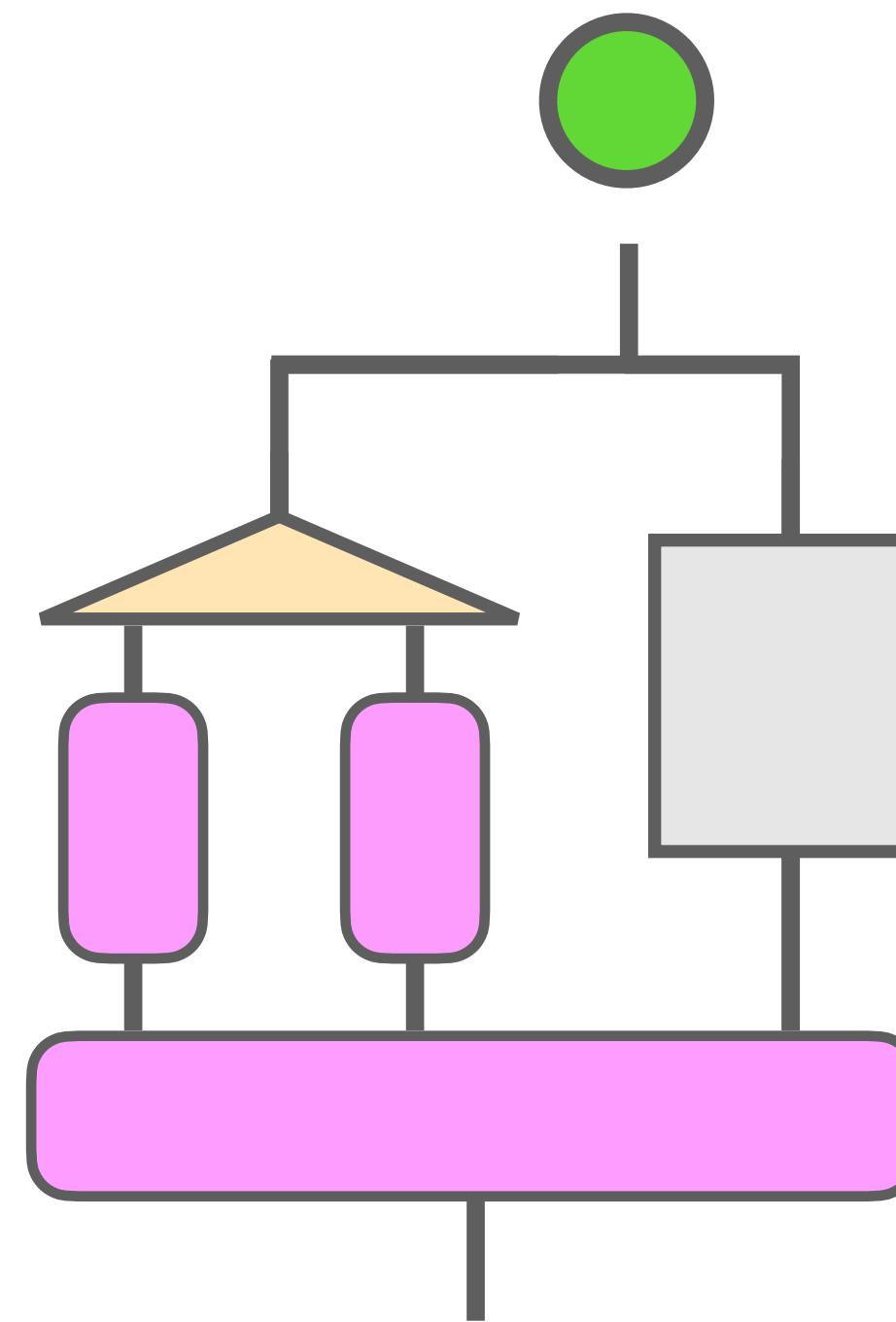
Durable Execution



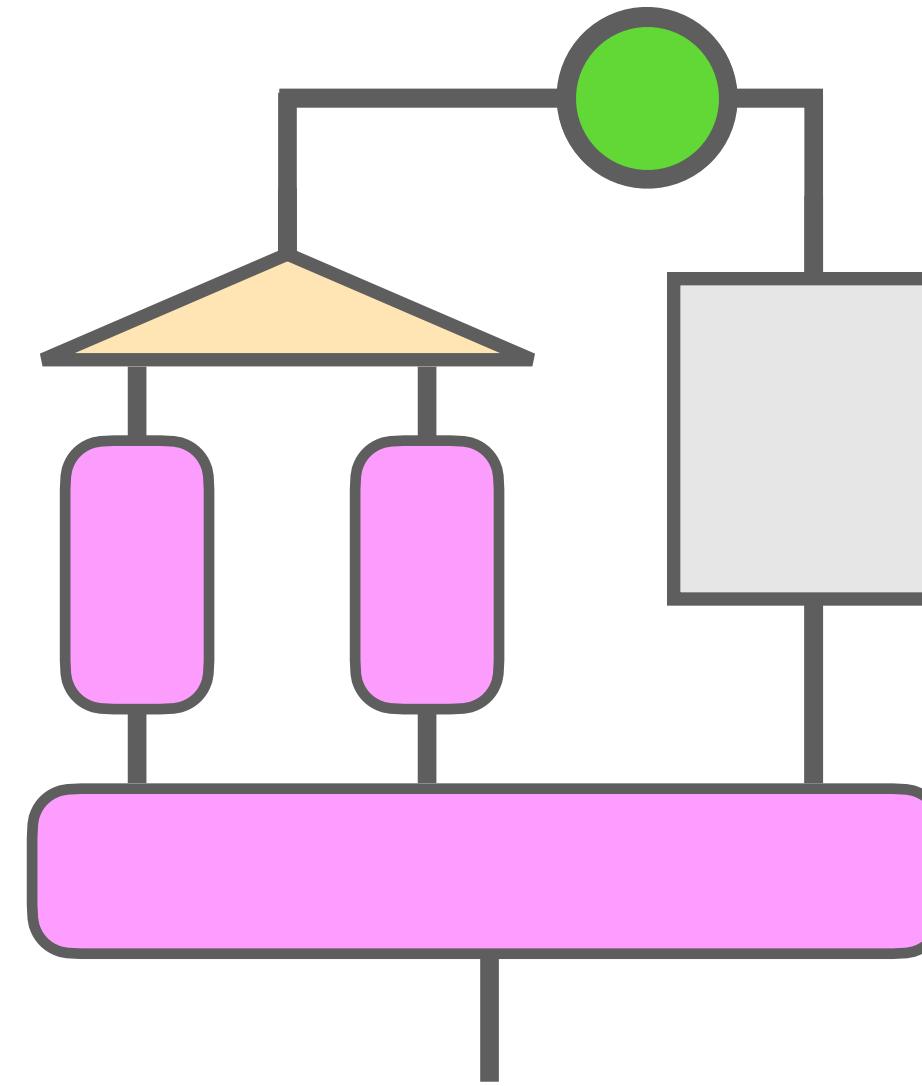
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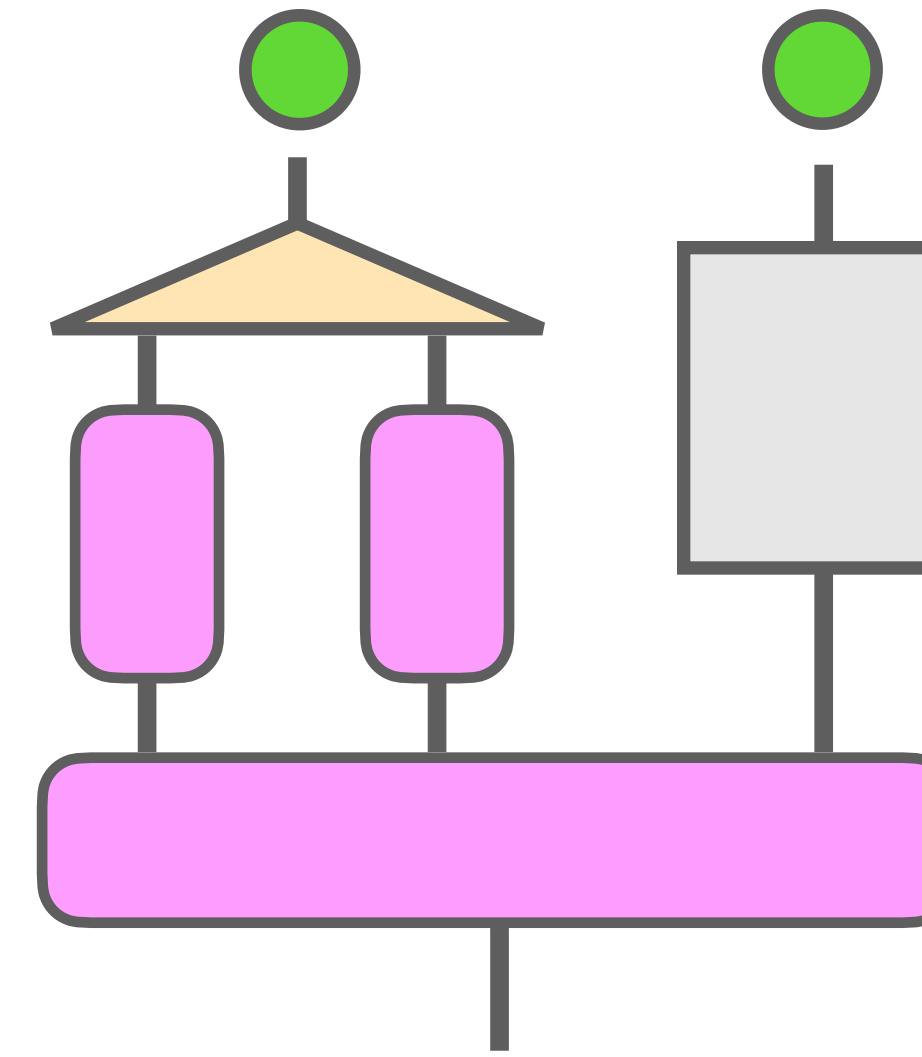
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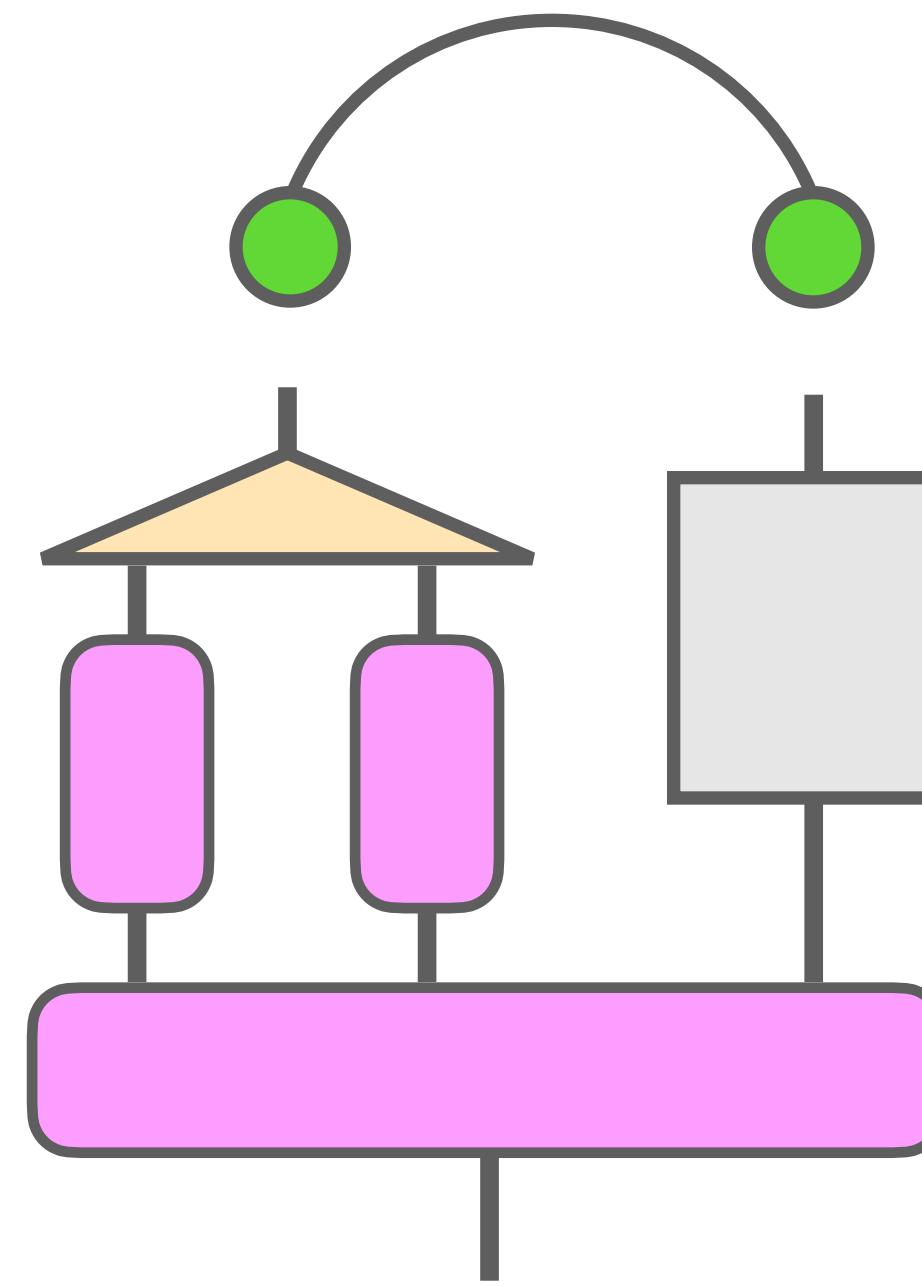
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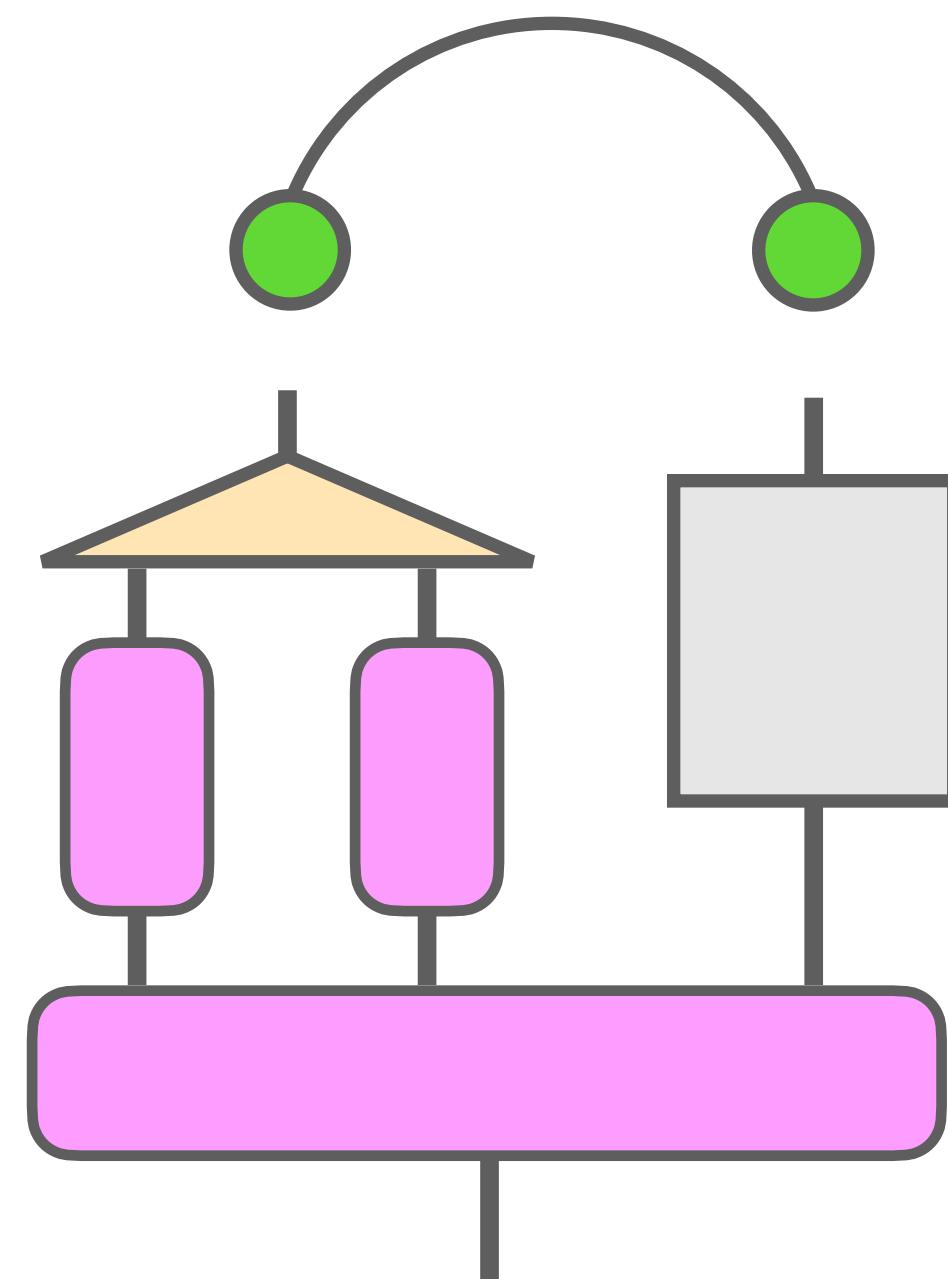
Durable Execution



Durable Execution

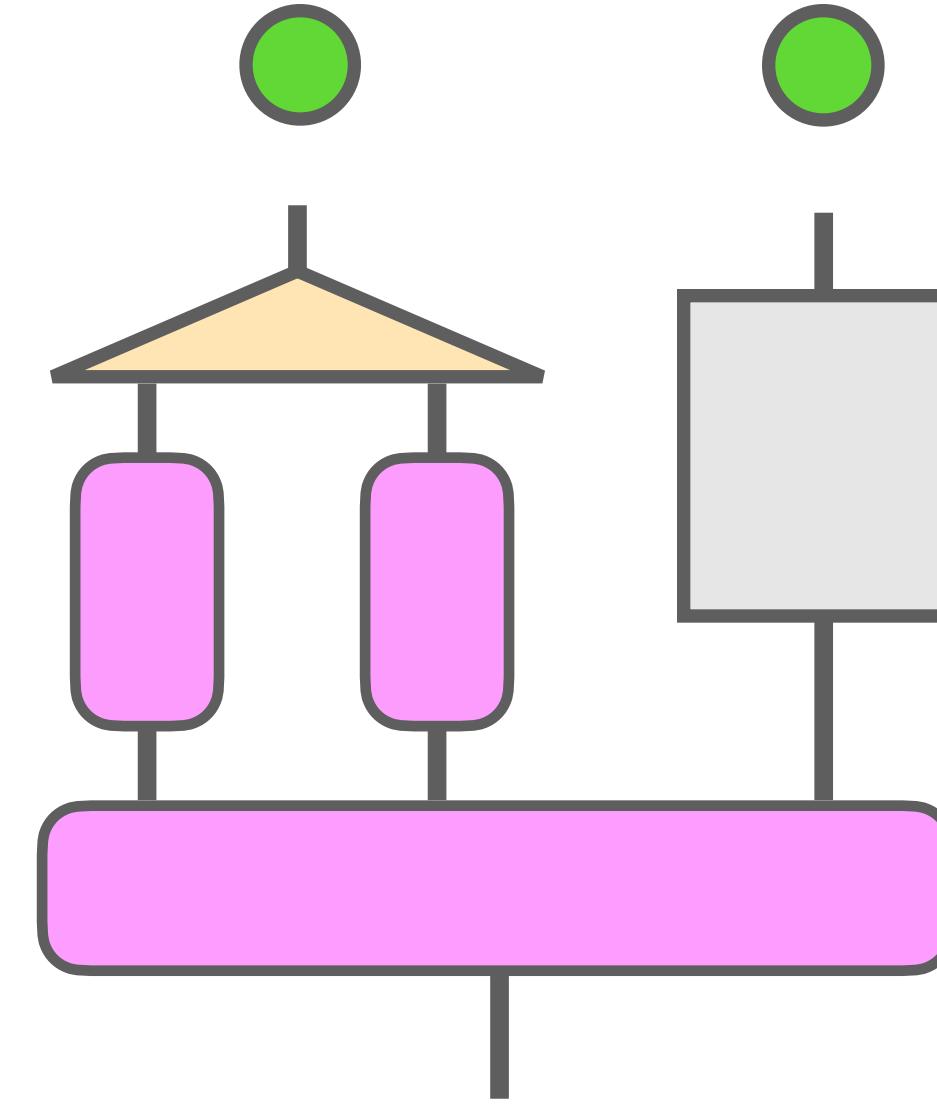


Durable Execution

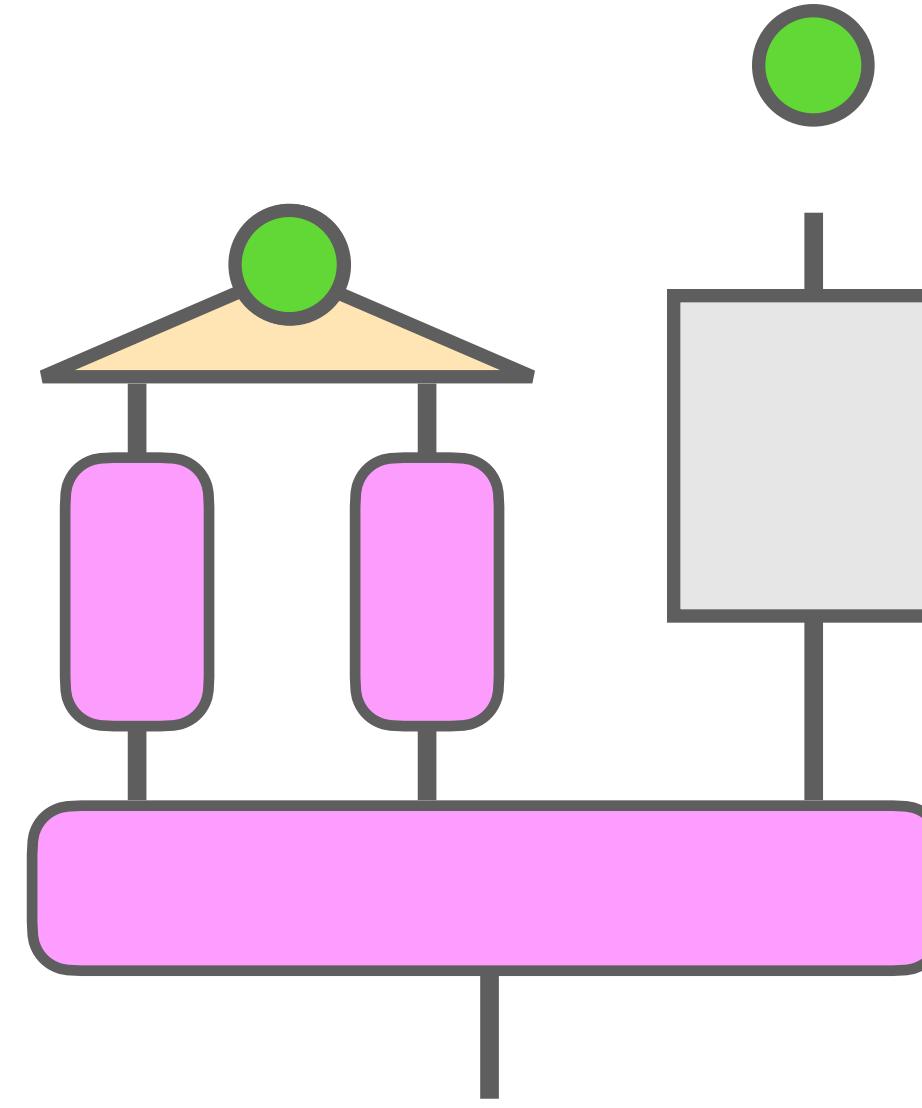


- available inputs
 - data
 - persistable
- continuation
 - data
 - persistable

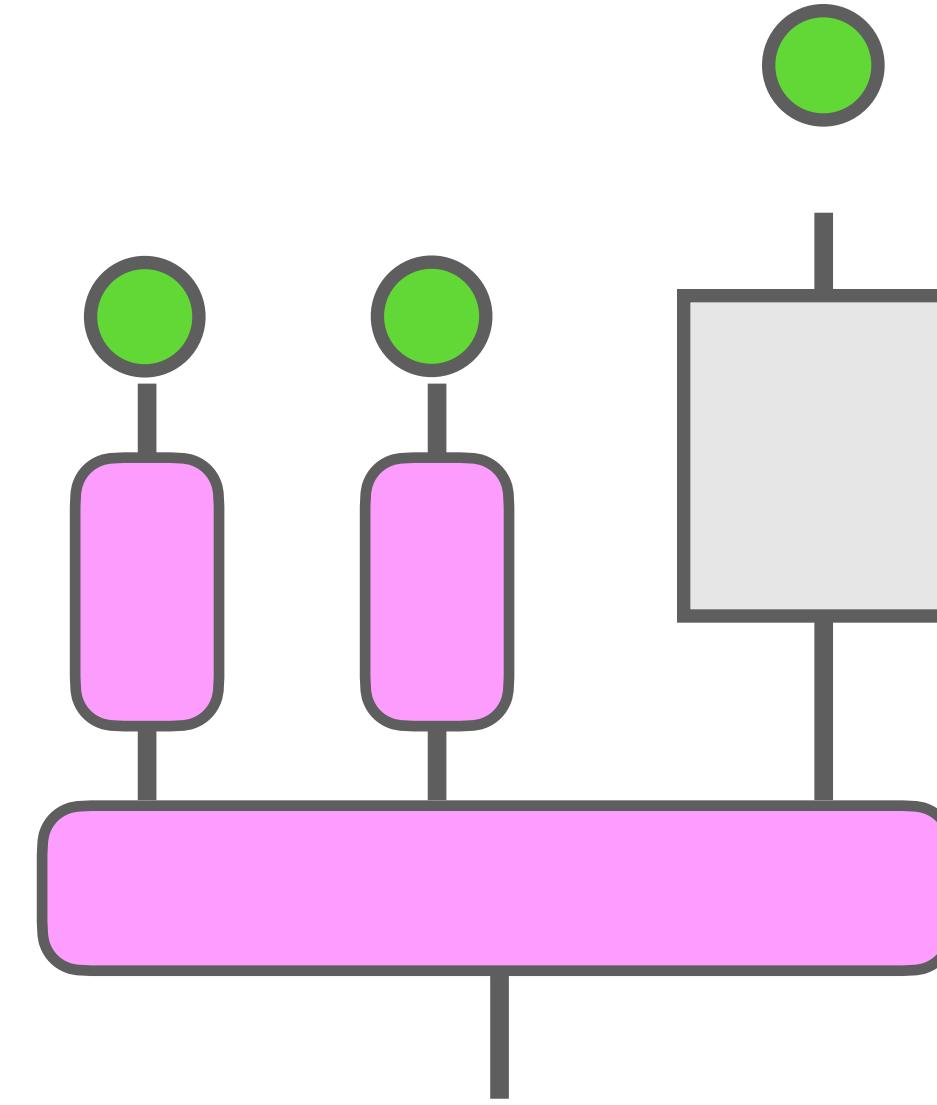
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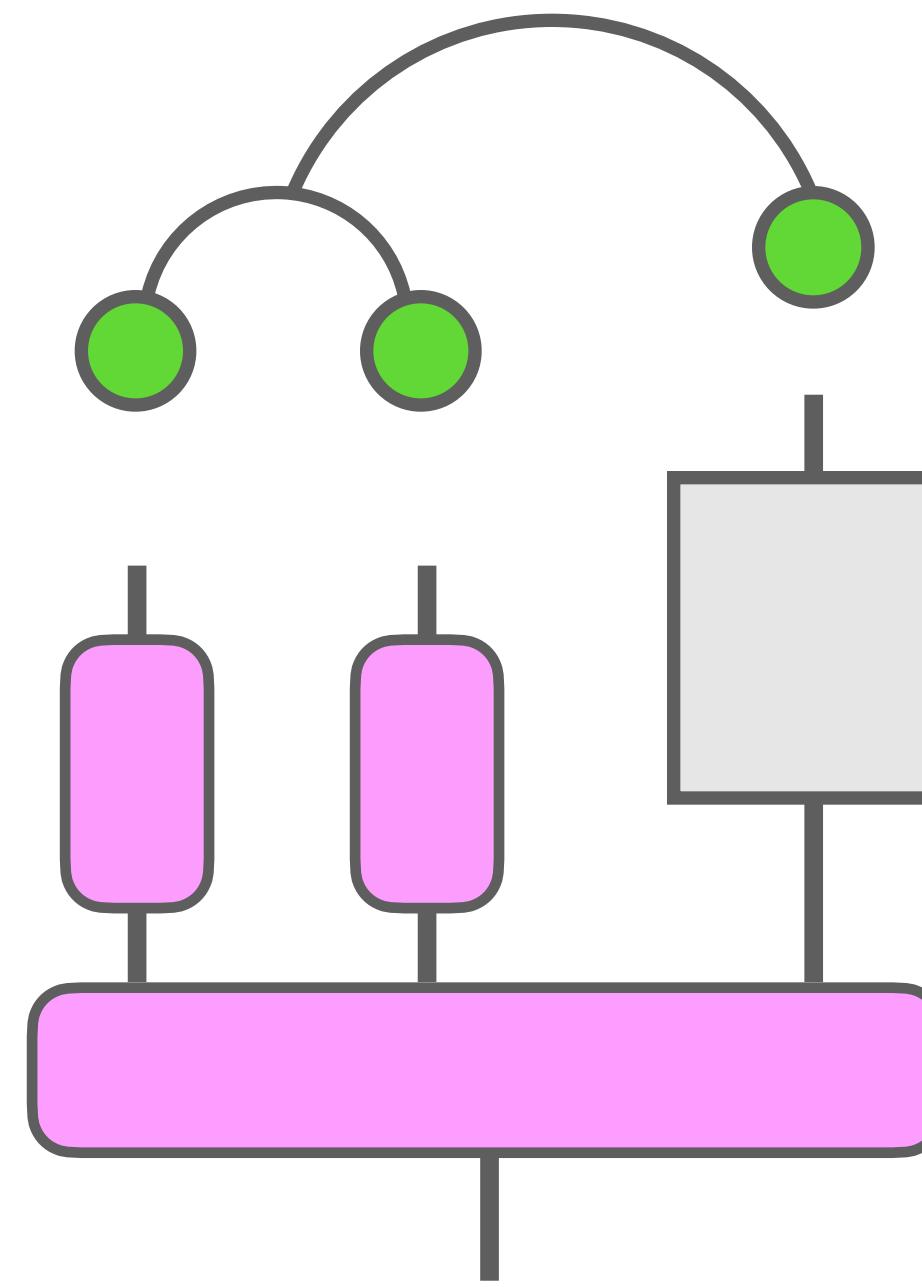
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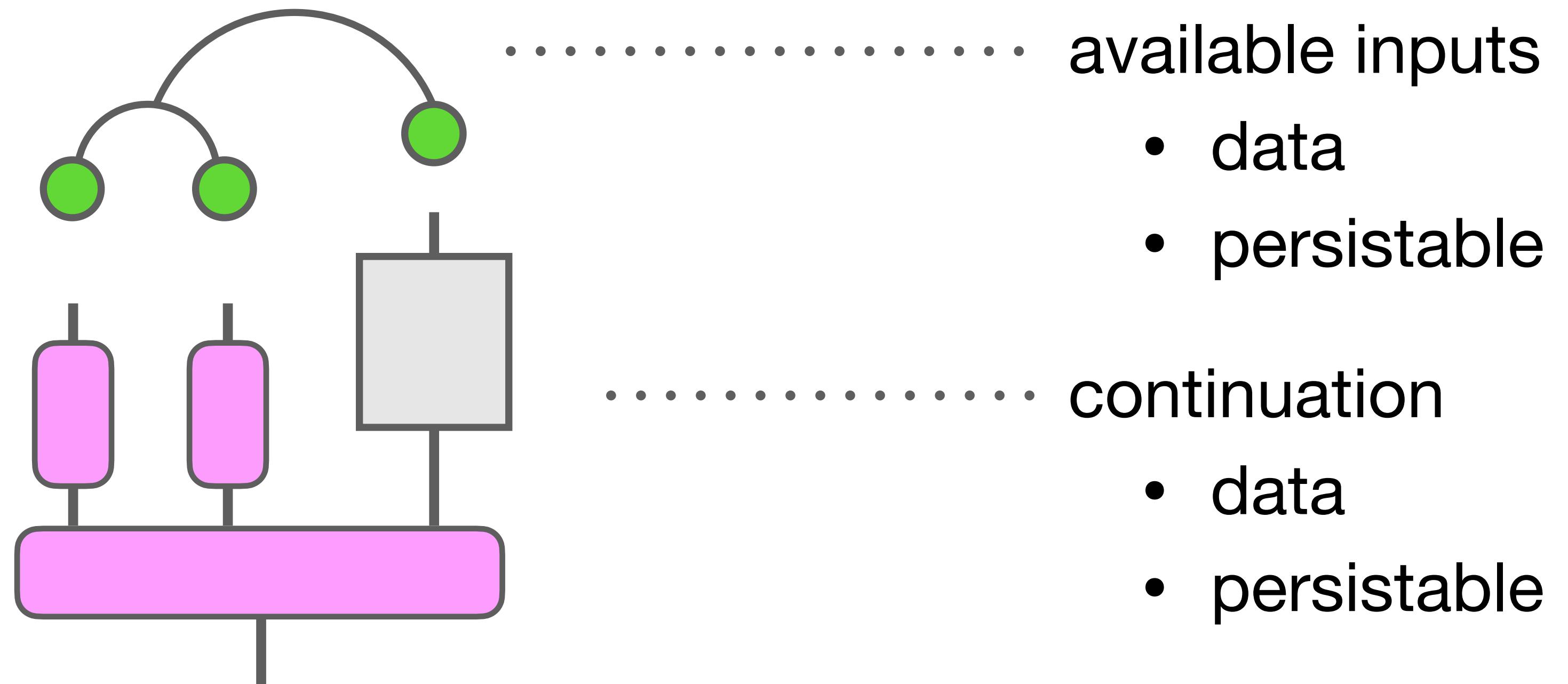
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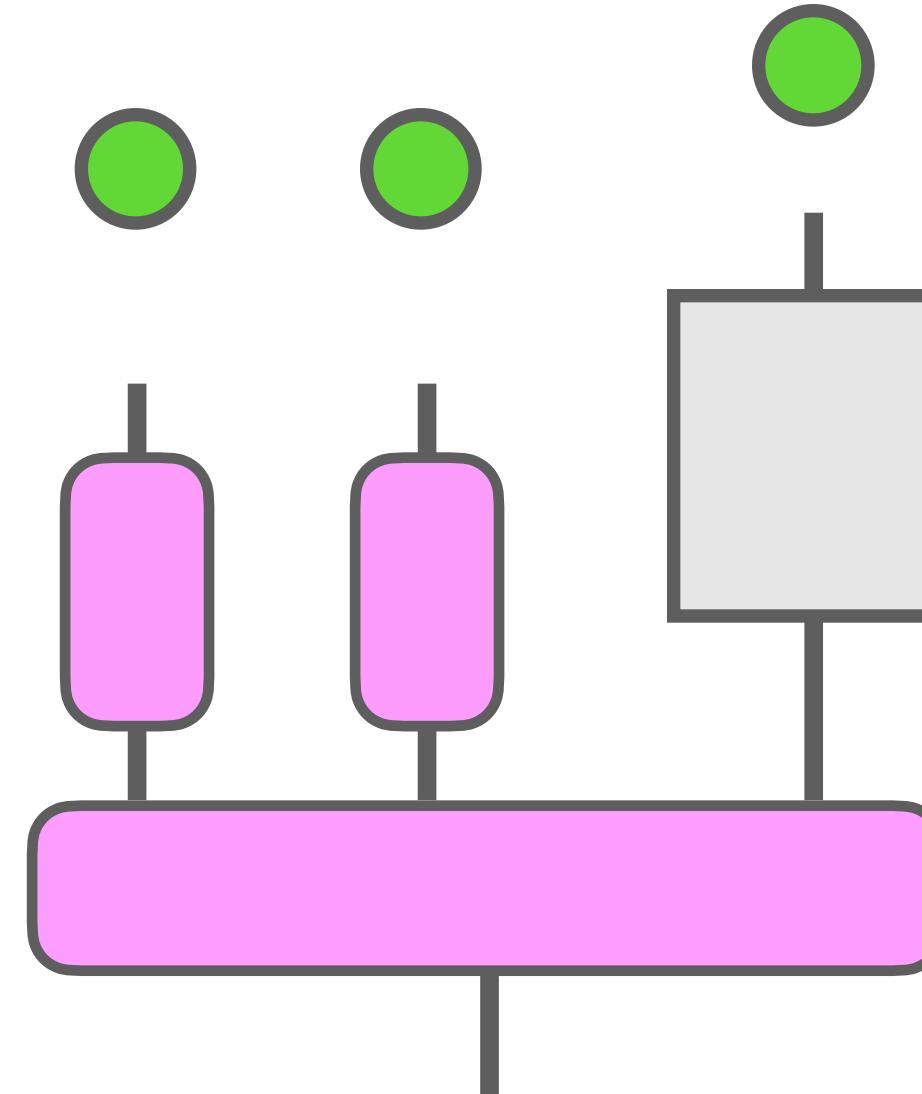
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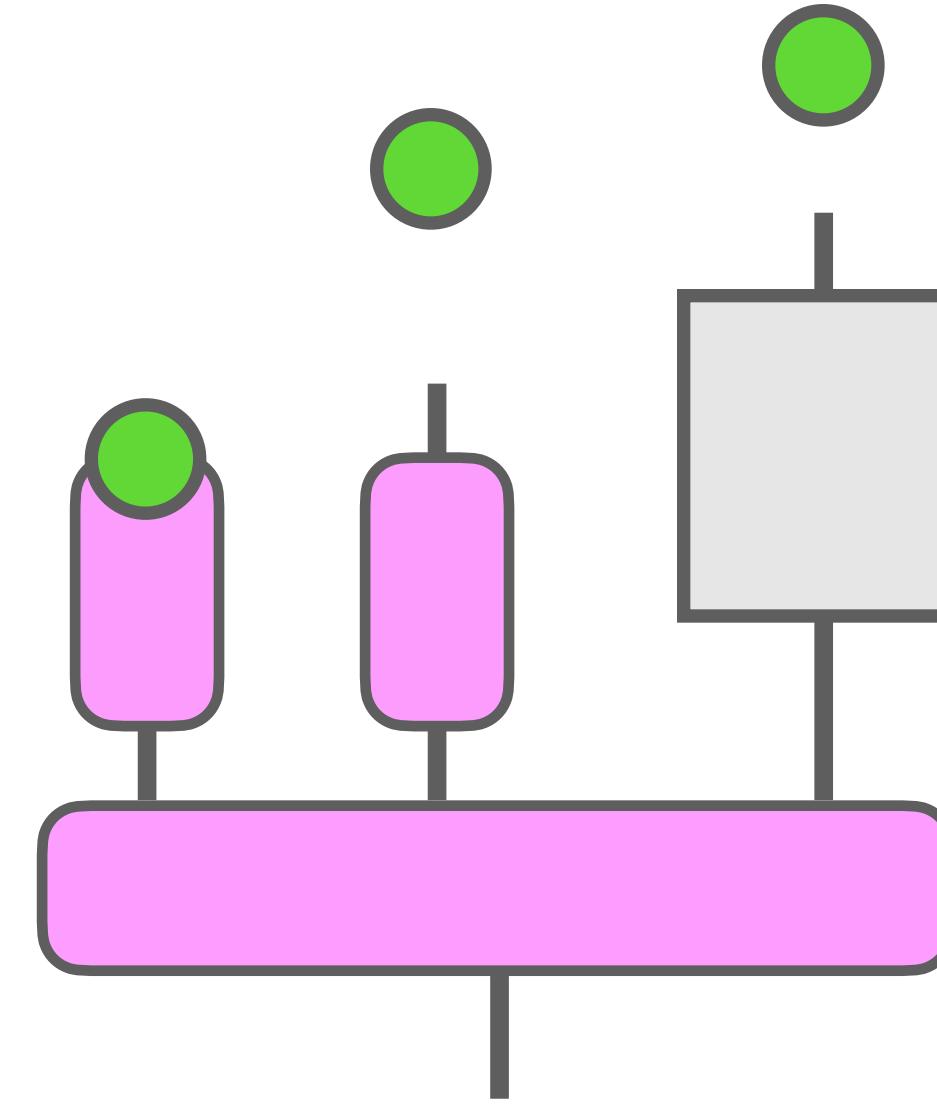
Durable Execution



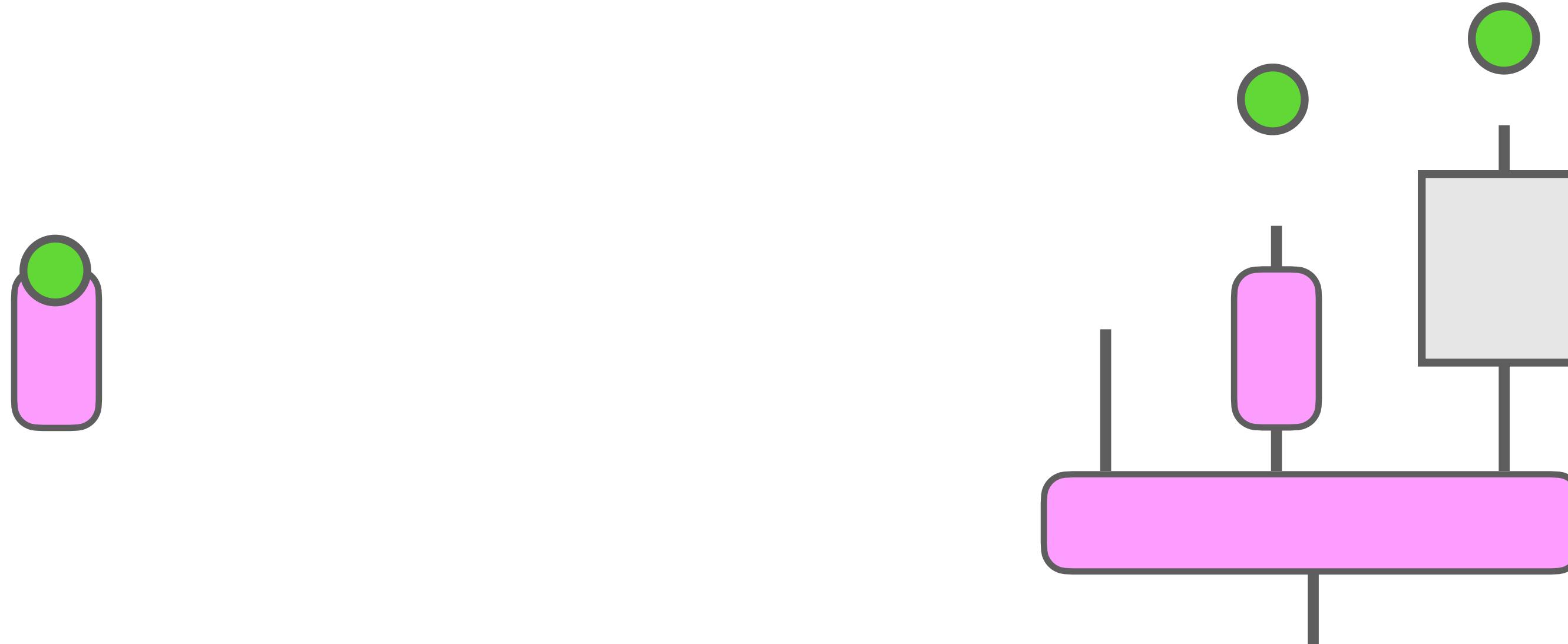
Durable Execution



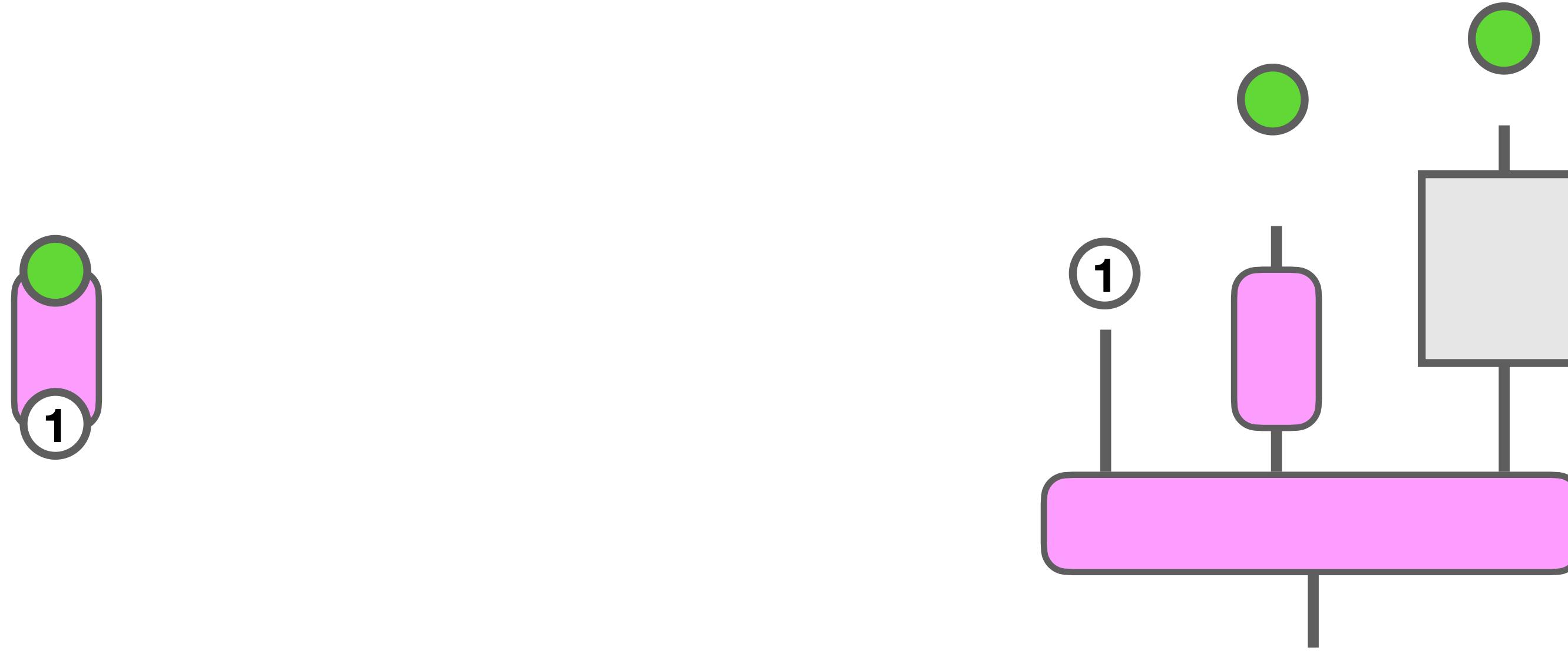
Durable Execution



Durable Execution

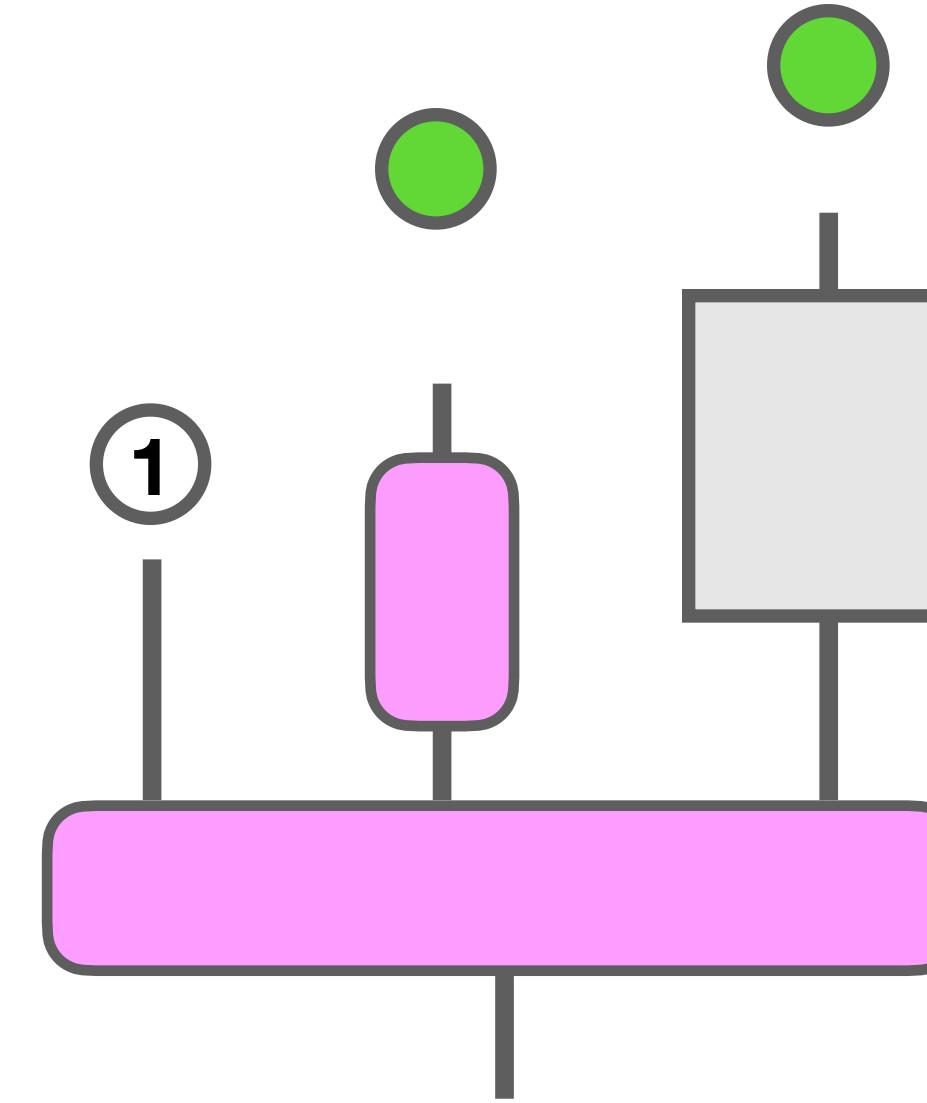
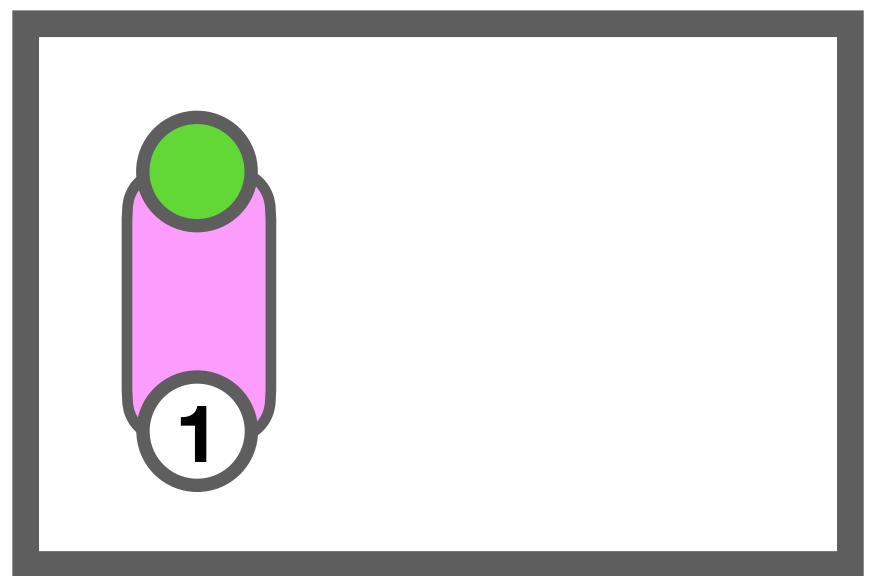


Durable Execution



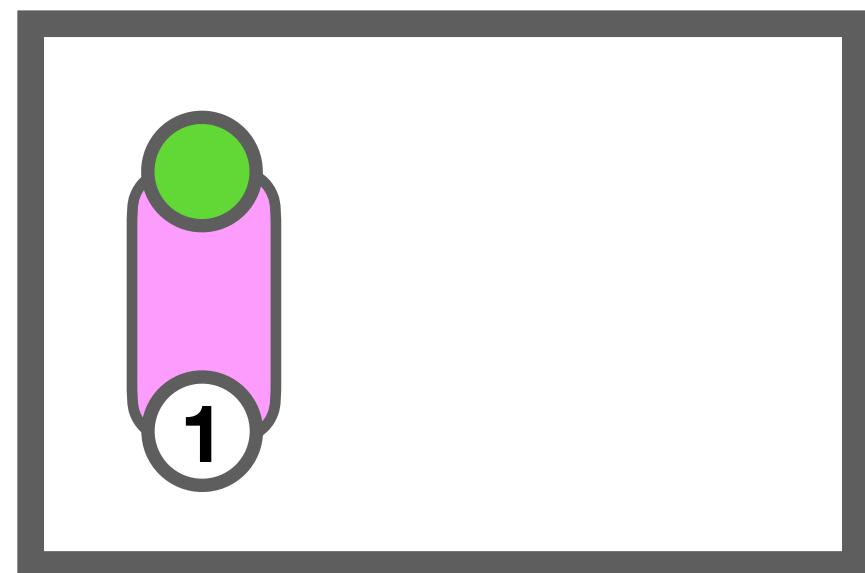
Durable Execution

In-progress
Activities

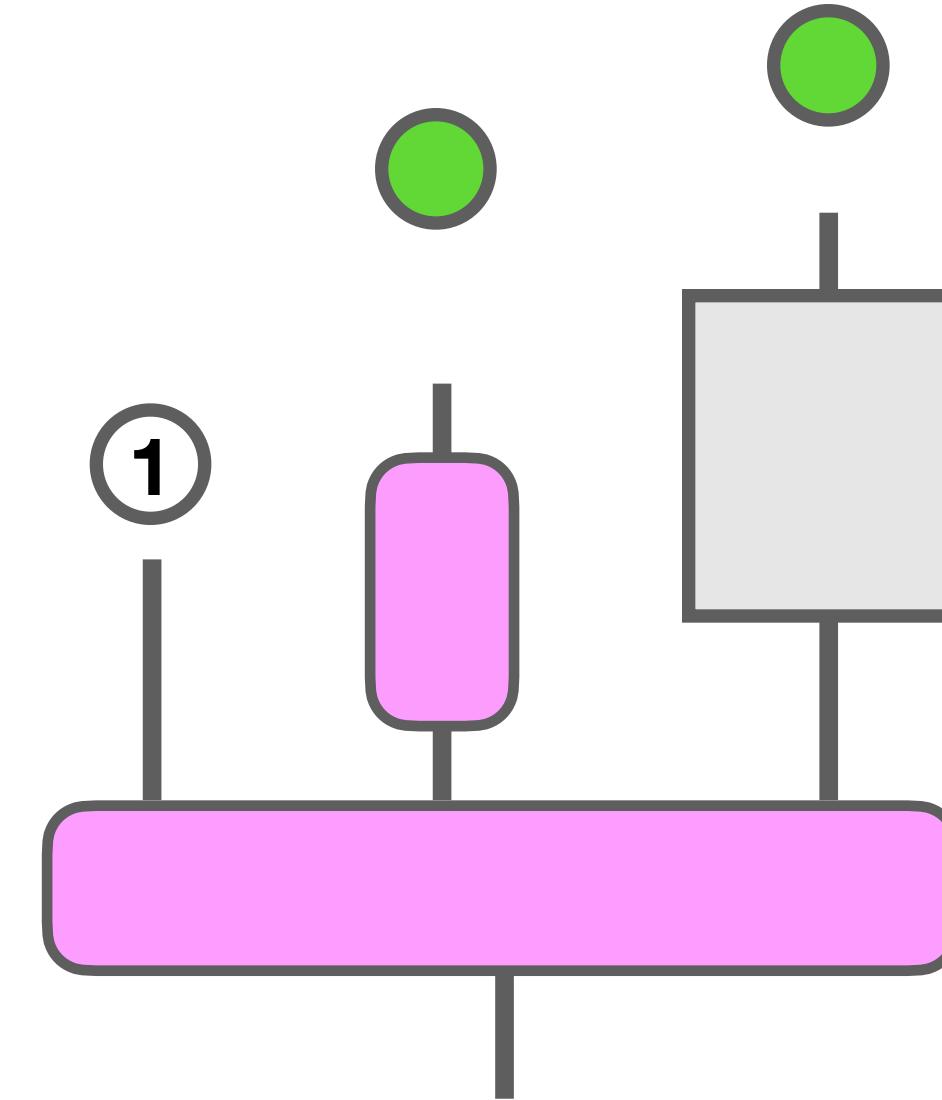


Durable Execution

In-progress
Activities

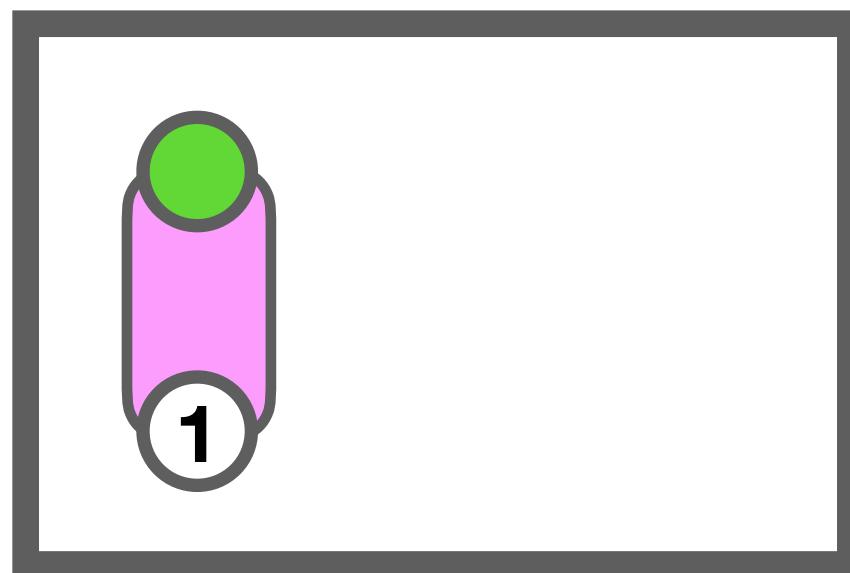


- persisted recipes
- restartable

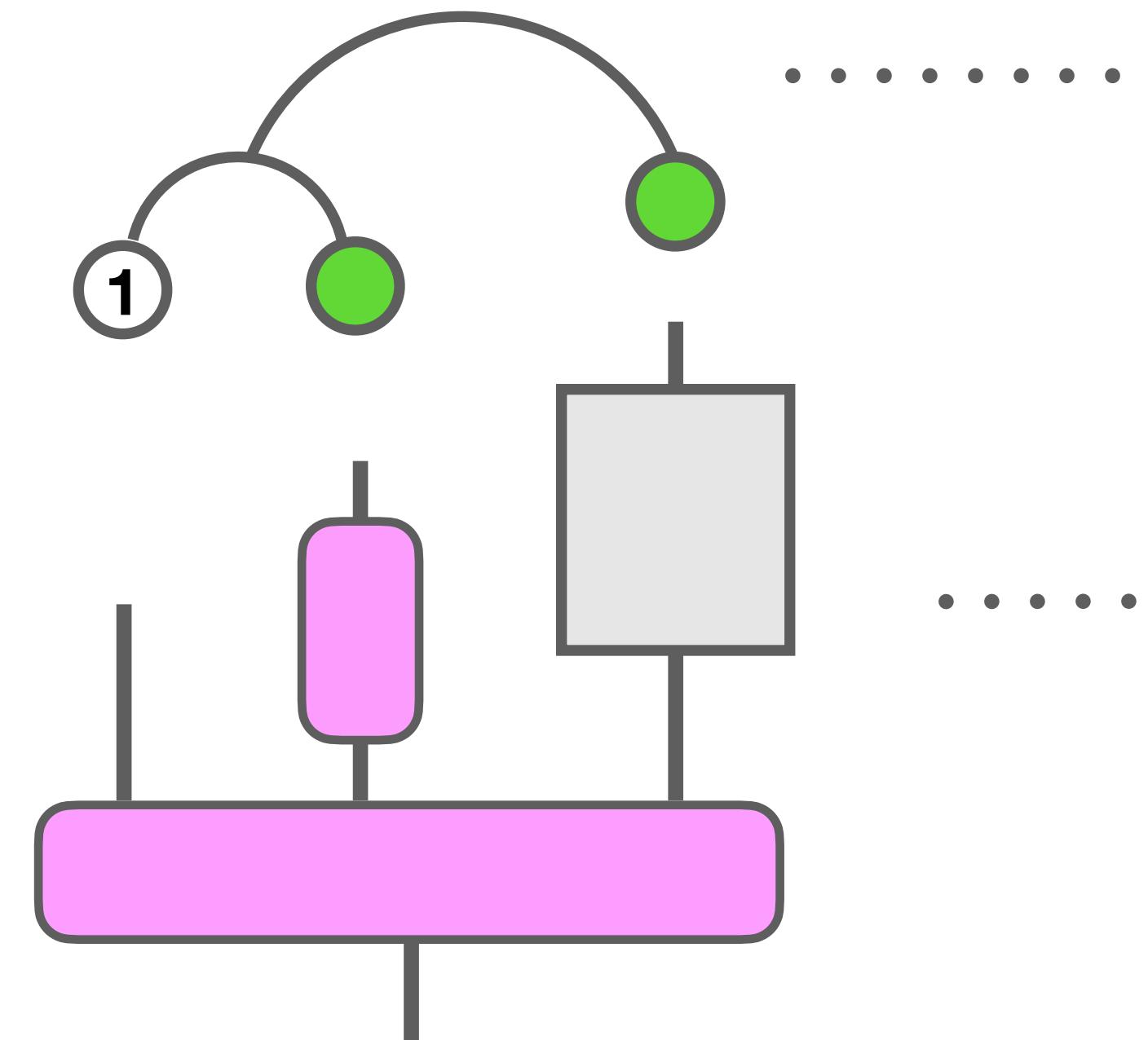


Durable Execution

In-progress Activities



- persisted recipes
- restartable



inputs

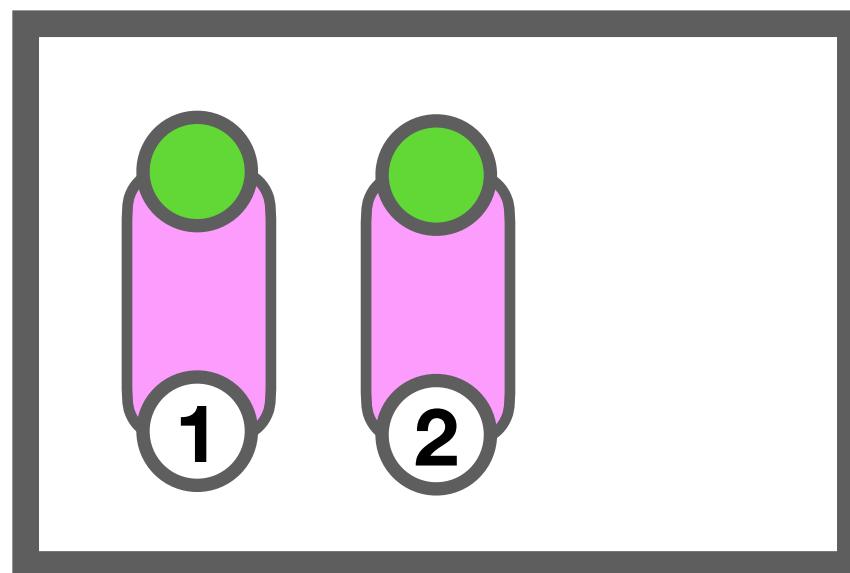
- available or *promised*
- persistable

continuation

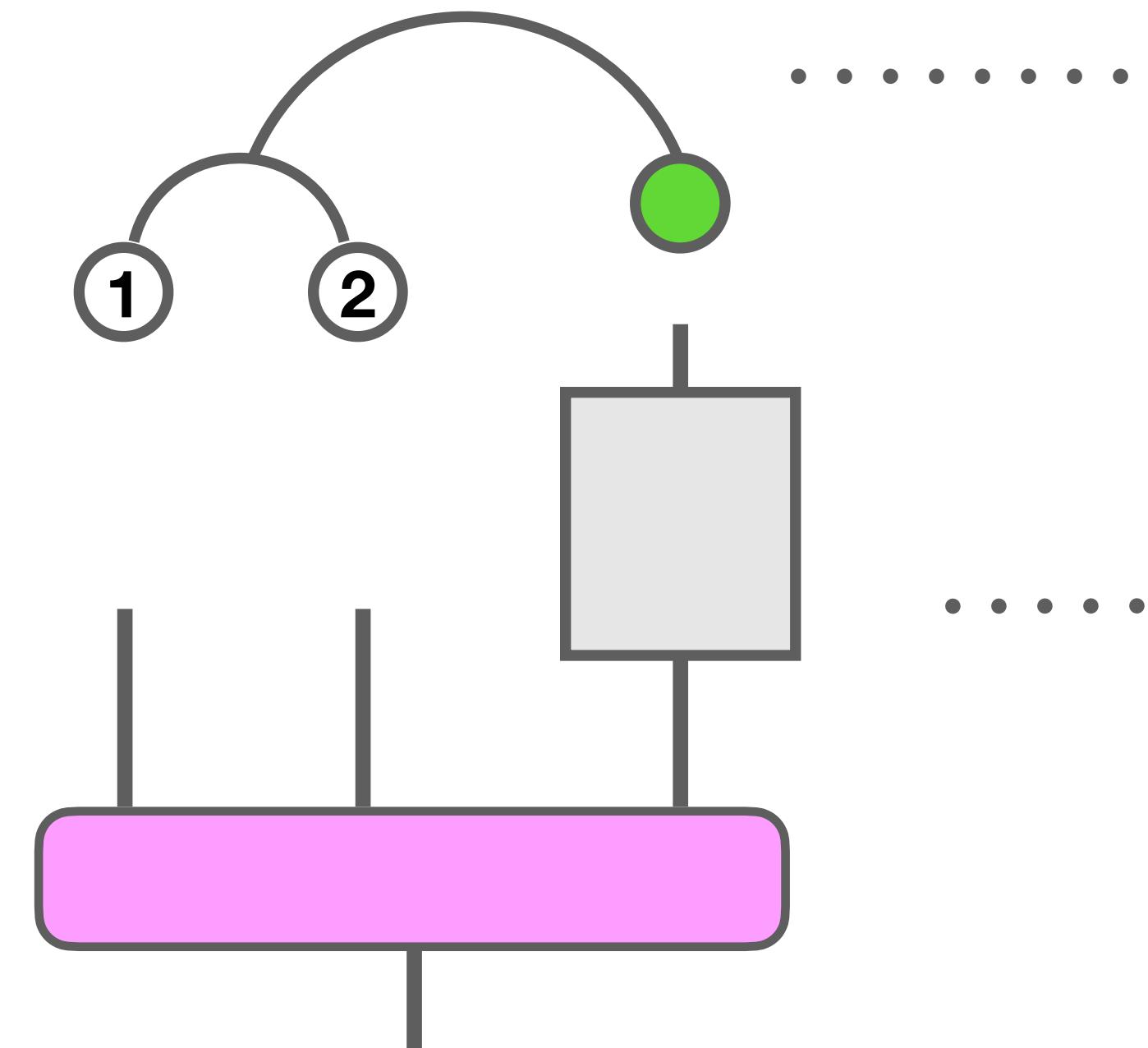
- data
- persistable

Durable Execution

In-progress Activities



- persisted recipes
- restartable



inputs

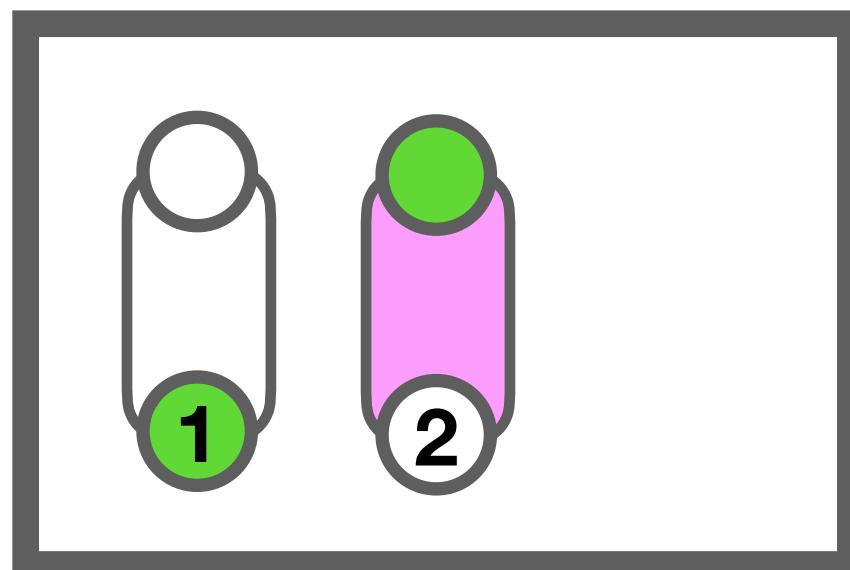
- available or *promised*
- persistable

continuation

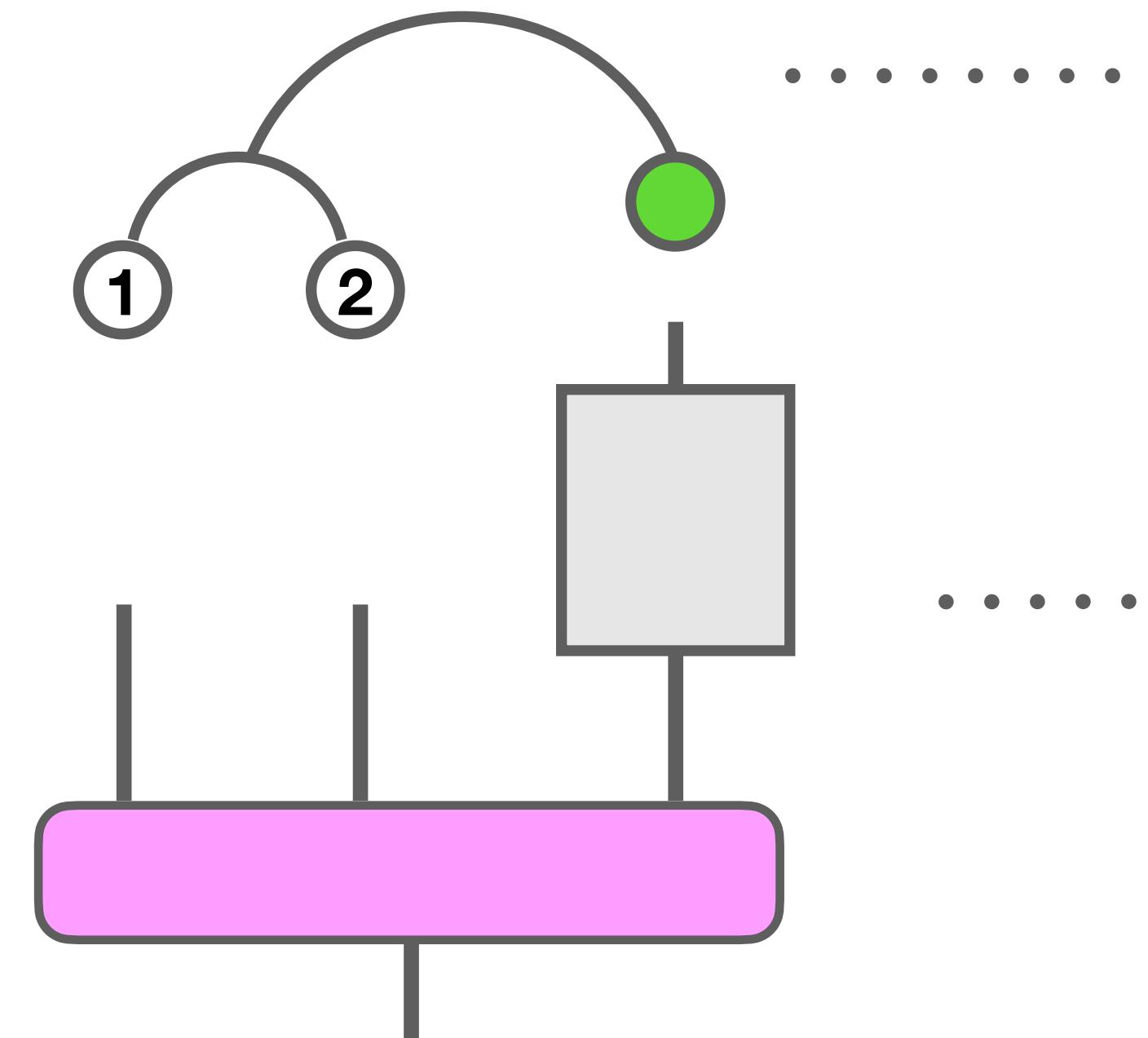
- data
- persistable

Durable Execution

In-progress Activities



- persisted recipes
- restartable



inputs

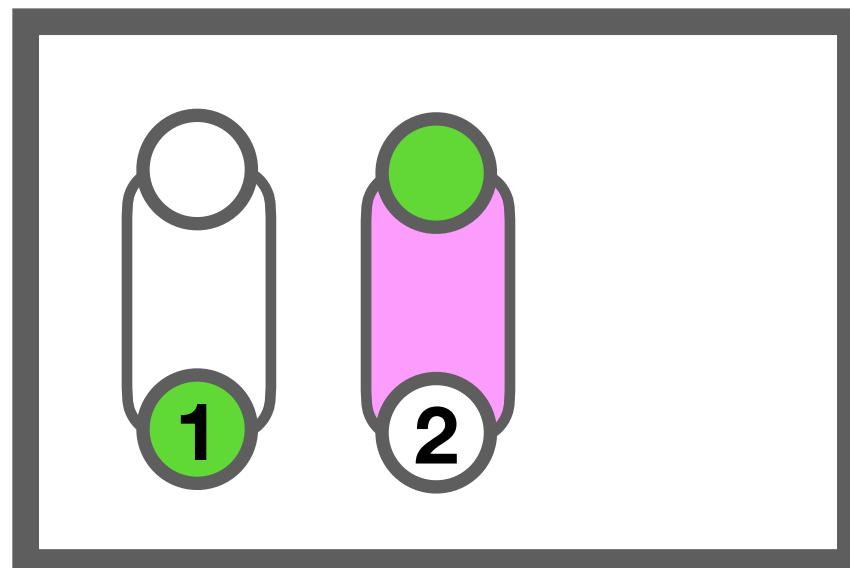
- available or *promised*
- persistable

continuation

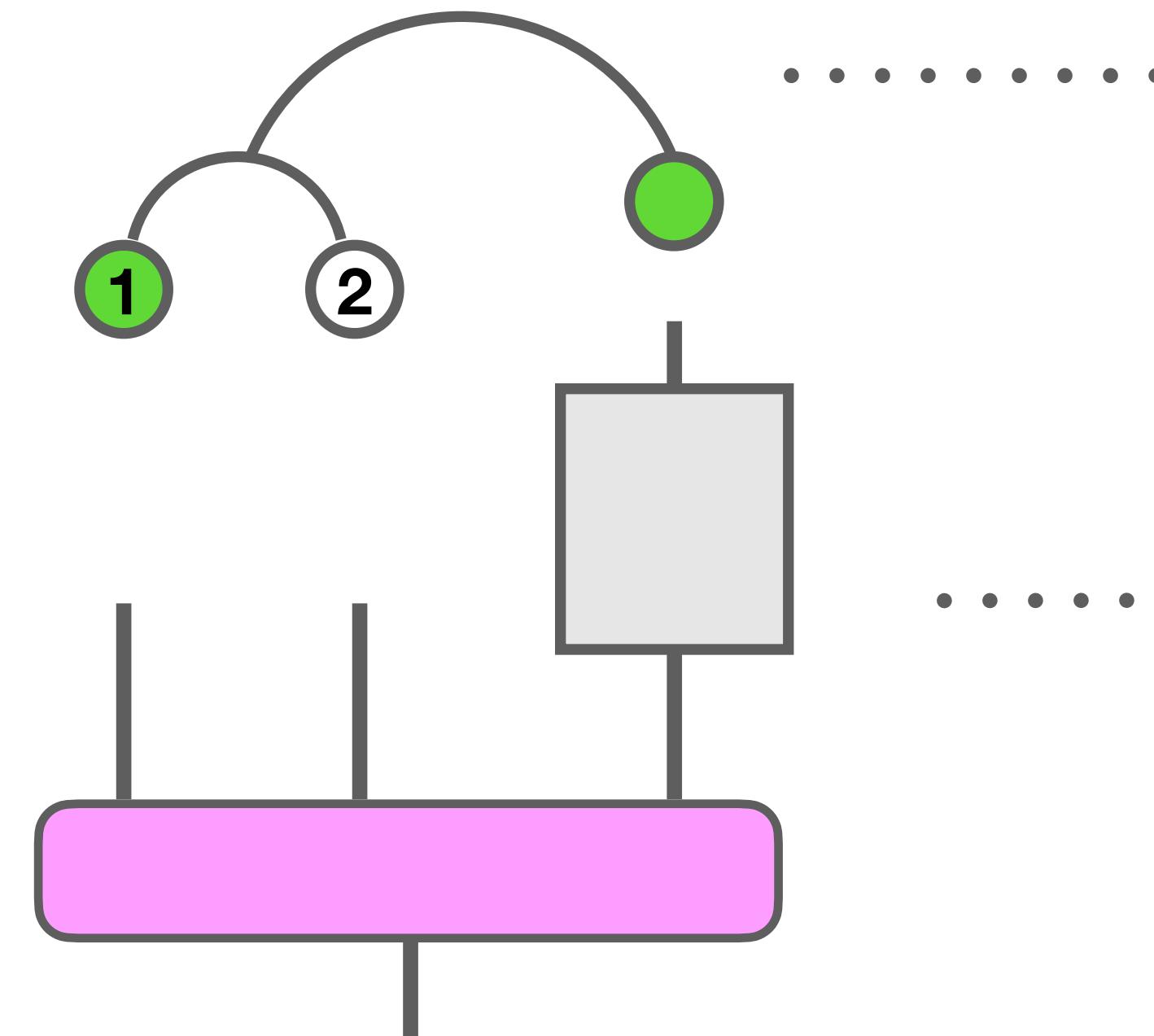
- data
- persistable

Durable Execution

In-progress Activities



- persisted recipes
- restartable



inputs

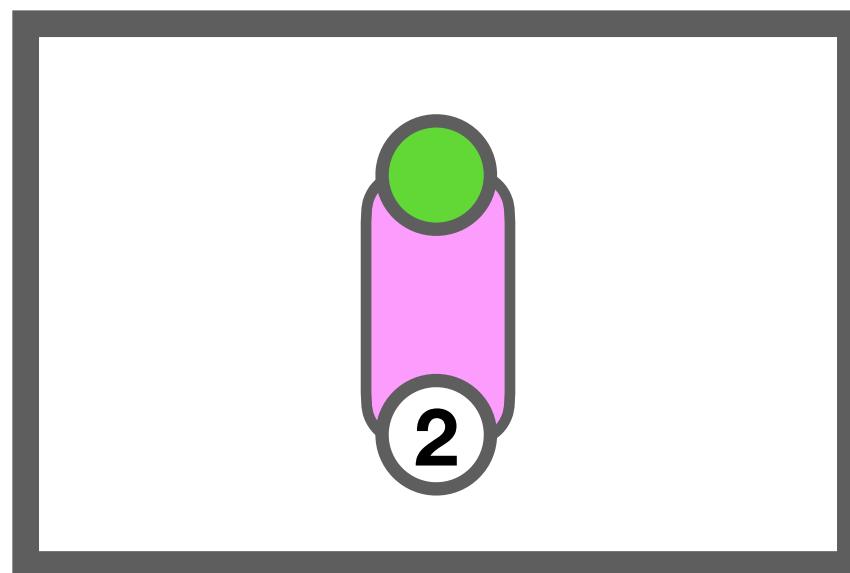
- available or *promised*
- persistable

continuation

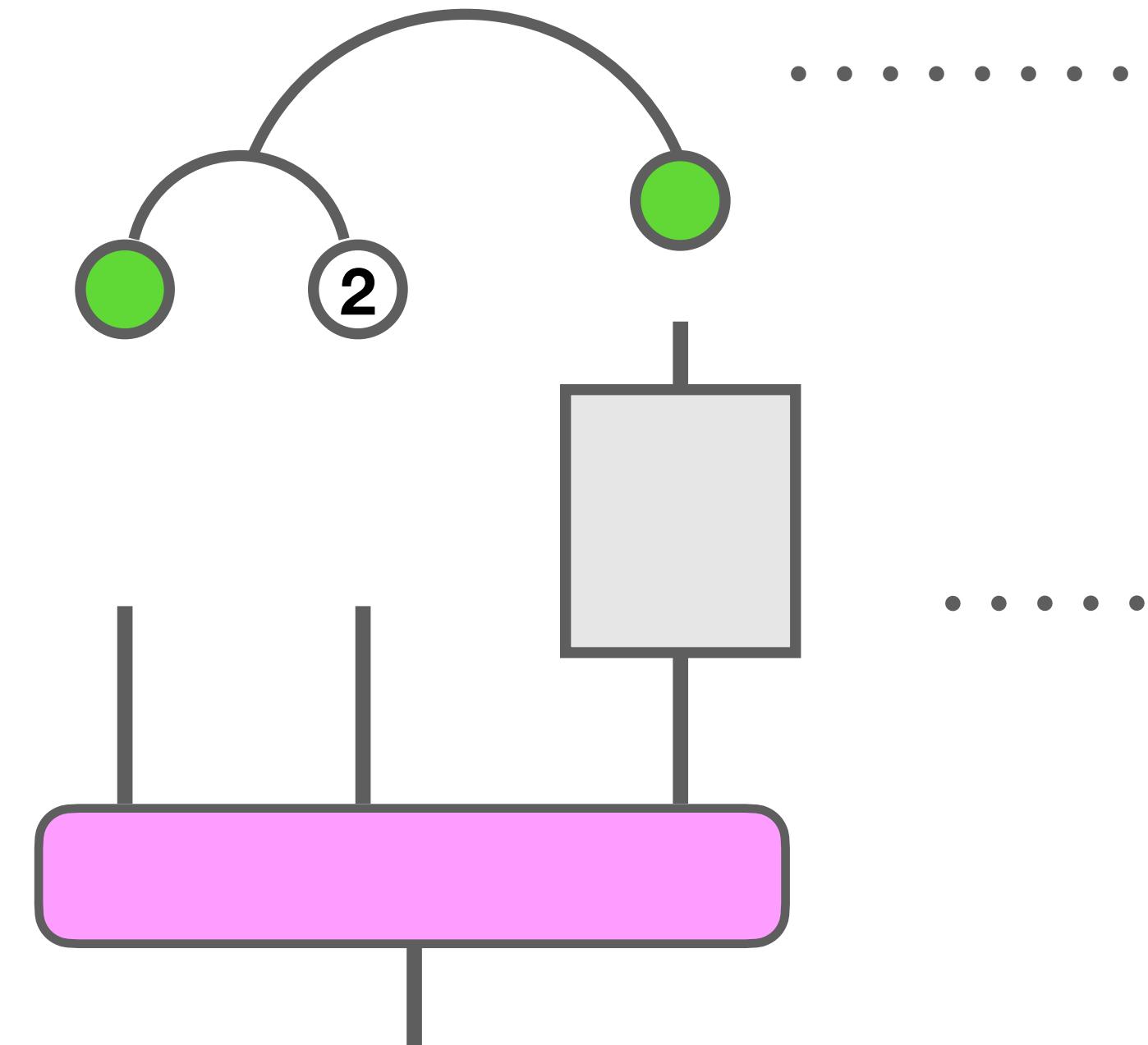
- data
- persistable

Durable Execution

In-progress Activities



- persisted recipes
- restartable



inputs

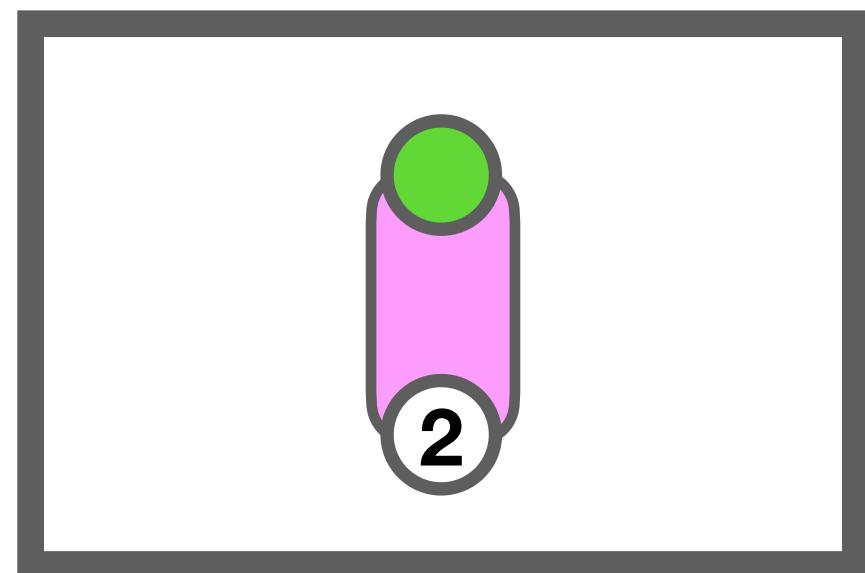
- available or *promised*
- persistable

continuation

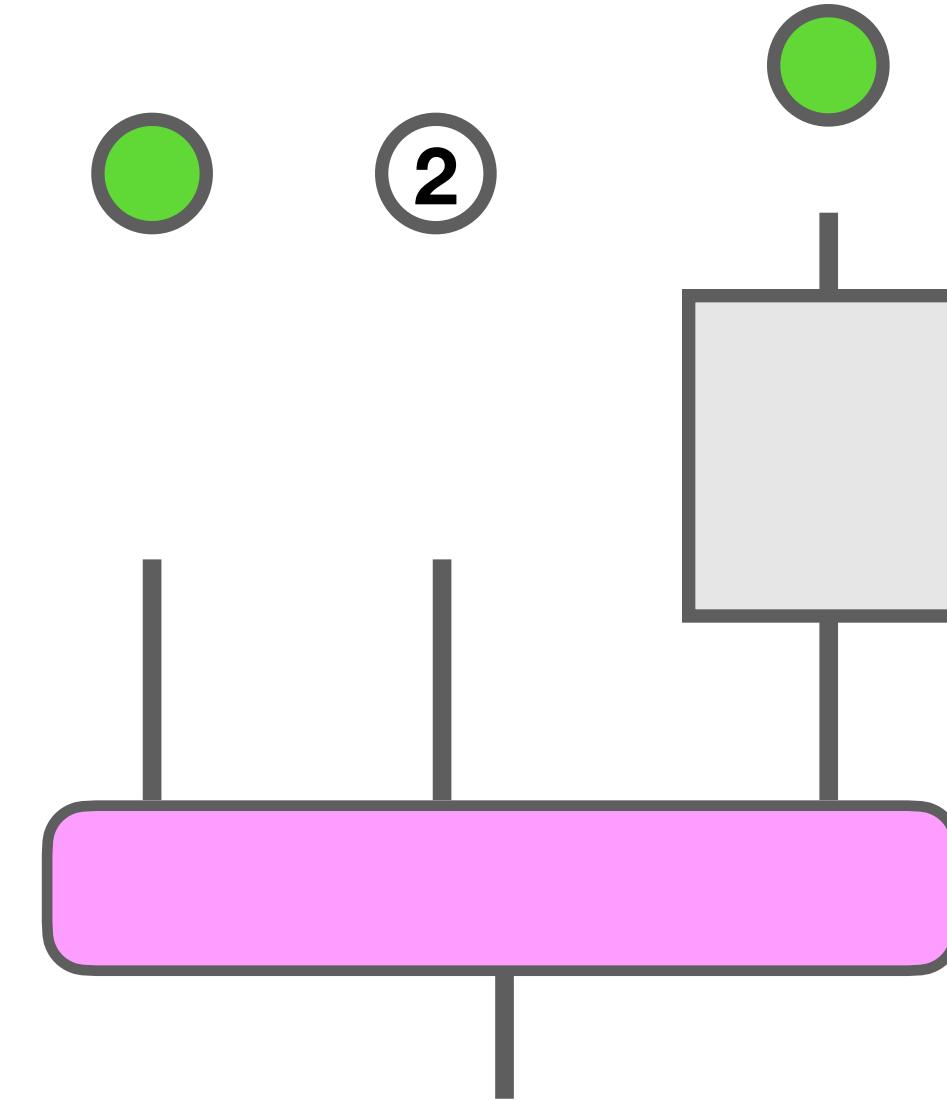
- data
- persistable

Durable Execution

In-progress
Activities

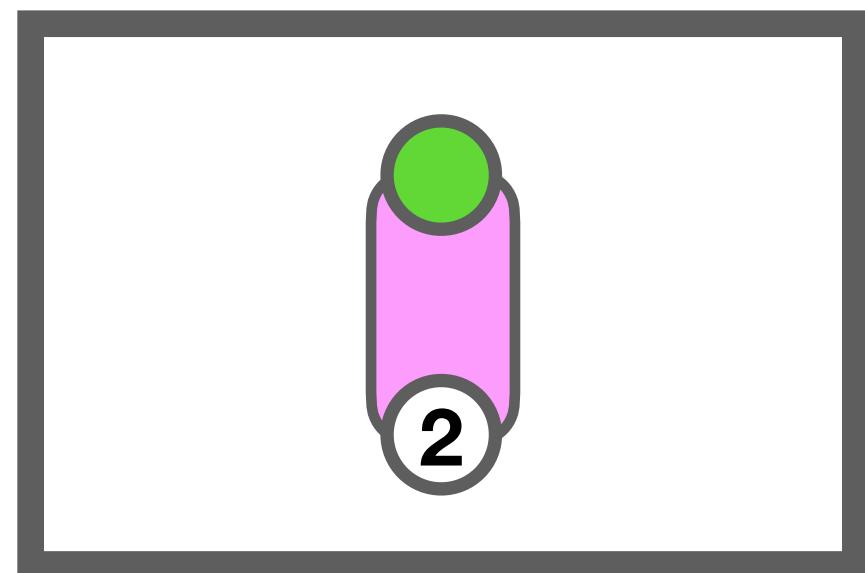


- persisted recipes
- restartable

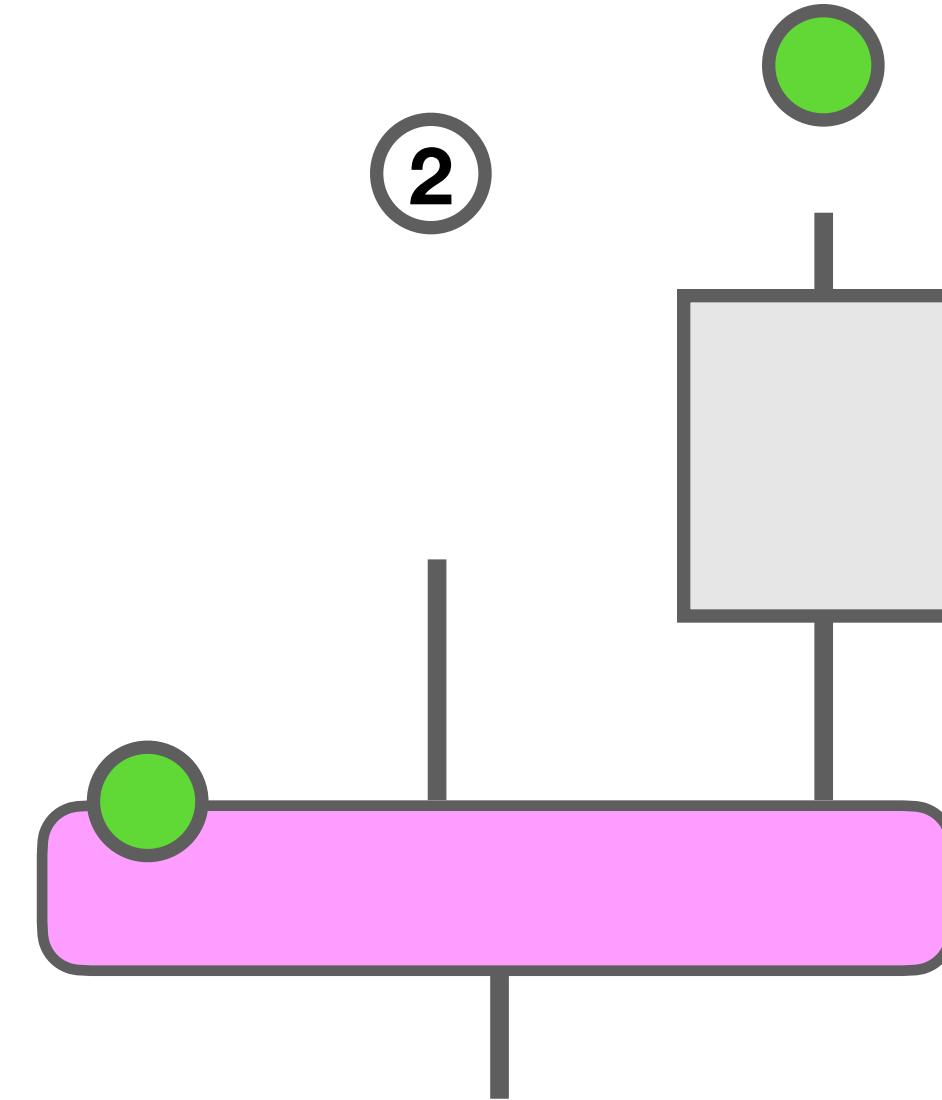


Durable Execution

In-progress
Activities

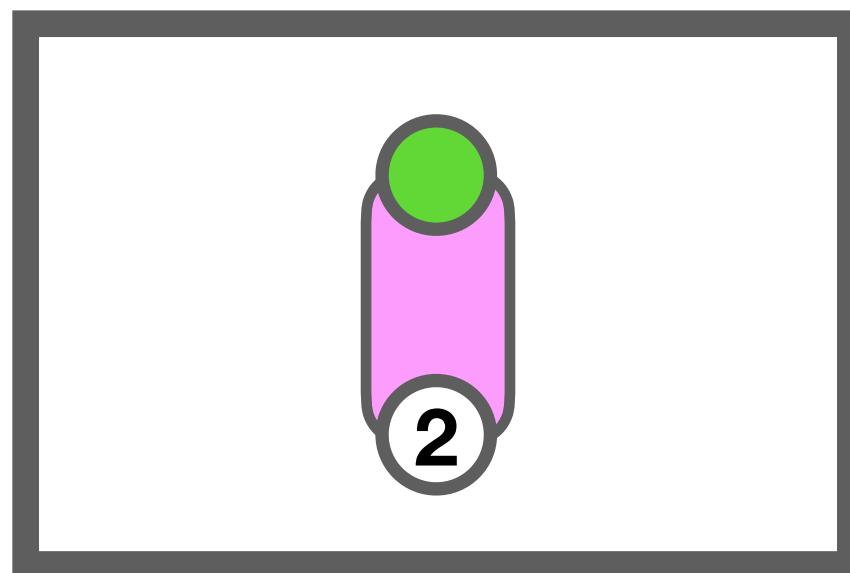


- persisted recipes
- restartable

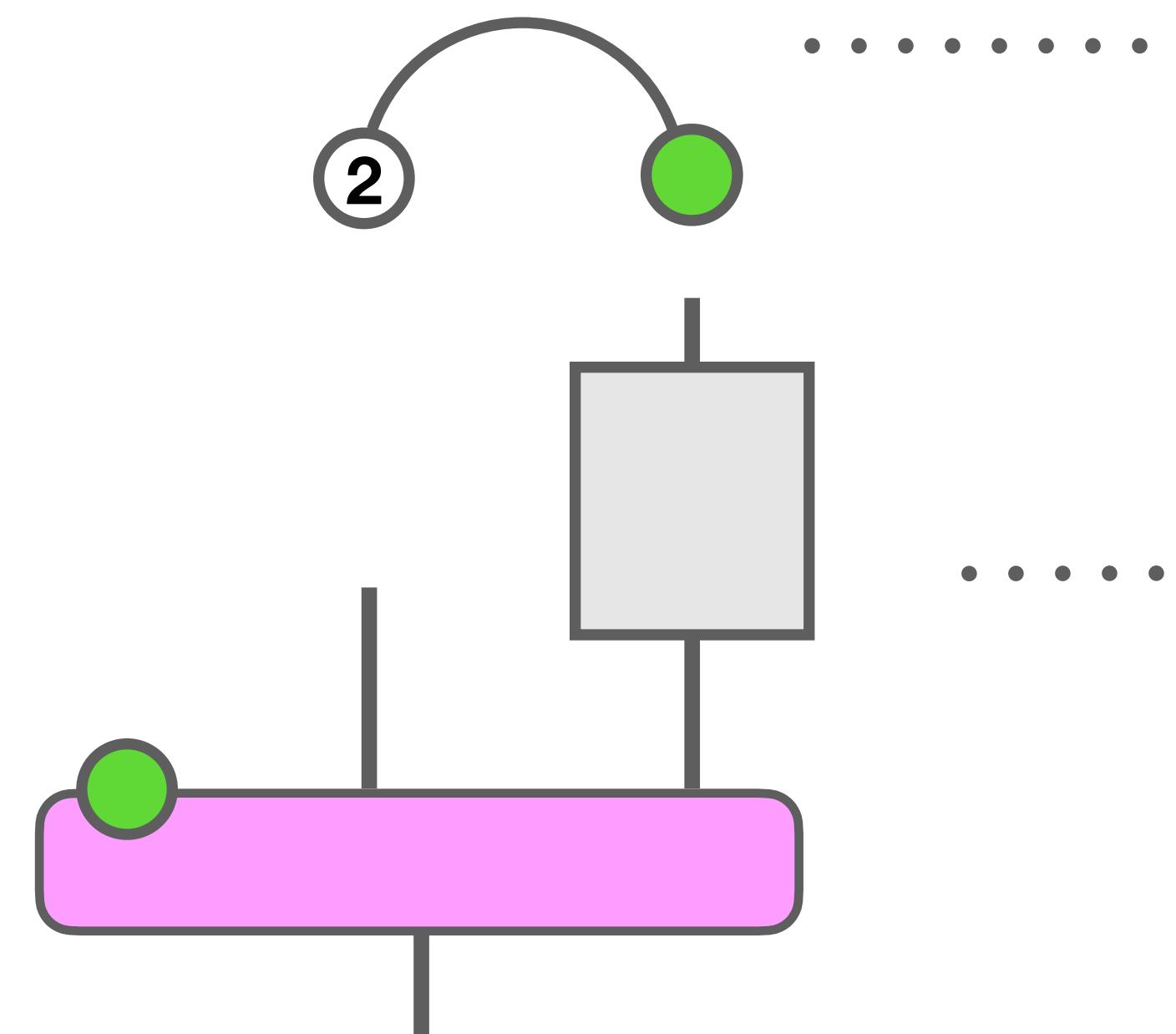


Durable Execution

In-progress Activities



- persisted recipes
- restartable



inputs

- available or *promised*
- persistable

continuation

- with *captured* values
- persistable

Durable Execution

Durable Execution

- **execution state always as data**

Durable Execution

- **execution state always as data**
- introspectable

Durable Execution

- **execution state always as data**
- introspectable
- opens possibilities

Durable Execution

- **execution state always as data**
- introspectable
- opens possibilities
 - visualize

Durable Execution

- **execution state always as data**
- introspectable
- opens possibilities
 - visualize
 - visualize mid-execution

Durable Execution

- **execution state always as data**
- introspectable
- opens possibilities
 - visualize
 - visualize mid-execution
 - edit mid-execution

Durable Execution

- **execution state always as data** Omitted “details”
- introspectable
- opens possibilities
 - visualize
 - visualize mid-execution
 - edit mid-execution

Durable Execution

- **execution state always as data** **Omitted “details”**
 - Serialization
- introspectable
- opens possibilities
 - visualize
 - visualize mid-execution
 - edit mid-execution

Durable Execution

- **execution state always as data**
 - visualize
 - visualize mid-execution
 - edit mid-execution
 - introspectable
 - opens possibilities
- Omitted “details”**
- Serialization
 - pluggable for custom data types

Durable Execution

- **execution state always as data** **Omitted “details”**
 - Serialization
 - pluggable for custom data types
 - Persistence
- introspectable
- opens possibilities
 - visualize
 - visualize mid-execution
 - edit mid-execution

Durable Execution

- **execution state always as data**
 - **introspectable**
 - **opens possibilities**
 - **visualize**
 - **visualize mid-execution**
 - **edit mid-execution**
- Omitted “details”**
- **Serialization**
 - pluggable for custom data types
 - **Persistence**
 - storage format

Durable Execution

- **execution state always as data**
 - introspectable
 - opens possibilities
 - visualize
 - visualize mid-execution
 - edit mid-execution
- Omitted “details”**
- Serialization
 - pluggable for custom data types
 - Persistence
 - storage format
 - graph?

Durable Execution

- **execution state always as data**
 - introspectable
 - opens possibilities
 - visualize
 - visualize mid-execution
 - edit mid-execution
- Omitted “details”**
- Serialization
 - pluggable for custom data types
 - Persistence
 - storage format
 - graph?
 - single document?

Durable Execution

- **execution state always as data**
 - introspectable
 - opens possibilities
 - visualize
 - visualize mid-execution
 - edit mid-execution
- Omitted “details”**
- Serialization
 - pluggable for custom data types
 - Persistence
 - storage format
 - graph?
 - single document?
 - Orchestration

Durable Execution

- **execution state always as data**
 - **introspectable**
 - **opens possibilities**
 - visualize
 - visualize mid-execution
 - edit mid-execution
- Omitted “details”**
- Serialization
 - pluggable for custom data types
 - Persistence
 - storage format
 - graph?
 - single document?
 - Orchestration
 - coordinator, workers, scheduler, ...

Durable Execution

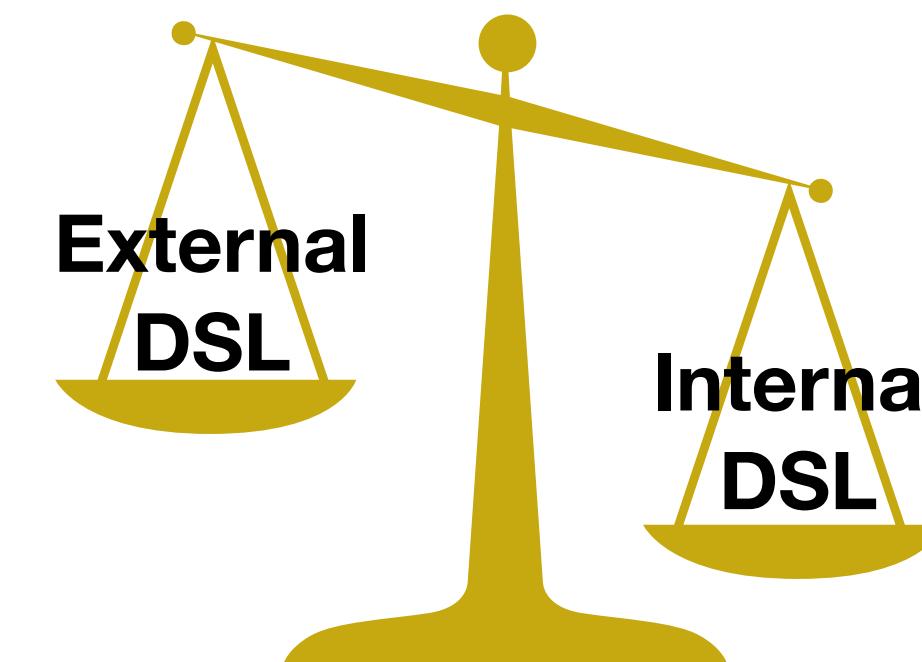
- **execution state always as data**
 - introspectable
 - opens possibilities
 - visualize
 - visualize mid-execution
 - edit mid-execution
- Omitted “details”**
- Serialization
 - pluggable for custom data types
 - Persistence
 - storage format
 - graph?
 - single document?
 - Orchestration
 - coordinator, workers, scheduler, ...
 - Externally completable promises

Distinctly Scala in Action

- Extension Methods `flow(expr)`, `expr switch { ... }`
- Extractors `case id ** history =>`
- Context Functions
`def delambdify[A, B](f: LambdaContext ?=> Expr[A] => Expr[B]): Flow[A, B]`
- Givens
- Opaque Types `Expr`
- Polymorphic Functions `sum: [X, Y] => (Flow[X, R], Flow[Y, R]) => Flow[X ++ Y, R]`
- lightweight Macros (source position, var names)
- Path-dependent types (not seen here, but heavily used in the library)

Take Aways

- **Programs-as-data** open new possibilities
- Does not take much to represent expressive control flows
- **Variables problematic**
 - Avoid internally to make some **illegal programs unrepresentable**
 - **Affordable** translation to point-free via canned implementation
- Expanding the case for internal DSLs



Thank you!

<https://github.com/TomasMikula/libretto/tree/main/lambda-examples>